



# Two different jumping mechanisms of water striders are determined by body size

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Current theory for surface tension-dominant jumps on water, created for small- and medium-sized water strider species and used in bioinspired engineering, predicts that jumping individuals are able to match their downward leg movement speed to their size and morphology such that they maximize the takeoff speed and minimize the takeoff delay without breaking the water surface. Here, we use empirical observations and theoretical modeling to show that large species (heavier than ~80 mg) could theoretically perform the surface-dominated jumps according to the existing model, but they do not conform to its predictions, and switch to using surface-breaking jumps in order to achieve jumping performance sufficient for evading attacks from underwater predators. This illustrates how natural selection for avoiding predators may break the theoretical scaling relationship between prey size and its jumping performance within one physical mechanism, leading to an evolutionary shift to another mechanism that provides protection from attacking predators. Hence, the results are consistent with a general idea: Natural selection for the maintenance of adaptive function of a specific behavior performed within environmental physical constraints leads to size-specific shift to behaviors that use a new physical mechanism that secure the adaptive function.

locomotion | water strider | allometry | jumping | biomechanics

Scaling relationships among morphological traits, the biomechanical mechanisms in which they are used, and the adaptive behaviors they serve, are the outcomes of combinations of organism's biological features, physical constraints from the organism's environment, and the nature of traits' functions (1–13). Compared to the allometry among morphology and structural components (4, 6, 8), the allometric relationship between the morphology and behavioral/biomechanical mechanisms is relatively less studied. Surface tension-dominant locomotion of water striders (14–20) provides a unique opportunity to study the relationship between morphology and behavior that clearly serves an antipredatory function under the constraints imposed by the physical properties of water surface.

Water striders (Gerridae) are true bugs (Insecta: Hemiptera) that live on the surface of water (21). They experience physical constraints on locomotion as water surface can break when the load exceeds the force resulting from surface tension of water (17–19). Studies on several water strider species have shown that they are able to jump up vertically from the unbroken water surface (18, 19, 22, 23) in response to predatory attacks from below (24, 25). These species are known to have a Weber number around 0.1 (16, 26, 27), indicating that their jumping thrust is mainly derived from surface tension rather than drag force. The theoretical model (19) allows us to understand how water striders optimize their jumping performance within the physical constraints of water surface properties. It predicts that water surface breaks during a jump if the value of  $\Omega M^{1/2}$  exceeds  $4/L + 0.1$  (a threshold indicated with the black broken line in Fig. 1; mathematical symbols are explained in Table 1 and the basic formulae are explained in the caption of Fig. 1). The function involves three dimensionless variables (19): downward stroke ( $L$ ; an indication of how far the leg can reach downward during a jump), angular leg velocity ( $\Omega$ ), and body mass ( $M$ ). Water striders adjust the angular velocity of their downward leg movements ( $\Omega$ ) to the species-specific downward stroke,  $L$ , that largely depends on the midleg length, and to the species-specific body mass ( $M$ ) such that they maximize the takeoff speed and minimize the takeoff delay without breaking the water surface. This optimal behavior  $\Omega$  observed in small and medium water strider species is marked as the green-shaded “observed” area of jumps located just under the theoretical threshold in Fig. 1 (19).

The jumping behavior was studied in only several Palearctic/Nearctic water strider species with body weights below 50 mg (18, 19, 22, 23), which corresponds to midleg lengths smaller than  $L = 10$  (referred to as typical mid-size water striders; *SI Appendix, Fig. S1*). They

## Significance

Water striders live on the water surface and jump to escape from underwater predators. They utilize the surface tension to achieve high jump efficiency from the water surface without breaking it. We report that the world's largest water striders jump with breaking the water surface. Our theoretical model shows that it is beneficial for larger species to use both drag and surface tension in jumping with water surface breaking, whereas small species only benefit from surface-tension-dominant jump. The simulation results and empirical observations demonstrate that these two behavioral phenotypes based on different physical principles are the outcome of predation pressure toward the water striders of different body sizes who spent life on the surface of water.

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The authors declare no competing interest.

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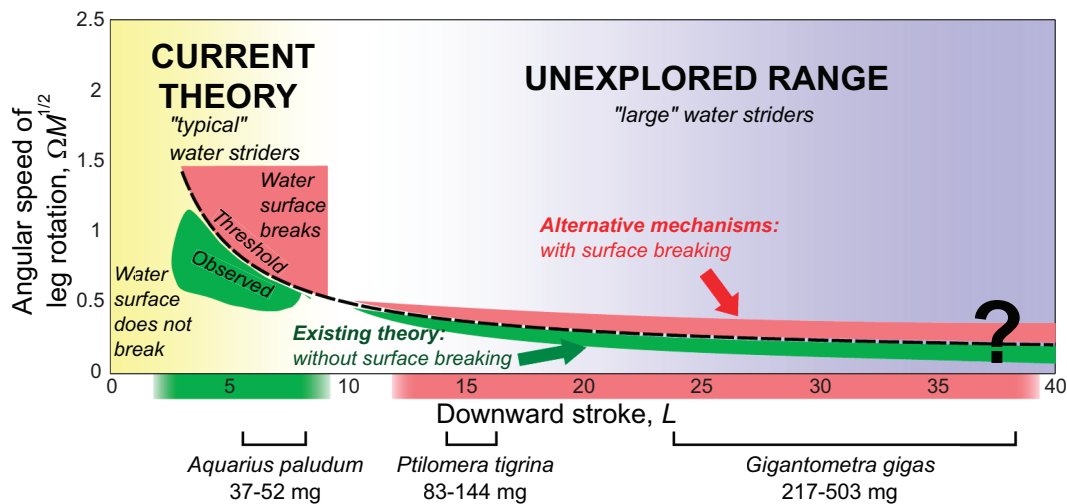
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**Fig. 1.** Graphical explanation of the research aims. Theoretical model (19) proposes an optimized surface tension jumping strategy for smaller water strider species weighing up to ~50 mg (indicated by the yellow shaded area on the *Left* side of the panel). These species have leg lengths up to ~3 cm, which corresponds to dimensionless downward strokes of up to ~10 ( $L = \Delta l/l_c$ ; explanations of mathematical symbols are in Table 1) indicated by the green shaded area under the horizontal axis. Angular velocity of leg rotation during a jump,  $\omega$ , is expressed as a nondimensional variable,  $\Omega = \omega(l_c/g)^{1/2}$  and is combined with a nondimensional measure of body mass,  $M = m/(\rho l_c^2 C_{l,w})$ , into one function,  $\Omega M^{1/2}$ . Yang et al. (19) empirically determined that the angular speeds of downward leg rotation by the “typical” water striders locate in the observed green shaded area under the black broken line marking the threshold described by the formula:  $\Omega M^{1/2} = 4/L + 0.1$ . The pink shaded area above the threshold line represents jumps that lead to the breaking of water surface and lower jump performance (19).  $\Omega M^{1/2}$  was treated by Yang et al. (19) as an index of angular speed of leg downward movement rotation because an individual water strider has control over their leg speed but not body weight. We asked whether two large subtropical water strider species, *Gigantometra gigas* ( $L$  up to 40; body weight 217 to 503 mg) and *Ptilomera tigrina* ( $L$  between 14 and 16; body weight 83 to 144 mg), use relatively low angular speeds of midleg rotation (green shaded area below the threshold line) and follow the same physical principles for surface tension powered jumps as the small species, or they jump with water surface breaking by using higher angular speeds of midleg rotation resulting in  $\Omega M^{1/2}$  value above the threshold line.

represent a fraction of the morphological diversity among Gerridae including large species in subfamilies Gerrinae and Ptilomerinae (*SI Appendix, Fig. S1B*). We were interested in the applicability of this theory to the jumps of the larger sized water striders (“unexplored range” shaded in violet in Fig. 1 and see also *SI Appendix, Fig. S1*). We considered two feasible mechanisms involved in jumps of the large water striders (Fig. 1): a) according to the current theory, the large water striders do not break the water surface when they jump, or b) the large water striders break the water surface resulting in different biomechanics, perhaps similar to the basilisk lizards running on water (28, 29) or fishing spider galloping and jumping on water (30). We suspected that the second mechanism is possible because the large body size may cause a shift in the jumping mechanism toward a relatively high role of drag forces [i.e., mechanisms characterized by the higher Weber number (16)].

We first focused on the world’s largest water strider, *Gigantometra gigas* [Fig. 2A; (31, 32)], to study their jumping in natural habitats and to provide a theoretical model of the biomechanics of jumping on water by these heavy water striders. After confirming that the giant water striders break the water surface during jumping (second mechanism), we built a theoretical model to predict the water strider’s body size at which the allometric switch (from the first mechanism to the second mechanism) is expected, and we tested the predictions using observations of jumps in another previously unstudied large species, *Ptilomera tigrina*, with body mass of 83 to 144 mg, as well as in the previously studied typical medium-sized water strider *Aquarius paludum* with body mass of 37 to 52 mg.

## Results and Discussion

**Empirical Observations and Kinematics of Jumps in *G. gigas*.** The detailed research on jumping behavior was carried out on the giant water striders, *G. gigas* (Fig. 2A), from the population in Pu Mat National Park, Vietnam (see *SI Appendix, Tables S1, S2, and S4* for morphological data). We were able to trigger vertical jumps in

freely skating giant water striders in their natural habitat (*Movie S1 and SI Appendix, Supplementary Materials PARTS 2 and 3*) by imitating predator attacks from under the water surface or by creating quick movements in their visual field. We observed that *G. gigas* as well as the other large-sized water strider, *P. tigrina*, broke the water surface when they jumped on the water surface (*SI Appendix, Tables S5 and S6*). The insects jumped upward to the height of about 10 to 30 cm (2.5 to 10 times their body length). Next, we filmed 57 upward jumps from a stationary position by 17 individuals in an experimental basin setup in the field (example in *Movie S1*). We analyzed in full detail the three best clips with male water striders (we chose males in order to test the world-largest water striders; males are larger than females, *SI Appendix, Table S1*) facing the camera and performing relatively symmetrical (left and right) coordinated leg movements (Fig. 3 and *SI Appendix, Figs. S5 and S6*). The remaining nondigitized jumps showed generally similar characteristics comprising three phases: surface tension phase, transition phase, and drag phase (see below).

From the detailed analysis of jumps it was evident that a jump starts with the pure surface tension phase (Fig. 2B1), which ends at the moment when the surface starts breaking under at least one of the midlegs. The surface tension phase is then followed by a transition phase, during which the midlegs’ tarsi and tibia gradually break the water surface until they are entirely immersed in the water (Fig. 2B2; yellow-shaded vertical bands in Fig. 3 and *SI Appendix, Figs. S5 and S6*). After midlegs entirely break the water surface, the drag phase begins. During the drag phase, the midlegs’ tarsi and tibia surrounded by air caught within (air sheath, Fig. 2F) and around (air bubble, Fig. 2B3 and E) the layer of densely packed hairs (Fig. 2D2 and G1) are moving downward through the water (i.e., providing upward drag; Fig. 2B2, B3, and E) pushing the body upward until the legs themselves reach the deepest point and start moving upward. The air bubble starts detaching from the midleg usually after the moment when midleg reaches the deepest point (except for only 2 cases in *SI Appendix,*

**Table 1. Explanations of the symbols used in the model and present in the main text. Full list of all symbols with descriptions is presented in *SI Appendix, Table S11***

Explanations of the symbols appearing in the main text

$L = \Delta l_i / l_c$	Downward stroke: dimensionless maximal reach of the average of two midlegs [scaled by the capillary length, $l_c$ (originally used in ref. 19)]
$\Omega = \omega(l_c/g)^{1/2}$	Dimensionless angular velocity of the average four legs' rotation of a jump (originally used in ref. 19)
$M = m/(\rho l_c^2 C l_w)$	Dimensionless index of insect body mass with respect to the leg; body mass with respect to maximal water mass can be displaced by the average of four legs (originally used in ref. 19)
$L_m = \Delta l_i / l_c$	Midleg downward stroke; dimensionless maximal reach of the midleg (modified $L$ for midleg only)
$\Omega_m = \omega_e(l_c/g)^{1/2}$	Dimensionless angular velocity of midleg rotation of a jump (modified $\Omega$ for midleg only)
$M_m = m/(\rho l_c^2 C_{m0} l_m)$	Dimensionless index of insect body mass with respect to the midleg; body mass with respect to maximal water mass can be displaced by the midleg (modified $M$ for midleg only)
$\omega$	Angular velocity of midleg rotation of a jump
$\omega_e$	Derived angular velocity of midleg rotation of the empirical jump
$\omega_t$	Hypothetical angular velocity of midleg rotation of the hypothetical jumps (i.e., surface tension jumps of <i>Gigantometra gigas</i> and <i>Ptilomera tigrina</i> ; drag-involving jump of <i>Aquarius paludum</i> )
$\omega_c$	Critical angular velocity of leg rotation; For a given midleg length and body mass, descending midleg can produce a dimple of the critical dimple depth, $h_c$ , with $\omega_c$
$D_b$	Duration of dimple breaking
$l_c = [\sigma/(\rho g)]^{1/2}$	Capillary length
$\Delta l_i = l_i - y_i$	Maximal downward reach of the midleg
$l_w$	Wetted length of the leg
$l_i$	Entire length of the midleg consisting of femur, tibia, and tarsus
$l_m$	Constant wetted length of midleg (the length of tibia plus tarsus of the midleg)
$y_i$	Initial height of the body center from the undisturbed free surface
$\sigma$	Surface tension coefficient of water
$\rho$	Density of water
$g$	Gravitational acceleration
$m$	Mass of the water strider
$C$	Flexibility factor; function of wetted length of a leg, $l_w$ , and its bending rigidity, $B$
$C_{m0}$	Midleg flexibility factor; function of wetted length of a midleg, $l_m$ , and its bending rigidity, $B$ (bending rigidity is explained in <i>SI Appendix, Table S11</i> ).
$E$	Young's modulus of insect cuticle
$r$	Radius of the wetted midleg as a cylinder
$r_b$	Radius of the wetted midleg as a cylinder surrounded by air bubble

Table S7). The hindlegs usually do not break the water surface, but maintain the dimple and provide the thrusting force stemming from surface tension (*SI Appendix, Fig. S15*).

A volume of air was captured by a midleg during and after surface breaking. We differentiated this volume of air into the portion caught in the "air sheath" and the portion caught in the "air bubble". The former is the air captured inside the hair layer, which remains attached during the leg movement and the latter is the air surrounding the leg that is detached from the leg and slowly floats upward to the surface (Fig. 2B4; see more details in *SI Appendix, Fig. S10*). Based on the size of the detached bubbles, we evaluated that the volume of air bubble around one midleg ranges from 10 to 80 mm<sup>3</sup> (*SI Appendix, Table S8*).

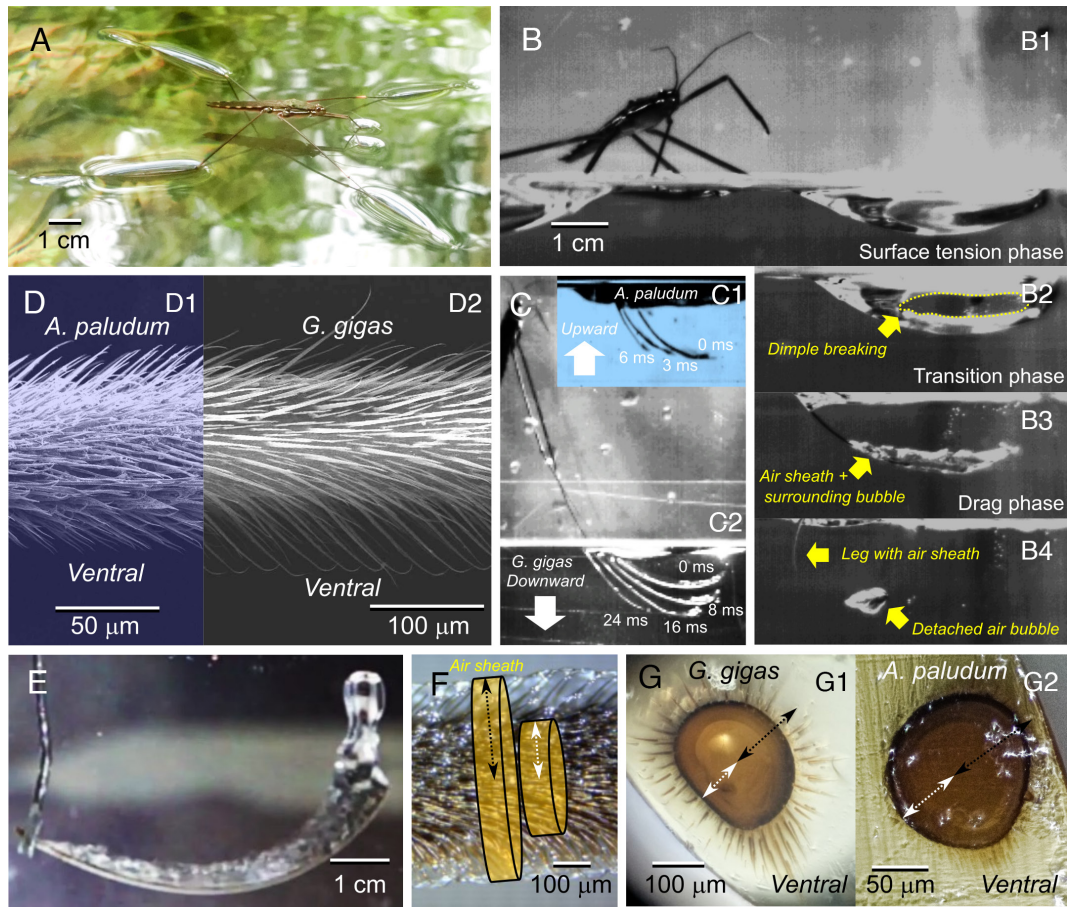
Finally, after the downward midleg movement stops and the leg reaches the deepest point, an additional small increase in momentum (hence, in body speed) may occur (present in Fig. 3 and *SI Appendix, Fig. S5* but not in *SI Appendix, Fig. S6*) for several milliseconds (<10 ms). It appears that during this time hindlegs create a dimple of constant depth (*SI Appendix, Fig. S15 A and C*), and the wetted hindleg length gradually decreases. The abrupt and short increase in the angular downward velocity by hindleg's femur (Fig. 3 B1 and C1 and *SI Appendix, Fig. S5 B1 and C1*) is a consequence of body

pitch change (head-upward/abdomen-downward; *SI Appendix, Fig. S15C*).

The momentum gained in the surface tension phase was from ~0.12 to ~0.28 g m/s, while the momentum values gained during the transition and drag phases were 0.20 to 0.22 g m/s and 0.04 to 0.12 g m/s, respectively (the means from the five repeated measures in each of 3 jumps/videos; Fig. 3A4 and *SI Appendix, Figs. S5A4 and S6A4*). Examination of Fig. 3 and *SI Appendix, Figs. S5 and S6* suggests that after midlegs reached the deepest point, the momentum gain was less than 0.05 g m/s, if noticeable at all. The transition and drag phases together contributed to an increase in body speed by 0.6 to 1.1 m/s, comprising approximately 50% of the speed achieved at the end of the surface tension phase. The maximum body speed near leaving the surface was 1.1 to 1.6 m/s (red arrows in Fig. 3A2 and *SI Appendix, Figs. S5 and S6*).

#### Theoretical Model Based on the Empirical Observations.

Inspired by the observations of jumps in *G. gigas*, we created a theoretical model of water strider's upward jumping. We modified the previous model (19) by a) considering midlegs and hindlegs separately, b) introducing transition and drag phases, in which



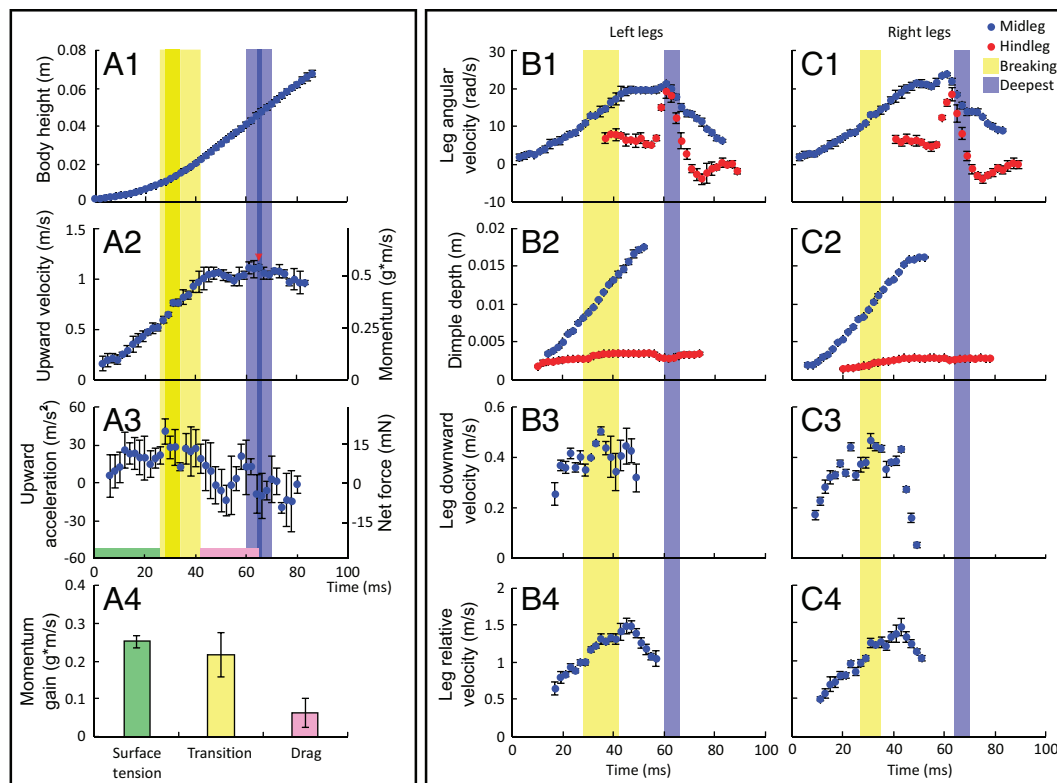
**Fig. 2.** Photographic explanation of how the giant water strider (*G. gigas*) jumps on water, including morphological adaptations on midlegs to capture air during penetration of the water. (A) *G. gigas* on the water surface. The hindleg's tibiae and tarsi press the surface downward and create dimples during jumping; (B) The midleg's femur+tibia+tarsi functional unit moves downward while bending and deforming the surface of water to create a dimple (B1), which eventually starts to break (B2), and each midleg continues to operate as a bending rod-like functional unit pushing down in the water after complete breaking (B3) and creating upward drag force. Air sheath is caught among the long hairs on midleg's tibia and tarsus (D2, F, and G1) and an additional air bubble surrounds the legs (B3), contributing to the drag force. Finally, the midlegs slide out and leave air bubbles (B4). (C) Stacked frames from a jump, starting with the moment right after surface breaking (0 ms) in *A. paludum* and *G. gigas*; in *A. paludum*, midlegs move upward after breaking (C1), the legs of *G. gigas* move downward in the water (here up to 16 ms from the moment of breaking the surface); (D) SEM image of midleg tibia of the giant water strider (D2) compared with *A. paludum* (D1); (E) a frame from a high-speed movie (Movie S1) of the midleg experimentally pushed downward in the water to illustrate the presence of air bubble surrounding the fast-moving leg; (F) midleg tibia in water in static situation: the layer of air sheath captured in the hairs around the leg increases the effective radius of the leg; (G) cross-section of the midleg's tibia to illustrate the distribution of hairs: relatively shorter hair on *A. paludum* (G2), and longer hair on *G. gigas* (G1). In (F) and (G), the white broken line with arrowheads indicates the actual radius of the leg while the black broken line with arrowheads indicates the effective radius that captures air sheath and creates drag force (with additional air bubble caught during leg downward). The radius of leg with hair capturing air sheath is marked as  $r$ , and the radius of leg with the surrounding air bubble is marked as  $r_b$  in the model and in Fig. 5. Photo credits: P. G. Jablonski, J. Ha, W. Kim & S.-i. Lee.

midlegs are surrounded by air sheath and capture air bubbles, c) allowing midlegs to reach deeper dimple depths before the water surface breaks depending on their length, d) assuming that the hindlegs create only the capillary force without breaking the surface. Therefore, our model calculates upward thrust from surface tension (capillary force before breaking the surface) or/and upward drag (after completely breaking the surface) of descending midlegs while adding the surface tension from hindlegs. In the transition phase (during breaking), midlegs provide both capillary and drag force.

We assumed that the air bubble is detached from the leg after it reaches the deepest depth (SI Appendix, Table S7). Additionally, we assumed that the left and right legs move in a synchronized manner (this synchronization makes shorter transition phase than empirically observed) with an angular velocity of leg rotation ( $\omega$ ) calculated according to the assumptions and formulae explained by Yang et al. (19). The surface tension phase was modeled according to the existing model (19) with an addition of the role of surface tension applied on hindlegs by assuming that their dimple depth grows in the same

way as the dimple of the midlegs until it reaches its constant depth specific for hindlegs (constant dimple depth,  $h_{hm}$ , empirically derived in SI Appendix, Supplementary Materials PARTS 9 and 10). We also permitted deeper maximum dimples for both midlegs and hindlegs (see page 38 in Supplementary Materials) owing to longer and more elastic legs in the giant water strider compared to the typical water striders (based on the empirical observations and measurements in SI Appendix, Figs. S12 and S13).

For a given midleg length and body mass, if the angular velocity of leg downward rotation is lower than the critical angular velocity of leg rotation,  $\omega_c$ , the descending midleg produces a dimple that is shallower than the critical dimple depth,  $h_c$ , at which water surface breaks. In contrast, the midleg with the angular velocity of leg rotation higher than  $\omega_c$ , breaks the water surface because the dimple exceeds the critical depth,  $h_c$ , at the critical moment,  $t_c$ . The value of  $h_c$  used in the model was determined empirically and found to depend on the size of the water strider, specifically the length of the midleg tibia and tarsus (as shown in SI Appendix, Fig S13A). When the midleg reaches the depth of  $h_c$ , the transition phase begins. In



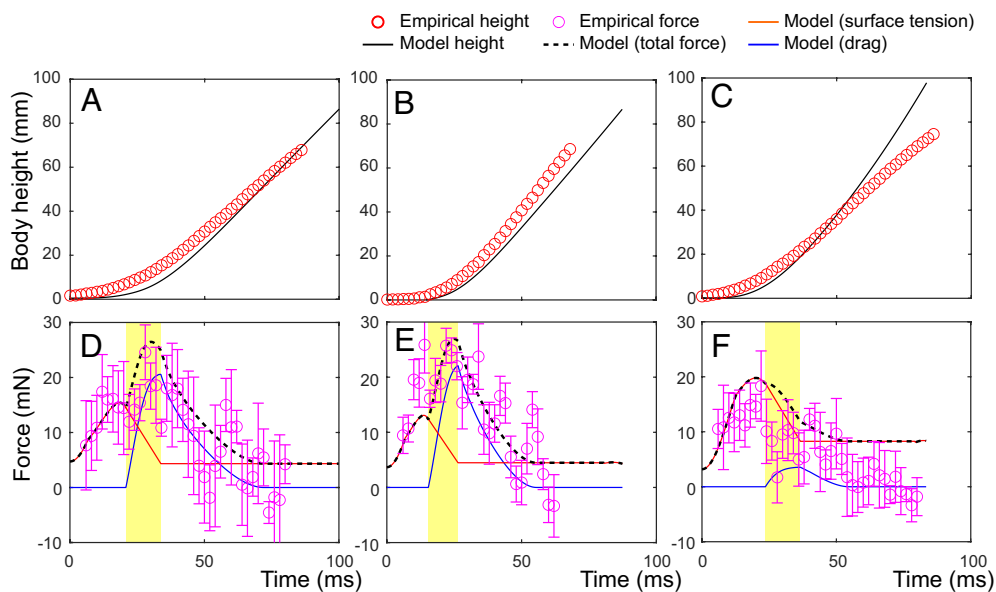
**Fig. 3.** Empirical analysis of the kinematics and dynamics of the jumping on water by the giant water strider, *G. gigas*. (A) variables obtained from the body movement: changes in body height above the water surface (A1), body velocity (A2) and body acceleration (A3) during the jump. Right side axes in A2 and A3 indicate the changes in body momentum (A2) and net force (A3) during the jump calculated from the body movement and body mass. A4 shows the comparison between the values of momentum gained during the three phases of jump: the surface tension phase (green), the transition phase (yellow), and the drag phase (purple). (B and C) contain variables concerning the Left (B) and Right (C) midlegs (blue circles) and hindlegs (red circles in B1, B2, C1, and C2): angular downward velocity (B1 and C1), depth (B2 and C2), downward velocity (B3 and C3) and downward velocity relative to the body position (B4 and C4). Yellow band across the panels indicates the transition phase for Left and Right separately in (B) and (C), which are overlaid on each other in (A). Blue bands across the panels indicate the bubble detaching duration for left and right leg separately. Red arrow in A2 indicates the moment of maximal body velocity. Filled circles and error bars indicate means and SDs, respectively, from 5 independent runs of frame-by-frame manual analysis of the same clip (EVT16). Leg depth (B2 and C2), leg velocity (B3 and C3), and relative leg velocity (B4 and C4; relative to the body center) were measured only until the moment soon after the deepest point was reached because afterward the detection of the deepest point was unreliable in the video. All the remaining variables are measured until the water strider loses contact with water. Results from analyses of two other jumps are in *SI Appendix, Figs. S5 and S6*.

the transition phase, the water breaking happens over the duration,  $D_b$ , and midlegs experience both capillary and drag forces. The value of  $D_b$  used in the model was also determined empirically to depend on the water strider size (length of midleg tibia + tarsus; *SI Appendix, Fig. S14*). After the surface is completely broken (drag phase begins), the legs are fully immersed in the water and are bent such that a large portion of midleg tarsus and tibia is roughly horizontal (Fig. 2C2) while descending in the water and creating upward drag force for the jump. The drag phase was modeled assuming a rod, with the length equal to the vertical downward projection of the immersed section of a bent midleg and the radius equal to either the radius of midleg's tarsus and tibia covered with air sheath and with or without air bubble (*SI Appendix, Supplementary Materials PART 7*), moving downward with the speed that is a by-product of midleg's angular velocity and the ascending water strider's body velocity. In the drag phase, the role of surface tension on hindlegs was modeled by using the empirically derived constant dimple depth,  $h_{bm}$ , during the jump after the constant depth is reached, and wetted leg length, which was calculated at each moment during a jump from femur leg length and body height above the water (*SI Appendix, Figs. S16 and S30–S32*).

**Model Validation.** Using empirically derived values of the angular velocity of midleg rotation ( $\omega_e$ ), the model reasonably predicted the insect trajectories in the specific videos of jumping *G. gigas*

males (Fig. 4A–C). The model also provided a reasonable fit with empirically estimated upward force (Fig. 4D–F), including the contribution of the air bubble around midleg's tibia and tarsus during the transition and drag phases. To expand the model for the smaller species, we tested the model predictions using an extra assumption that regardless of the species/body size, the ratio of wetted midleg radius with air bubble to the radius without air bubble is equal to the average value of these ratios from the fourteen individuals of *G. gigas* analyzed in detail (*SI Appendix, Table S8*). The model simulations correctly predicted body center height trajectories during empirically described jumps of *G. gigas* females and *P. tigrina* individuals (*SI Appendix, Fig. S19*). The angular velocities of midleg rotation ( $\omega_e$ ) for these individuals were derived from empirical observations of midleg coordinates and velocities for *G. gigas*, *P. tigrina*, and also *A. paludum* (*SI Appendix, Figs. S20–S23*).

**Model Simulations of Jumps for Four Size Classes.** We used the model to predict jump outcomes (Fig. 5) for body weights and leg lengths corresponding to four size classes of three species of water striders (from the smallest to the largest, consistent with Fig. 1): *A. paludum* female, *P. tigrina*, *G. gigas* females, *G. gigas* males. We used males and females of *G. gigas* separately due to the strong body size dimorphism in this species. *P. tigrina* does not show strong body size dimorphism. We observed females of *A. paludum*



**Fig. 4.** Comparison of the theoretical model predictions (lines) of body height trajectory and thrust force from theoretical simulations with empirically derived values (circles) from the three specific jumps of *G. gigas*. Theoretically calculated height (black solid line) and the empirically measured height (red circles) in the jumps of *G. gigas* are represented in A–C for the three analyzed videos: EVT16, EVT05 (2), and EVT41, respectively (shown in Fig. 3 and *SI Appendix*, Figs. S5 and S6). Calculated forces from the model for each video are represented in D–F for EVT16, EVT05 (2), and EVT41, respectively. The black dashed lines show the total generated force from two midlegs and two hindlegs. The orange and blue solid lines represent surface tension and drag, respectively. The purple circles represent the empirical force calculated from each movie by using body mass and acceleration with gravitational force added. The yellow shades represent the transition phase.

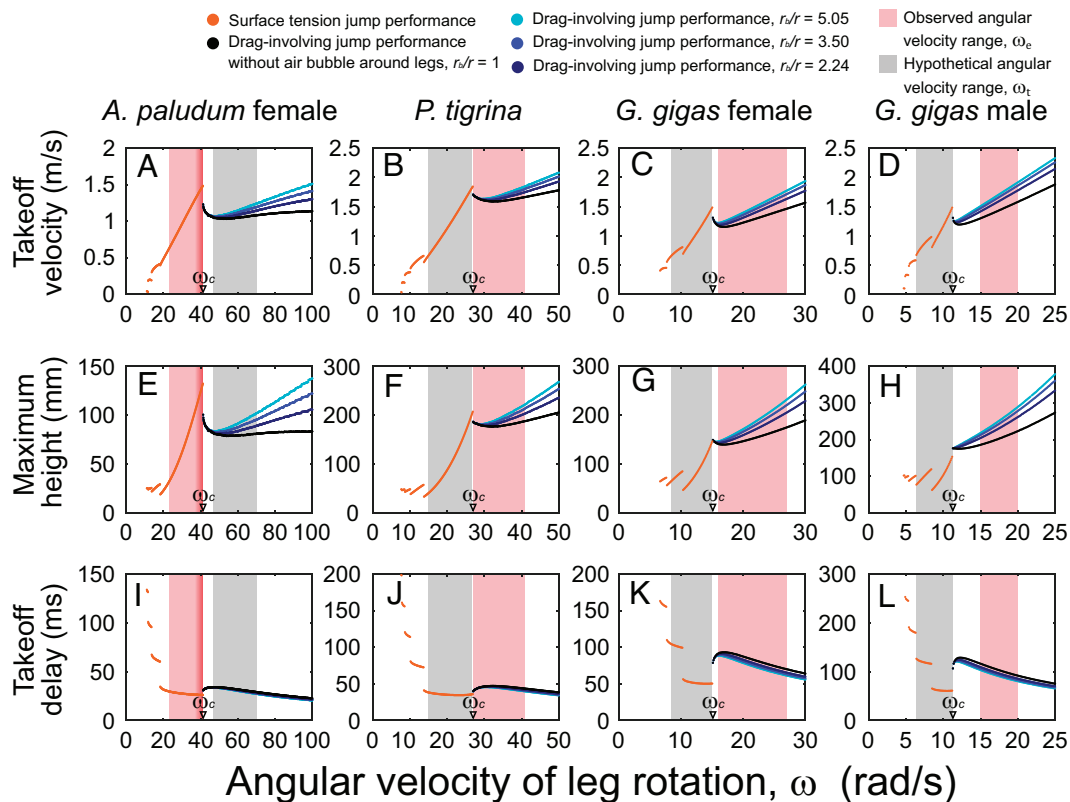
as the largest size class among the “typical-sized” water striders. Those predictions were calculated for a wide range of values of the angular velocity of midleg rotation ( $\omega$ ; on the horizontal axes in Fig. 5 and See *SI Appendix*, Table S13 for the specific values of parameters used in each simulation), and are shown as either orange dots or dots in one of the four colors (black, dark blue, blue, and light blue) in Fig. 5 representing performance during surface tension and drag-involving jumps, respectively.

These results allow us to compare the theoretically predicted jumping performance (takeoff velocity, takeoff delay, and maximum height) of each size class of water striders (represented by average body size for each class) for various angular midleg velocities, including the velocities actually used by the water striders ( $\omega_e$ , observed in precisely digitized jumps of multiple water striders of each species/sex classes, *SI Appendix*, Table S9; marked by vertical red shades in Fig. 5) and those that are only hypothetical/theoretical ( $\omega_t$ , marked by vertical gray shades in Fig. 5). This hypothetical angular velocity ( $\omega_t$ ) is the one that results in the absence of drag force in large species and results in existence of drag force in *A. paludum*. The ranges of hypothetical angular leg velocities for each of the three large classes (who perform drag-involving jumps) were determined by using the ratio  $\omega_e/\omega_c$  of *A. paludum*, while those for *A. paludum* (who performs surface tension jumps mostly) were determined by using the average ratio  $\omega_e/\omega_c$  of the three large classes (see details in *SI Appendix*, Supplementary Material PART 14).

We also calculated predictions using a range of values for Young’s modulus of insect cuticle,  $E$ , (Fig. 5 and *SI Appendix*, Figs. S24 and S25), as well as a range of the ratio of the wetted midleg radius with air bubble to the radius without air bubble (black, dark blue, blue, and light blue dots in Fig. 5 and *SI Appendix*, Figs. S24 and S25). Young’s modulus affects the critical angular velocity of the leg rotation,  $\omega_c$ , but not the general results from the model (compare Fig. 5 and *SI Appendix*, Figs. S24 and S25). The presence and increased size of the air bubble generally improve the performance of drag-involving jumps (as shown in Fig. 5 and *SI Appendix*, Figs. S24 and S25).

**Simulation Predictions for the Larger Water Striders.** For consistency among Figs. 1, 5, and 6, the model results are arranged from the smallest to the largest body size class in Fig. 5. As we built the model based on the largest water striders, we present the results for *Gigantometra* and *Ptilometra* first, before comparing them with the smaller species (*A. paludum*). The results demonstrate that if the large water striders had used the hypothetical lower angular velocities of midlegs ( $\omega_t$ ) than the critical surface-breaking velocity ( $\omega_c$ ,  $\sim 11.3$  rad/s,  $\sim 15.1$  rad/s, and  $\sim 27$  rad/s for *G. gigas* male and *G. gigas* female, and *P. tigrina*, respectively; marked on  $x$  axis of Fig. 5 for  $E = 10$  GPa) their jumping performance would have been lower than their actual jumping performance involving  $\omega_e$ . Relatively higher takeoff velocity (Fig. 5 B–D) and greater jumping height (Fig. 5 F–H) are likely to contribute to the success in avoiding attacks by underwater predators such as fish that snatch prey from the water surface. While, on average, the predicted takeoff delay across the gray shade appears not that different from the average predicted takeoff delay across the red-shaded band of  $\omega_e$  (Fig. 5 J–L), the hypothetical jumps by large water striders just below the critical value,  $\omega_c$ , may perform better in terms of shorter takeoff delay but then the body velocity and jump height would be lower than in drag-involving jumps.

Fish, in general, can reach speeds of about 1.4 m/s [median for maximal speed from 45 studies on 14 species (33), *SI Appendix*, Fig. S27]. Based on these data, we theoretically estimated that the maximum height of the hypothetical upward “jumps” (into air) by fish in pursuit of escaping (jumping) water strider would range from approximately 50 to 150 mm (lower and upper quartiles in *SI Appendix*, Fig. S27 B and C). Hence, the large water striders performing surface-breaking (i.e., drag-involving) jumps would be able to jump equal to or faster and/or higher than the fish within a presumably sufficiently short time (takeoff delay approximately up to 100 ms; Fig. 5 J–L) to escape capture. However, if they had performed surface tension jumps, the takeoff velocities and jump heights would not likely have been sufficient to escape from the fish, especially for the heaviest class (*G. gigas* males; Fig. 5 D and H).

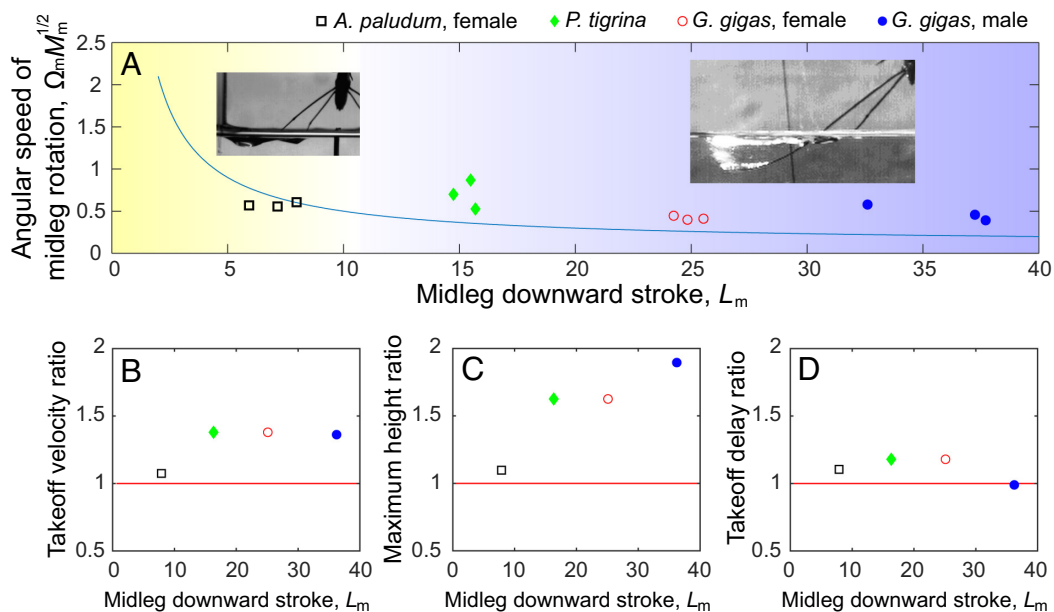


**Fig. 5.** Theoretically predicted jump performance as a function of midleg angular velocity for four classes of water striders' body size based on *A. paludum* females, *P. tigrina*, *G. gigas* females, and *G. gigas* males when  $E = 10$  GPa. Jump performance measured by three variables calculated by the model: takeoff velocity (A–D), maximum jump height (E–H), takeoff delay (I–L). Average empirical values (mass, leg length for each leg section, leg radius, initial height of the body) for each body size class were used to simulate the jumps for each body size class across a wide range of angular velocity of leg rotation (x axis). Orange dots represent surface tension jumps, and other dots represent drag-involving jumps. The radius ratio of 5.05, 3.5, 2.24, and 1 (i.e., no bubble situation) are represented as light blue, blue, dark blue, and black dots, respectively. The red-shaded vertical bars represent the ranges of the observed leg angular velocity values ( $\omega_e$ ). For smaller species, known to be able to precisely adjust their leg angular velocity in order to perform just under the threshold line (19, 22), a narrow band is additionally marked with darker shade for the range of  $\omega_e$  values that represent jumps in this optimal situation. The gray-shaded vertical bars represent the range of the hypothetical leg angular velocity ( $\omega_t$ ) for *A. paludum* using drag in their jumps, and for the other large species using surface tension jumps. The angular velocity of leg rotation,  $\omega_e$ , values were determined from slow motion jumping videos as explained in the *SI Appendix, Supplementary Materials PART 14* and shown in *SI Appendix, Table S9*. The performance of drag-involving jumps was calculated for three sizes of air bubble surrounding the leg: minimal, maximal, and average. Similar figures for Young's modulus of 5 and 15 GPa are shown in *SI Appendix, Figs. S24 and S25*.

Therefore, we hypothesize that the jumps observed in large water striders produced by midlegs' angular velocities that lead to surface breaking should help the insects to escape predatory attacks, while the hypothetical surface tension jumps produced by hypothetical (not observed in nature) lower angular velocities of midlegs might put large water striders under more serious risk of predation due to relatively slow speed and low jump height. In the simulation of *P. tigrina*, we found that within a narrow range of  $\omega$ , the optimal performance of surface tension jumps was equivalent to the performance of drag-involving jumps. However, since *P. tigrina* prefers fast-flowing habitats (34) where the maximum depth of dimple is expected to be shallower than in stagnant water (30), we hypothesize that this peak performance for surface tension jumps may not be achievable in their natural environment.

Finally, the results show that the presence of air bubbles around midlegs improves the performance of drag-involving jumps by enlargement of projected areas of thrusting legs (Fig. 5 and *SI Appendix, Figs. S24 and S25*). In our study, we assumed that this layer of air bubble enhances the drag because it increases the radius of a solid cylinder imitating the midleg in the model. However, the observed air bubble was dragged by the midleg while changing its shape (Fig. 2B), and we hypothesize that the air bubble of constantly changing shape may change the leg's drag coefficient and potentially enhance the drag more than just enlarging the projected area of the thrusting leg.

**Simulation Predictions for the Smaller Water Striders.** Unlike the larger water striders, the smaller water strider species such as *A. paludum* can achieve efficient escape without surface breaking (Fig. 5 A, E, and I; for  $E = 10$  GPa), if they are able to precisely adjust the leg velocity to their individual body mass (as suggested earlier in refs. 19 and 22) such that their  $\omega_e$  values lie just below the critical value,  $\omega_c$  (dark red shades on the right side of red-shaded vertical band in Fig. 5 A, E, and I). If they used leg angular velocity higher than the body size-specific critical value, the jump performance would become dramatically worse as already described by Yang et al. (19), and confirmed by us via considering drag calculations. This performance decrease cannot be recovered within the expected hypothetical range of ( $\omega_t$ , gray vertical shade) by faster leg velocity (even with the maximum volume of air bubble; Fig. 5 A and E). In order to achieve a performance comparable to the best performance in the surface tension jumps, this smaller species would need to use extremely fast angular leg velocities of 70 to 100 rad/s (Fig. 5 A, E, and I), which may not be easily achievable, or if achievable it may require more energy than the surface tension jumps. Even if they were achievable, they would not provide more protection from predatory attacks because the achievable performance of the hypothetical drag-involving jumps of *A. paludum* (Fig. 5 A, E, and I) is predicted to be lower or not higher than the best performance in the surface tension jumps



**Fig. 6.** Summary of the results. (A) empirically observed jumps in the four classes of water striders (from the smaller to the larger), *A. paludum* females, *P. tigrina*, *G. gigas* females, *G. gigas* males, in the simplified phase diagram based on the original model of surface tension jumping [Yang et al. (19); see Fig. 1] with the theoretical water surface breaking threshold line (blue solid line) to illustrate that large water striders use water surface breaking jumps that involve drag (inset photos). (B–D) comparison of the theoretically calculated performance in drag involving and surface tension dominant jumps for the four size classes of water striders: the points indicate the estimated ratios calculated by dividing the midpoint of performance (takeoff velocity in B, maximum height in C, and takeoff delay in D; all calculated based on Fig. 5) in the drag-involving jumps by the analogical midpoint of performance in the surface tension jumps. The black empty squares, green filled diamonds, red empty circles, and blue filled circles represent *A. paludum* females, *P. tigrina*, *G. gigas* females, and *G. gigas* males, respectively. In B–D, the red lines represent a ratio of 1, where the performances of drag-involving jumps and surface tension jumps are equal.

(i.e., those jumps with the observed leg velocity,  $\omega_e$ ) that is closer to the critical value,  $\omega_c$  (dark red shades in Fig. 5 A, E, and D).

We also observed a range of various values of  $\omega_e$  in individuals of various body sizes (SI Appendix, Table S9). Using the lower values of  $\omega_e$  within this range to theoretically predict jumping performance of a female with an average body mass (48 mg; average mass for *A. paludum* females, SI Appendix, Table S3) resulted in a relatively poor performance (left side of the red-shaded vertical band in Fig. 5 A, E, and D) compared to the performance for larger  $\omega_e$  values, highlighting the importance of leg rotation adjustment to body size for these water striders in performing surface-dominant jumps near the critical value,  $\omega_c$ .

These model predictions allow us to understand why smaller species, who are known to perform near the threshold (19), would not use the drag-involving jumps. Direct empirical observations provide further explanations. In our previous empirical studies (18, 19, 22), we have occasionally observed surface breaking in the smaller species jumping in the laboratory conditions. The breaking occurred in the final moments of jump when the tibia-tarsi section was more-or-less vertically oriented ( $>45^\circ$  to horizontal; example in Fig. 2C1), and the insect moves upward (Fig. 2C1) preventing the immersed leg, including its leg tips, moving downward (i.e., the leg could not create upward drag force, or even might provide downward drag force). Additionally, we noticed that the midlegs of the typical smaller water strider species, such as *A. paludum*, seem not to create pronounced air sheaths in the water presumably due to shorter hairs on the legs (Fig. 2D and G), further diminishing the role of drag for powering the jump in these water striders.

**Comparison of the Larger and Smaller Water Striders.** Taken together, our results provide an understanding of why jumping behaviors of the three classes of large water striders with body mass ranging from  $\sim 80$  to  $\sim 500$  mg and midleg downstroke

( $L_m$ ) ranging from  $\sim 15$  to  $\sim 38$  (*G. gigas* males, *G. gigas* females, and *P. tigrina*) do not conform to the relationship between size and leg angular velocity within the surface-tension-dominated mechanism of jumping (Fig. 6A), while jumping of *A. paludum* females with body mass of  $\sim 40$  to  $\sim 50$  mg and  $L_m$  of  $\sim 6$  to  $\sim 8$  occurs in accordance with the theory of surface tension jumping. According to calculations based on the theoretical model (19), it is possible for large water striders to jump without breaking the water surface if they rotate their legs by 38 to 67% of their current angular velocity (SI Appendix, Table S5; using threshold line in Fig. 6A). However, the performance of their surface tension jumps would be worse than that of drag-involving jumps (Fig. 6B and C), and it would not protect them from attacking predators.

In contrast, one of the largest classes of typical water striders, *A. paludum* females, does not achieve noticeably better jump performance with drag-involving jumps than with surface tension jumps (black square in Fig. 6B and C) is located near the ratio value of 1). Hence, the shift from surface tension jumps to drag-involving jumps is predicted to occur in the species whose size lies between *A. paludum* and *P. tigrina*, (SI Appendix, Fig. S1), i.e., within the range of dimensionless midleg length ( $L_m$ ) from  $\sim 8$  to  $\sim 15$ , corresponding to the midleg length between 26 and 44 mm and body mass between  $\sim 50$  and  $\sim 80$  mg (maximal *A. paludum* = 54 mg, minimal *P. tigrina* = 83 mg).

Previous studies (16, 26, 27) have determined that water strider locomotion is characterized by the Weber number of about 0.1, and our data of *A. paludum* female confirm this knowledge (an average value of 0.17 among individuals in Fig. 6A). However, our results demonstrate that Weber number can be around 2 for jumps of the large water striders (1.75, 2.91, and 1.55 for *G. gigas* male, *G. gigas* female, and *P. tigrina*, respectively; average values among individuals in Fig. 6A and SI Appendix, Table S10) indicating that drag plays an important role, similar to fishing spiders galloping and jumping on water (30). Unlike the basilisks (28, 29), this



locomotion of large water striders does not include the fast slapping of the water surface, but it includes fast downward expansion of an already existing dimple beyond the point of breaking, leading the capture of air bubbles. Published data on several small water strider species (18, 19, 22, 23), combined with our observations of *A. paludum*, *P. tigrina*, and *G. gigas*, match the model predictions but currently there is not enough information on jumping behavior of a variety of species within Gerridae to fully evaluate the central prediction of the model: Evolutionary transitions from smaller to larger body size along branches of Gerridae phylogenetic tree will be associated with transitions from surface-tension to drag-involving jumps, especially in habitats of high predation risk where achieving sufficiently high jumping performance is important to evade predatory attacks. Future comparative studies of a variety of small and large water strider species should be able to more precisely determine the body size and midleg length at which the transitions occur. The two subfamilies of water striders, Gerrinae and Ptilomerinae, are promising study taxa because of their wide range of species body sizes (*SI Appendix, Fig. S1B*) and a variety of the habitats that they use.

**General Conclusions.** In summary, drag-involving jumps allow large water striders to achieve performance that is comparable to the surface tension jumps of the smaller typical water striders, and appears sufficient to evade predatory attacks. Hence, the results suggest that selection for sufficiently fast jumping might have led to a change in the mechanisms of jumping in the large and heavy water striders, leading to evolution of specialized hairs on their midlegs' tibiae and tarsi that capture air and enhance the drag, which is important for their jumps. The results illustrate a general idea that natural selection for a specific outcome of behavior is influenced by physical constraints in certain habitats, which can break the theoretically expected scaling relationships predicted from the specific biomechanics of the behavior. As a result, a shift to a new mechanism may occur to ensure similar or better behavioral outcomes, such as escape performance from predators, and this mechanism may cause new morphological adaptations and different scaling relationships.

Many of the water strider robots developed thus far are relatively heavy [ $\sim 0.5$  to  $\sim 10$  g (35–45)]; except for the  $\sim 70$ -mg jumping robot (18) inspired by the theory for surface tension-dominant jumping (19)] compared to the size range of water striders studied in nature [ $\sim 10$  to  $\sim 50$  mg (17, 19, 46)]. In a recent study (27), it was shown that utilizing drag can be beneficial for large jumping robots. However, we illustrate here that in nature, adaptive pressure has already optimized the jumping behavior of large-sized water striders by shifting their behavior toward drag utilizing jumps. This highlights the importance of understanding the proximate physical mechanisms and natural selection pressures associated with animal locomotion in designing water walking robots.

## Methods

**Study Species and Locations.** The experiments on *G. gigas* were carried out in Pu Mat National Park, Vietnam. *P. tigrina* jumps were studied at two sites: near the Me Linh Station for Biodiversity (21°23'01.9"N 105°42'44.2"E = Google map: 21.383870, 105.712264); Vinh Phuc Province, Vietnam, and at the "May waterfalls" (Thac May; 20°21'51.4"N 105°26'51.6"E = Google map: 20.364275, 105.447665), in the vicinity of the Cuc Phuong National Park, Vietnam. *A. paludum* individuals used in research came from water bodies located in and near Seoul, S. Korea.

**Experiments.** Water striders were filmed using Trouble Shooter camera (TS 1000 set to 500 fps) in a  $30 \times 30$  cm<sup>2</sup> Plexiglas box filled with water. A second camera (Sony SR11) recorded from above simultaneously (*SI Appendix, Supplementary*

*Material PART 3: SI Appendix, Fig. S3*). Each individual was photographed and weighed immediately after a test (with few exceptions of individuals that escaped before measurements). Additional colored movies were filmed using a Sony RX-III camera. The photos included a ruler and were taken in a manner that allowed for body and length measurements from the photos.

**Digitizing and Analysis.** We chose three best-quality videos of male *G. gigas* for detailed digitization. The videos were digitized manually using MAXTRAQ program (see details in *SI Appendix, Supplementary Material PART 6*). Digitization and calculation were repeated 5 times to minimize potential human error and resolution noise. The velocities of the body and legs were based on the differences in positions of digitized points between consecutive frames. As the raw coordinates showed random fluctuations due to the errors in tracking, we used the moving average of three values of three consecutive frames: the preceding frame, the focal frame, and the following frame. The acceleration values were obtained in the same way from the velocity values (moving average of three consecutive values of acceleration). The momentum and force applied to the body were calculated from the velocity, acceleration, and the body mass according to standard formulas.

The jumping of *G. gigas* was divided into three phases. The surface tension phase lasted until the frame when the water surface started breaking under the midleg. The transition phase (marked with the yellow vertical band in Fig. 3 and *SI Appendix, Figs. S5 and S6*) lasted from the first frame with water breaking until the frame before the first frame when midlegs were entirely immersed (and surface tension did not contribute to the jump). The drag phase lasted from the first frame when midlegs were entirely immersed until the body center reached the maximum velocity. Cumulative momentum gained during each of the three jump phases was calculated in each jump. We also determined the moment when the air bubble formed and detached from the midleg. For each frame, we determined the angle between vertical line and hindleg's as well as midleg's (left and right leg separately) femur and used these values to extract angular velocity of legs (see details in *SI Appendix, Supplementary Materials PART 6*). The hindleg's maximum dimple depth was also digitized (see details in *SI Appendix, Fig. S9*) because it is crucial in the empirical analyses and in the mathematical model (*SI Appendix, Supplementary Materials PARTS 9 and 10*).

The total volume of air bubbles captured around the midleg during the drag phase was calculated by adding the volumes of all air bubbles formed by air detached from the leg during the last stages of the drag phase ( $n = 14$ , *SI Appendix, Table S8*). In volume calculations, we used the vertical diameter of each air bubble after its shape stabilized and approximated a sphere.

The dimensionless indices crucial in the mathematical model, the maximal downward reach of legs ( $L$ ) and the combination of leg downward angular speed with the insect mass ( $\Omega M^{1/2}$ ) were calculated for Fig. 6 based on the previous study (19). However, unlike in the original model (19) that used average leg length (from four legs: two hindlegs and two midlegs), we followed the reasoning introduced in the recent model correction (22), which we further modified: we used only the empirically established midleg length (*SI Appendix, Tables S1–S4*) in calculations of those indices (*SI Appendix, Tables S12 and S13*). We did not use hindleg length in the determination of  $L$  because their push downward is shallower even in the surface tension jumps (19, 22), and they do not enter deeper into the water in drag-involving jumps (i.e., do not break surface; see *SI Appendix, Fig. S15*).

**Theoretical Model and Simulations of Jumps.** *SI Appendix, Supplementary Materials PART 7–11 and 19* contain the detailed presentation of the core mathematical part of the model, and additional details concerning assumptions and parameters based on empirical observations. We assumed that the cuticle of water striders has Young's modulus similar to that of locusts, reported to be up to  $\sim 10$  GPa (47, 48). As the modulus of insect cuticles can vary widely (49, 50), We additionally run the model using values of 5 and 15 GPa.

We used the model to theoretically simulate jumps and to predict jump outcomes for body masses and leg lengths corresponding to four size classes based on real water striders from the three study species: (from the largest to the smallest): *G. gigas* males, *G. gigas* females, *P. tigrina*, *A. paludum* females. We used males and females of *G. gigas* separately due to the strong body size dimorphism in this species, and we used females of *A. paludum* because they represent the largest size from among the typical-sized water striders. Those predictions were calculated for wide ranges of values of the midleg angular velocity ( $\omega$ ) covering the surface tension-based and drag-involving jumps and were expressed as three measures of jump performance:

takeoff velocity, maximum jump height, and takeoff delay. *SI Appendix, Table S13* contains the specific values of parameters used in each simulation.

**Data, Materials, and Software Availability.** Datasets associated with analyses/figures are located in the [supporting information](#). The Matlab code for the theoretical model is available at Zenodo <https://doi.org/10.5281/zenodo.7847879> (51).

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## Supporting Information for

## Two different jumping mechanisms of water striders are determined by body size

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**Supplementary Materials PART 1.** Morphology of the study species: *Gigantometra gigas*, *Ptilomera tigrina*, and *Aquarius paludum*.

**Table S1.** Morphology of the giant water striders, *Gigantometra gigas*, from the study site in Pu Mat National Park, Vietnam.

Variable	Males	Females
Sample size (nr of individuals)	16	9
Mass (mean $\pm$ SD, min-max; mg)	414 $\pm$ 59, 316-511	265 $\pm$ 40, 217-318
Body length (cm)	3.52 $\pm$ 0.20	3.39 $\pm$ 0.32
<b>FRONT LEGS:</b>		
Tibia Thickness (mm)	0.41 $\pm$ 0.05	0.39 $\pm$ 0.04
Femur length (cm)	1.11 $\pm$ 0.10	1.00 $\pm$ 0.10
Tibia length (cm)	0.89 $\pm$ 0.07	0.75 $\pm$ 0.06
Tarsus length (cm)	0.27 $\pm$ 0.03	0.23 $\pm$ 0.03
Total leg length (cm)	2.27 $\pm$ 0.17	1.99 $\pm$ 0.15
<b>MIDLEGS:</b>		
Tibia Thickness (mm)	0.46 $\pm$ 0.08	0.39 $\pm$ 0.04
Femur length (cm)	4.84 $\pm$ 0.45	3.32 $\pm$ 0.28
Maximum wetted leg length (Tibia + tarsus length; cm)	5.35 $\pm$ 0.60	3.85 $\pm$ 0.24
Total leg length (cm)	10.19 $\pm$ 1.04	7.17 $\pm$ 0.43
<b>HINDLEGS:</b>		
Tibia Thickness (mm)	0.56 $\pm$ 0.09	0.40 $\pm$ 0.05
Femur length (cm)	4.95 $\pm$ 0.69	3.21 $\pm$ 0.11
Maximum wetted leg length (Tibia + tarsus length; cm)	7.35 $\pm$ 1.16	4.06 $\pm$ 0.50
Total leg length (cm)	12.30 $\pm$ 1.25	7.26 $\pm$ 0.57

**Table S2.** Morphology of the three individuals of *Gigantometra gigas* for whom the jumps were fully analyzed. Thickness of the tibia was measured near the femur/tibia joint as a diameter of leg measured along the horizontal line (parallel to the water surface in the normal position of a leg of a water strider standing on the water surface). The thickness is used in the model to calculate drag force after correction for the presence of air bubble that surrounds the leg moving in the water (see calculations in Supplementary Materials PART 7)

Clip name	Mass (mg)	Middle leg			Hind leg	
		Basal tibia thickness (mm)	Femur length (cm)	Constant wetted length: <i>tibia + tarsus</i> (cm)	Femur length (cm)	Constant wetted length <i>tibia + tarsus</i> (cm)
EVT16	483	0.455	4.809	5.460	4.742	7.948
EVT05 (2)	375	0.390	4.286	4.578	4.274	6.336
EVT41	325	0.475	4.913	5.405	4.824	7.717

**Table S3.** Morphology of *Ptilomera tigrina* from two study sites: the Melinh Station for Biodiversity, Vinh Phuc Province, Vietnam, and at the "May waterfalls" (Thac May) of the Cuc Phuong National Park, Vietnam; and morphology of *Aquarius paludum* females from Seoul, South Korea.

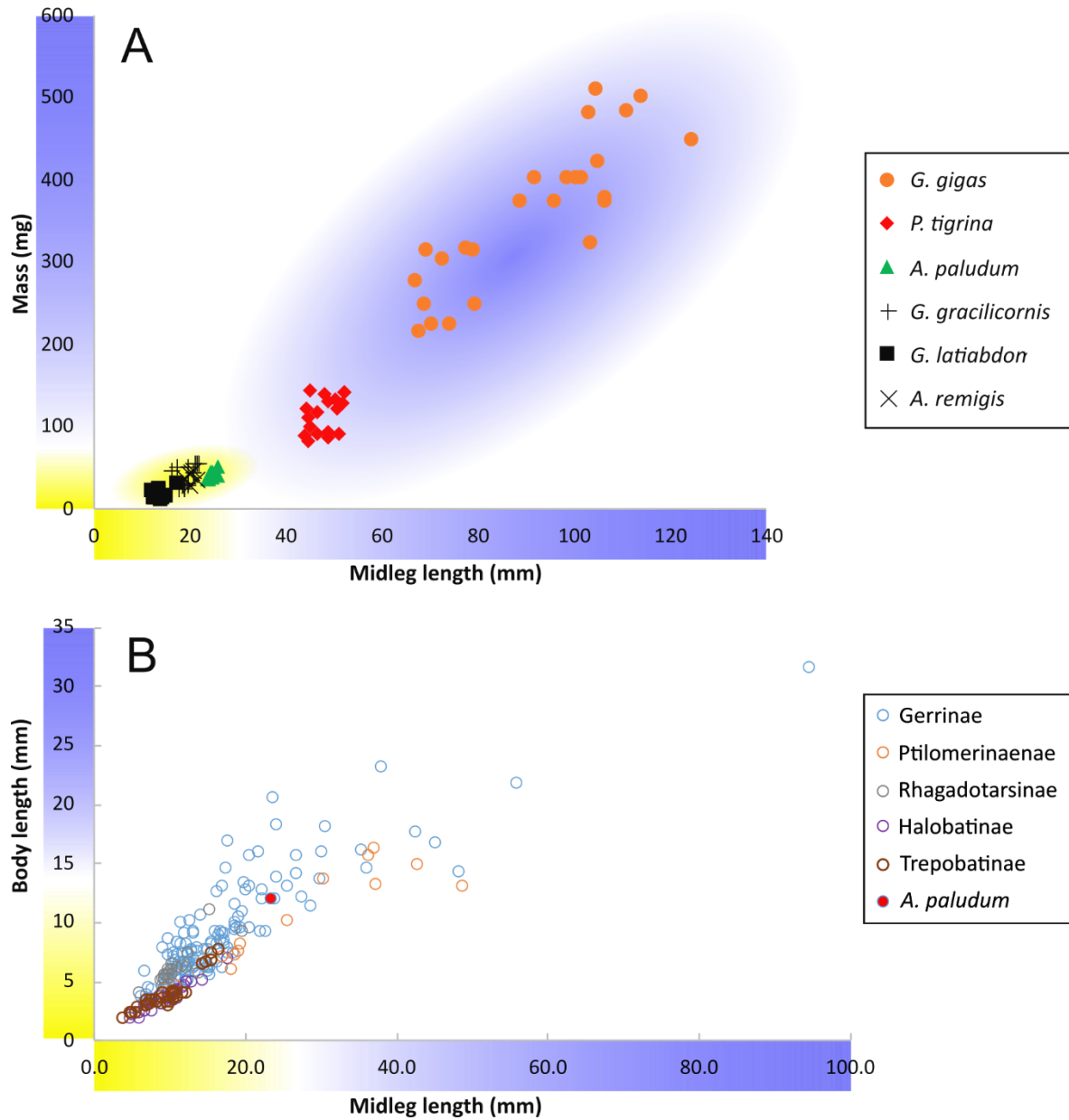
Variable	<i>Ptilomera tigrina</i>	<i>Aquarius paludum</i>
Sample size (nr of individuals)	18	8
Mass (mean ± SD, min-max; mg)	115 ± 22, 83-144	48 ± 4, 43-54
Body length (cm)	1.72 ± 0.08	1.55 ± 0.06
<b>MIDLEGS:</b>		
Tibia thickness (mm)	0.31 ± 0.03	0.18 ± 0.02
Femur length (cm)	2.40 ± 0.16	1.15 ± 0.10
Maximum wetted leg length (Tibia + tarsus length; cm)	2.39 ± 0.16	1.34 ± 0.07
Total leg length (cm)	4.79 ± 0.30	2.50 ± 0.16
<b>HINDLEGS:</b>		
Femur length (cm)	2.76 ± 0.23	1.21 ± 0.08
Maximum wetted leg length (Tibia + tarsus length; cm)	1.91 ± 0.19	0.95 ± 0.07
Total leg length (cm)	4.66 ± 0.42	2.16 ± 0.14

**Table S4.** The midleg downward stroke,  $L_m$ , the dimensionless angular velocity of middle leg rotation of a jump,  $\Omega_m$ , and the dimensionless index of insect body mass with respect to the middle leg,  $M_m$ , were calculated according to the following formula from Yang et al. (1), but modified to focus on the midleg, as  $L_m = \Delta l_l / l_c$ ,  $\Omega_m = \omega_e (l_c / g)^{1/2}$ ,  $M_m = m / (\rho_l^2 C_{m0} l_m)$ , because we observed that hindleg does not penetrate the water surface (see details in Supplementary Material PART 8, 19). The summary of these data is shown in Fig. 6.

Parameter/ variable (unit)	<i>G. gigas</i> male			<i>G. gigas</i> female			<i>P. tigrina</i>			<i>A. paludum</i> female		
	EVT05 (2)	EVT16	EVT41	EVT28	EVT33	EVT35	C0046	C0049	C0066	P_Female _evt25	P_Female _evt32	P_Female _evt33
$m$ (kg)	374.76e-6	483.23e-6	325.41e-6	305.67e-6	226.81e-6	226.81e-6	134e-6	134e-6	123e-6	48.5e-6	42.6e-6	42.6e-6
$y_l$ (m)	0.00017	0.00165	0.00088	0.00333	0.00435	0.00274	0.00271	0.00473	0.00806	0.00271	0.00473	0.00806
$l_l$ (m)	88.64e-3	102.69e-3	103.17e-3	72.59e-3	70.13e-3	70.13e-3	44.72e-3	44.72e-3	50.63e-3	0.02434	0.02413	0.02413
$l_m$ (m)	45.78e-3	54.60e-3	54.05e-3	39.80e-3	38.87e-3	38.87e-3	22.70e-3	22.70e-3	25.56e-3	13.56e-3	13.06e-3	13.06e-3
$\omega_e$	20	15	16	16	19	17	41	33	29	39	40	41
$L_m$	32.604	37.240	37.701	25.527	24.240	24.836	15.481	14.740	15.688	7.970	7.151	5.921
$\Omega_m$	0.333	0.250	0.266	0.266	0.316	0.283	0.682	0.549	0.483	0.649	0.666	0.682
$M_m$	3.029	3.369	2.169	2.388	1.993	1.993	1.624	1.624	1.190	0.874	0.696	0.696
$\Omega_m M_m^{1/2}$	0.579	0.458	0.392	0.411	0.446	0.399	0.869	0.700	0.526	0.607	0.555	0.569

**Table S5.** Calculations of theoretical threshold conditions for the large water striders, assuming that the surface-tension-dominant mechanism applies to the jumping by the large water striders (in Table S4). The table shows the predictions of the theoretical critical angular leg velocity values for the empirically observed body masses.

Species	Observed mass (mg)	Observed angular velocity (rad/s)	Theoretical critical angular velocity (rad/s)	Angular velocity ratio (theoretical /observed)
<i>G. gigas</i> male	483	15	6.79	0.45
<i>G. gigas</i> male	375	20	7.69	0.38
<i>G. gigas</i> male	325	16	8.41	0.53
<i>G. gigas</i> female	306	16	9.98	0.62
<i>G. gigas</i> female	227	19	11.28	0.59
<i>G. gigas</i> female	227	17	11.11	0.65
<i>P. tigrina</i>	134	41	16.90	0.41
<i>P. tigrina</i>	134	33	17.51	0.53
<i>P. tigrina</i>	123	29	19.56	0.67



**Fig. S1.** Relationship between body size and midleg length in the previously studied (yellow ranges on axes) and the unstudied (blue ranges on axes) species of Gerridae divided into 5 subfamilies. (A) the absolute midleg length (mm; the variable crucial for empirical biologists and directly related to the dimensionless downward stroke  $L$ , the key variable crucial in the theoretical hydrodynamic model of jumping and shown on the horizontal axis in Fig. 1) and the species body mass (empirical variable related to the dimensionless body mass  $M$ , contributing to the index of angular velocity of midleg rotation,  $\Omega M^{1/2}$ , which is the key variable the theoretical hydrodynamic model of jumping and is shown on the vertical axis in Fig. 1) for several species from the “typical” water striders (measured in this study: *Gerris latiabdominis*, *G. gracilicornis*, *Aquarius remigis*, *A. paludum*), and from the two large species that have rarely been studied before and were measured here (*Ptilomera tigrina* and *Gigantometra gigas*). (B) Reconstructed data from Table 16 in Matsuda 1960 (2). Matsuda states the unit converting rule on page 32: “In table 16, 82 units are equal to 10 mm. For those values with asterisks, 173.7 units are equal to 10 mm.” However, in comparison with our measurement data, the rule seems clearly to be a mistake. Therefore, we used the converting rule where ‘173.7 units are equal to 10 mm’, which leads to results consistent with our data on leg and body lengths directly measured by us from specimens. Yellow-shaded area indicates the range of body masses and leg lengths of small and medium sized Palearctic and Nearctic water striders that have typically been studied in the past. Blue-shaded area indicates body and leg lengths that have not been studied earlier. The data point for *A. paludum* is highlighted to indicate the largest of the species (belongs to Gerrinae) studied that uses surface-tension jump.



## Supplementary Materials PART 2: Description of the Supplementary Movies and links to additional movies deposited to Wikimedia.

### Description of the content of the supplementary video clips with the article:

**Supplementary Movie 1 – *Gigantometra gigas* jumping in the natural habitat and the water container and the bubble sheath around the leg.** Movie timeline: 1-3 s. – normal speed (1x); 4-10 s. – slowed down 8x; the clip shows two examples of upward jumps by the giant water strider and landing on the water surface (C0143). The water strider leaves the field of view in the video that was filmed at a closer distance (C0153). Movie timeline: 11-12 s. – normal speed (1x); 13-16 s. – slowed down 10x; the clip shows two examples of two different upward jumps by the giant water strider in the water container in the front (EVT16) and side view (EVT19). Movie timeline: 17-22 s. – slowed down 20x; the clip shows two examples around the leg of jumping water strider (EVT22 (2)) and dead leg striking into the water surface (C0143 dead leg).

**Supplementary Movie 2 – *Ptilomera tigrina* jumping in the water container and the bubble sheath around the leg.** Movie timeline: 1-3 s. – slowed down 4x; 4-6 s. – slowed down 16x; the clip shows two examples of two different upward jumps by the water strider in the water container in the front (C0046) and side view (C0049).

**Supplementary Movie 3 – *Aquarius paludum* jumping in the water container without breaking water surface.** Movie timeline: 1-3 s. – slowed down 4x; 4-6 s. – slowed down 20x; the clip shows an example of an upward jump by the water strider in the water container in the front (P\_female\_evt26) and side view (P\_female\_evt25).

### Description of the content of the additional video clips available at Wikimedia and You tube (with links):

**NATURAL HABITAT JUMP1.mp4.** The clip shows an example of an upward jump by the giant water strider. The movements are slowed down (0.0375 normal speed). The second smaller water strider jumping belongs to the genus *Ptilomera*. *The movie (C0143) was captured in the field at 239.76fps and saved in the standard format of 29.97fps, which was additionally slowed down to 30% of playback speed.*

Wikimedia:

[https://commons.wikimedia.org/wiki/File:Gigantometra\\_gigas\\_upward\\_jump\\_in\\_Natural\\_Habitat\\_Pumat\\_National\\_Park\\_Jump\\_1.webm](https://commons.wikimedia.org/wiki/File:Gigantometra_gigas_upward_jump_in_Natural_Habitat_Pumat_National_Park_Jump_1.webm)

Youtube: <https://youtu.be/2EuG5vT4YHs>

**NATURAL HABITAT JUMP 2.mp4.** The clip shows an example of an upward jump by the giant water strider. The movements are slowed down (0.125 normal speed). The giant water strider enters the field of view from the left. The smaller water strider on the right belongs to the genus *Ptilomera*. *The movie (C0153) was captured in the field at 239.76fps and saved in the standard format of 29.97fps, resulting in the slowdown of 0.125 relative to the normal speed.*

Wikimedia: [https://commons.wikimedia.org/wiki/File:The\\_giant\\_water\\_strider\\_\(Gigantometra\\_gigas;\\_Gerridae\)\\_Natural\\_Habitat\\_Jump\\_2.webm](https://commons.wikimedia.org/wiki/File:The_giant_water_strider_(Gigantometra_gigas;_Gerridae)_Natural_Habitat_Jump_2.webm)

Youtube: <https://youtu.be/iGN1gJBlk5k>

**NATURAL HABITAT JUMP3.mp4.** The clip shows an example of an upward jump by the giant water strider. The movements are slowed down (0.0375 normal speed). The second smaller water strider jumping belongs to the genus *Ptilomera*. *The movie (C0027) was captured in the field at 479.52 fps and saved in the standard format of 29.97fps, resulting in the slowdown of 0.0625 relative to the normal speed.*

Wikimedia: [https://commons.wikimedia.org/wiki/File:Gigantometra\\_gigas\\_\(Gerridae\)\\_Natural\\_Habitat\\_Jump\\_3.webm](https://commons.wikimedia.org/wiki/File:Gigantometra_gigas_(Gerridae)_Natural_Habitat_Jump_3.webm)

Youtube: <https://youtu.be/zyW-eV9kxs8>

**NATURAL HABITAT JUMP4.mp4.** The clip shows an example of an upward jump by the giant water strider filmed at a closer distance. The water strider leaves the field of view. The movements are slowed down (0.125 normal speed). The giant water strider enters the field of view from the left. *The movie (C0148) was captured in the field at 239.76fps and saved in the standard format of 29.97fps, resulting in the slowdown of 0.125 relative to the normal speed.*

Wikimedia: [https://commons.wikimedia.org/wiki/File:Gigantometra\\_gigas\\_\(Gerridae\)\\_Natural\\_Habitat\\_Jump\\_4.webm](https://commons.wikimedia.org/wiki/File:Gigantometra_gigas_(Gerridae)_Natural_Habitat_Jump_4.webm)

Youtube: <https://youtu.be/tCtFqIHHisU>

**NATURAL HABITAT JUMP5.mp4.** The clip shows a close-up on the water surface under the water strider legs. The movements are slowed down (0.01875 normal speed). At the end of the clip, several small bubbles of air, which was originally wrapped around midlegs during the drag phase of the jump, “pop-up” on the water surface after being dis-attached from the legs (visible in the supplementary video “JUMP IN THE BOX.mp4”). *The movie (C0086) was captured in the field at 959.04 fps and saved in the format of 59.94 fps, which was additionally slowed down to 30%.*

Wikimedia: [https://commons.wikimedia.org/wiki/File:Gigantometra\\_gigas\\_\(Gerridae\)\\_Natural\\_Habitat\\_Jump\\_5.webm](https://commons.wikimedia.org/wiki/File:Gigantometra_gigas_(Gerridae)_Natural_Habitat_Jump_5.webm)

Youtube: <https://youtu.be/bbwkCEwDtrA>

**JUMP IN THE TANK 1.AVI.** The clip shows an example of an upward jump by the giant water strider filmed by Trouble Shooter camera (TS1000) with 500 fps. This is one of the three movies analyzed (EVT16).

Wikimedia: [https://commons.wikimedia.org/wiki/File:Gigantometra\\_gigas\\_\(Gerridae\)\\_JUMP\\_IN\\_THE\\_TANK\\_1.webm](https://commons.wikimedia.org/wiki/File:Gigantometra_gigas_(Gerridae)_JUMP_IN_THE_TANK_1.webm)  
[https://commons.wikimedia.org/wiki/File:Gigantometra\\_gigas\\_\(Gerridae\)\\_Jump\\_in\\_Tank\\_1\\_annotated\\_EVT16\\_50%25.webm](https://commons.wikimedia.org/wiki/File:Gigantometra_gigas_(Gerridae)_Jump_in_Tank_1_annotated_EVT16_50%25.webm)  
Youtube: <https://youtu.be/wSd5EKYdPi8>

**JUMP IN THE TANK 2.mp4.** This clip shows a close up of the midlegs moving downward and surrounded by air bubble caught in the hair around the leg. Eventually, the legs are quickly moving upward and leave the air bubble, which forms air bubbles that travel slowly upwards towards the surface. This clip (*EVT22 (2) ind20*) was filmed by Trouble Shooter camera (TS1000) at 500 fps.

Wikimedia: [https://commons.wikimedia.org/wiki/File:Gigantometra\\_gigas\\_\(Gerridae\)\\_JUMP\\_IN\\_THE\\_TANK\\_2\\_70PERC.webm](https://commons.wikimedia.org/wiki/File:Gigantometra_gigas_(Gerridae)_JUMP_IN_THE_TANK_2_70PERC.webm)  
Youtube: [https://youtu.be/ReE8NOhjo\\_4](https://youtu.be/ReE8NOhjo_4)

**JUMP IN THE TANK 3.mp4.** This clip shows nearly symmetrical movements downwards of midlegs. The movements are slowed down (0.03125 normal speed). The air released from the legs under water creates small air bubbles that travel slowly upwards towards the surface. *The movie (C0041) was captured with Sony RX10-III at 959.04 fps and saved in the format of 59.94 fps, which was additionally slowed down to 50%.*

Wikimedia: [https://commons.wikimedia.org/wiki/File:Gigantometra\\_gigas\\_\(Gerridae\)\\_JUMP\\_IN\\_THE\\_TANK\\_3.webm](https://commons.wikimedia.org/wiki/File:Gigantometra_gigas_(Gerridae)_JUMP_IN_THE_TANK_3.webm)  
Youtube: <https://youtu.be/DagN4SMZOgc>

**JUMP IN THE TANK 4.mp4.** This clip shows a close-up on legs seen approximately from the side to illustrate that during fast leg downward movements the air bubble around the legs is extended along the direction of leg movements (also seen in the two other clips: JUMP IN THE TANK 2 and DEAD LEG DOWNWARD MOVE). Therefore we could imagine that a cross-section of leg including the air bubble may resemble an irregular ellipse rather than a circle. The drag force is proportional to the effective leg diameter, which is a function of the diameter of the leg plus the thickness of the air measured during downward movement in the plane perpendicular to the leg downward movement (see Supplementary Materials PART 7 for more details on how this aspect was simplified in the theoretical model). The movements are slowed down (0.015625 normal speed). *The movie (C0046) was captured with Sony RX10-III at 959.04 fps and saved in the format of 59.94 fps, which was additionally slowed down to 25%.*

Wikimedia: [https://commons.wikimedia.org/wiki/File:Gigantometra\\_gigas\\_\(Gerridae\)\\_JUMP\\_IN\\_THE\\_TANK\\_4.webm](https://commons.wikimedia.org/wiki/File:Gigantometra_gigas_(Gerridae)_JUMP_IN_THE_TANK_4.webm)  
Youtube: <https://youtu.be/DagN4SMZOgc>

**DEAD LEG DOWNWARD MOVE.mp4.** This clip shows how the air bubble is created around the midleg during fast downward movements in the water. The movements are slowed down (0.03125 normal speed). *The movie (C0143) was captured in the field at 959.04 fps and saved in the format of 59.94 fps, which was additionally slowed down to 50%.*

Wikimedia: [https://commons.wikimedia.org/wiki/File:Gigantometra\\_gigas\\_\(Gerridae\)\\_DEAD\\_LEG\\_DOWNWARD\\_MOVE.webm](https://commons.wikimedia.org/wiki/File:Gigantometra_gigas_(Gerridae)_DEAD_LEG_DOWNWARD_MOVE.webm)  
Youtube: <https://youtube.com/shorts/-f6E80VricM?feature=share>

### **JUMPING OF *AQUARIUS PALUDUM*:**

**Near-vertical jumps of water strider (*A. paludum*) slow motion.** - The video clip shows a slow motion of a water strider jumping upwards. Note the “dimples” under the legs and how they increase in depth while the legs push down and “bend” the water surface without breaking it. The model in *Nat Comm* 7, 13698 (2016) <https://doi.org/10.1038/ncomms13698> focuses on this ability of insects to jump upward without breaking of the water surface. It shows that this ability results in maximization of the jump speed and minimization of the latency between the jump initiation and leaving the water surface in the response to attacking predators.

Wikimedia: [Water-striders-adjust-leg-movement-speed-to-optimize-takeoff-velocity-for-their-morphology-ncomms13698-s2.ogv](https://commons.wikimedia.org/wiki/File:Water_striders_adjust_leg_movement_speed_to_optimize_takeoff_velocity_for_their_morphology_ncomms13698-s2.ogv)  
Youtube: <https://youtu.be/8sjSmX5pNw8>

**Water strider *A. paludum* jump side view.** - Slow motion video of the water strider *Aquarius paludum* jumping on the water surface. Side view reveals the backward leg movements. The speed is approximately 0.006 of normal speed.

Wikimedia: [https://commons.wikimedia.org/wiki/File:Water\\_strider\\_A\\_paludum\\_jump\\_side\\_view.webm](https://commons.wikimedia.org/wiki/File:Water_strider_A_paludum_jump_side_view.webm)  
Youtube: <https://youtu.be/cDwGRvFiNoM>

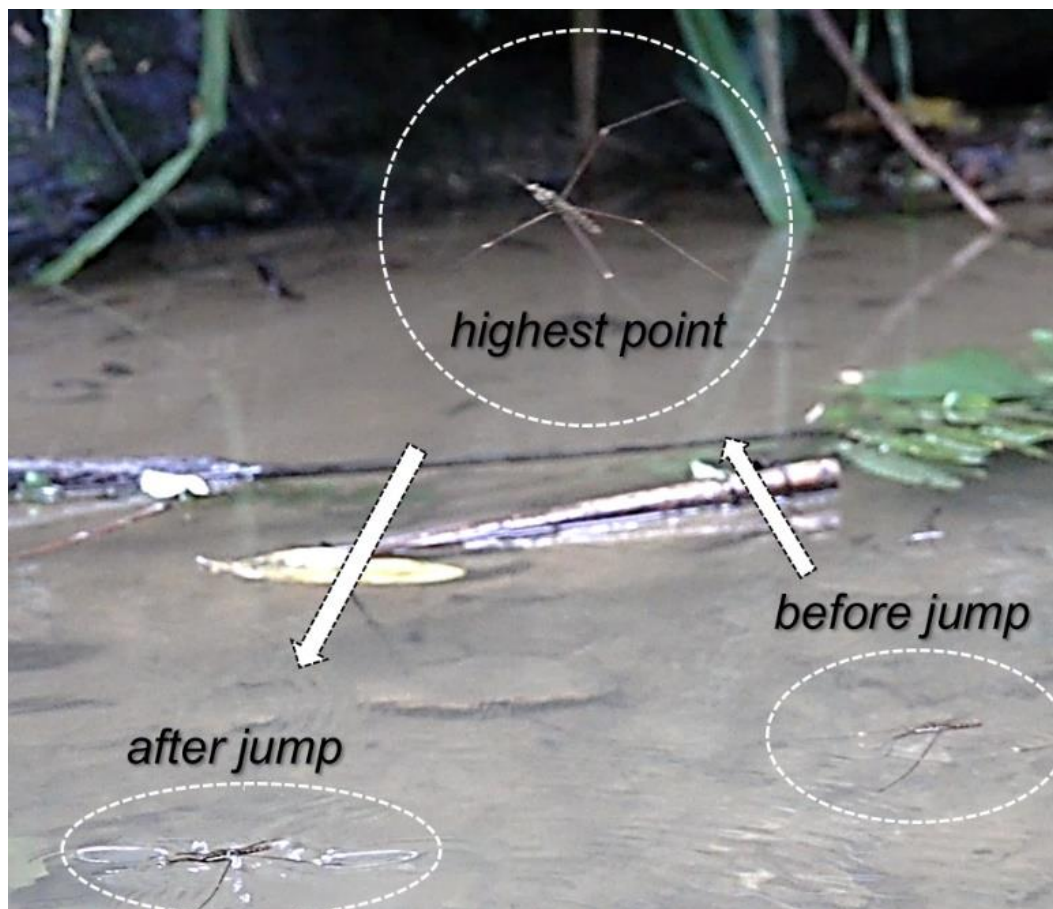
**Waterstrider *A. paludum* jump frontal view.** - Slow motion video of the water strider *Aquarius paludum* jumping on the water surface. Frontal view reveals the inward leg movements. The speed is approximately 0.006 of normal speed.

Wikimedia: [https://commons.wikimedia.org/wiki/File:Waterstrider\\_A\\_paludum\\_jump\\_frontal\\_view.webm](https://commons.wikimedia.org/wiki/File:Waterstrider_A_paludum_jump_frontal_view.webm)  
Youtube: <https://youtu.be/GLv7Ob16jLc>

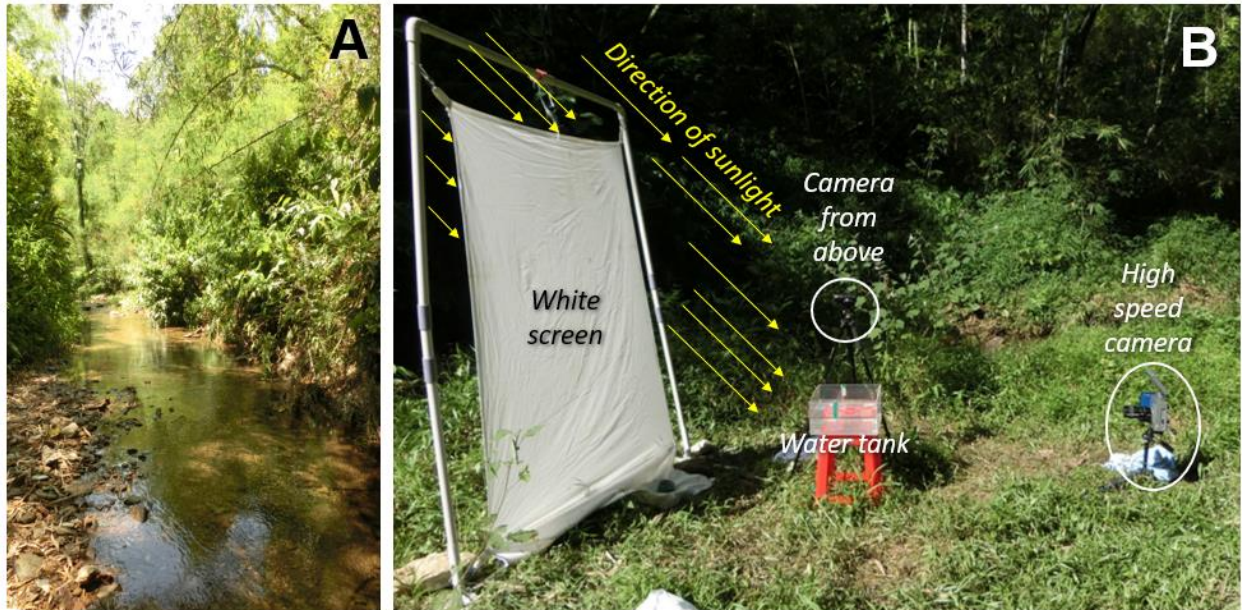
**Water strider *A. paludum* jump on solid substrate.** - This video of a water strider jumping on a solid substrate illustrates that the leg movements are composed of two phases. First phase comprises downward movement against the substrate surface (normally surface of water) dominates. The second phase comprises mostly horizontal movements: first backwards then inwards. When this happens on water, where each leg creates a dimple, the leg movements are associated with the dimple shifts backwards and then inwards. The speed is approximately 0.006 of normal speed.

Wikimedia: [https://commons.wikimedia.org/wiki/File:Water\\_strider\\_A\\_paludum\\_jump\\_on\\_solid\\_substrate.webm](https://commons.wikimedia.org/wiki/File:Water_strider_A_paludum_jump_on_solid_substrate.webm)  
Youtube: <https://youtu.be/4Sr0im-umSU>

**Supplementary Materials PART 3: Jumps of large-sized water striders.**



**Fig. S2. Jumping in the natural habitat.** An example of a record of one jump in the natural habitat. Three frames are put together here and photo-edited to represent the moment just before jump, the moment of reaching the highest point, and the moment right after landing on the water surface again. In the natural habitat, jumps of the giant water strider were triggered by imitating attacks from under the water surface using long bent sticks, or by creating a very fast visual stimulus by waving a sheet of paper in the visual field of the water strider. High speed movies were shot using Sony RX10-III. See details in Supplementary Movie 1.



**Fig. S3. Field methods.** (A) Study site in the natural habitat of the giant water strider in the Pumat National Park area. (B) Experimental setup used in the field to obtain high-speed movies of jumping giant water striders. A water strider was put in a transparent water tank. Jumping was triggered by poking the insect gently from under water using a hook-shaped wire. Battery-operated high-speed camera (TS 1000) was used to film the jump, while standard camcorder filmed it from above to provide information about distance of the insect to the front wall of the tank (this distance was crucial to translate pixel coordinates into centimeters). A white sheet of fabric spread behind the water tank appropriately located relative to the direction of sun light was used as a background. For some jumps, Sony RX10-III was used instead of the TS 1000.

In the water container, the slow-motion movies used for the detailed analyses have been shot using Trouble Shooter camera (TS 1000) set to film at 500 fps. The set-up is shown in Fig. S3. This setup requires two people for efficient work: one operates the high-speed camera, and the second person handles the water striders and triggers the jumps. Sometimes the water striders used their wings to escape from the water tank and these escapes were not analyzed.

**Table S6.** Observed number of water surface breaking by midlegs during jumping by the large-sized water striders: *G. gigas* and *P. tigrina*. Breaking was defined as breaking with at least one leg by assuming that in asymmetric jumps the other has lighter load.

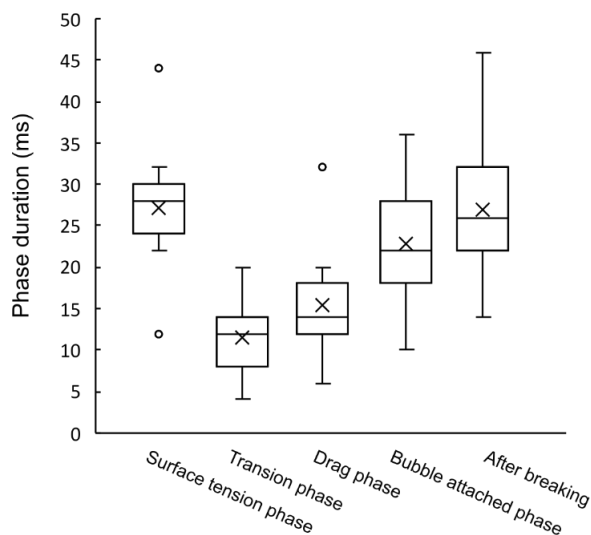
	<i>G. gigas</i>	<i>P. tigrina</i>	sum
Breaking occurred	57	21	78
No breaking	0	2	2
sum	57	23	80

## Supplementary Materials PART 4: Duration of jump phases in *Gigantometra gigas*

The surface tension phase lasts for ~12-44 ms ( $27 \pm 7$  ms for a single leg,  $n = 15$ , mean  $\pm$  SD, Table S7; ~26 ms in Fig. 3; ~22 ms in Fig. S5; ~12 ms in Fig. S6 where the legs are relatively non-synchronized and the second leg starts breaking the surface after ~22 ms). The transition phase lasts ~4-28 ms ( $12 \pm 5$  ms, for a single leg,  $n = 15$ , Table S7; ~16 ms in Fig. 3; ~18 ms in Fig. S5; ~28 ms in Fig. S6, where it is relatively long because the two legs are not well synchronized). The drag phase lasts ~14-22 ms ( $15 \pm 6$ , for a single leg,  $n = 15$ , Table S7; ~22 ms in Fig. 3; ~14 ms in Fig. S5; ~22 ms in Fig. S6). The duration from the breaking to the detachment of the air bubble lasts 10-32 ms ( $23 \pm 7$ , for a single leg,  $n = 15$ , Table S7; marked with blue-shaded vertical bands in Fig. 3; Fig. S5, S6).

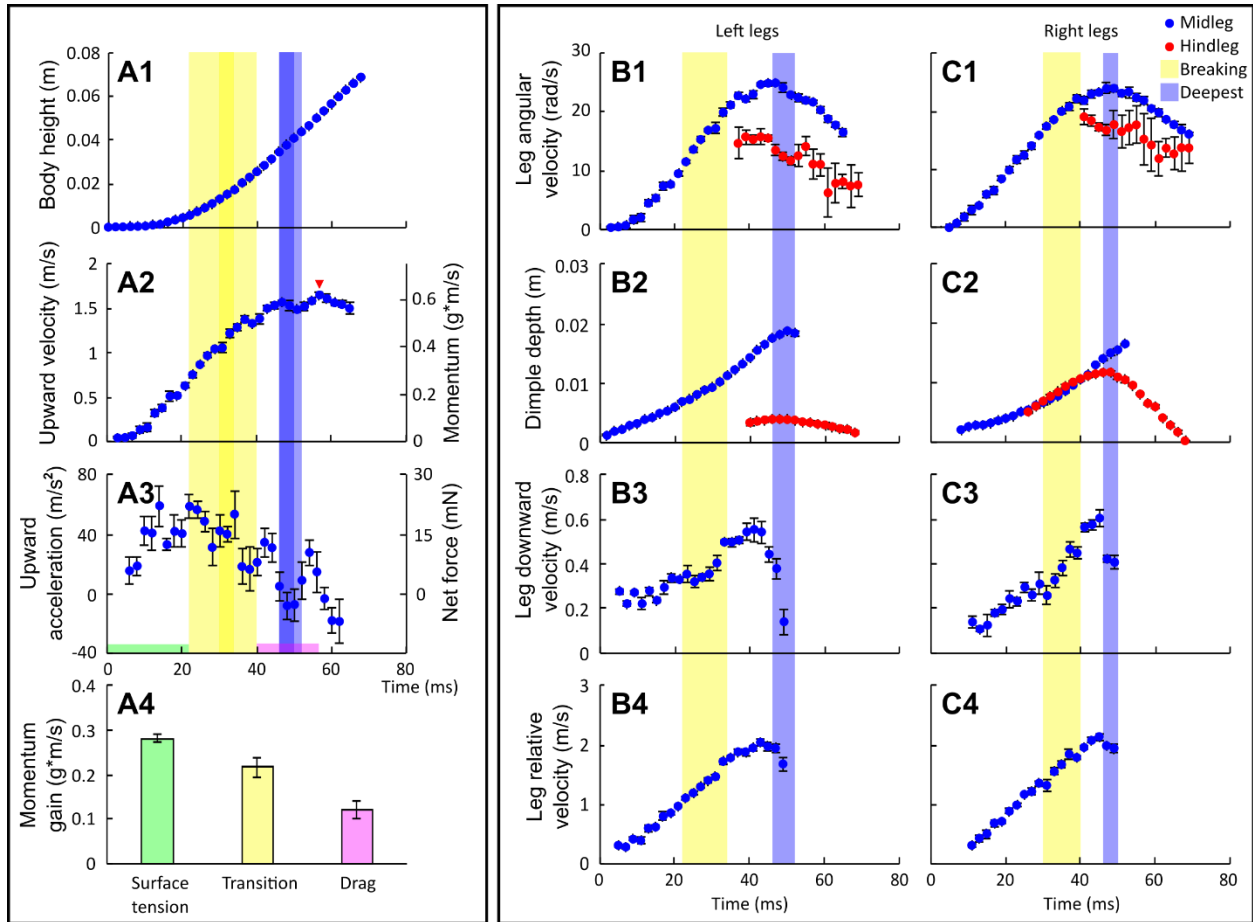
**Table S7.** Duration of jump phases of *G. gigas* recorded in the water container at the field site. “Surface tension phase” lasts from the start of the jump until surface breaking starts. “Transition phase” lasts from the moment when the first point of surface breaking is detected along one of the two midlegs until the moment when both midlegs fully break the surface. “Drag phase” lasts from the end of the “transition phase” until both midlegs have reached or passed through the deepest point (i.e., none of the two midlegs moved downward anymore). Bubble attached phase is from the start of surface breaking until the air bubble is completely detached from the leg and floats upwards in the form of bubbles. Bubble attached phase is usually included in the “After breaking phase”. “After breaking phase” is from the start of surface breaking until the midleg reaches the deepest point (hence it is a sum of “Transition phase + Drag phase”). See also Figure S4 based on these data.

Video (leg)	Surface tension phase (ms)	Transition phase (ms)	Drag phase (ms)	Bubble attached phase (ms)	After breaking (ms)
EVT05 (2) left	22	12	16	32	28
EVT05 (2) right	30	10	12	10	22
EVT16 left	28	14	14	24	28
EVT16 right	26	8	14	36	22
EVT41 left	22	18	16	22	34
EVT41 right	12	14	32	28	46
EVT12	26	20	20	28	40
EVT14	26	10	16	22	26
EVT28	30	8	6	16	14
EVT33	24	14	12	20	26
EVT35	32	6	12	18	18
EVT45	28	6	18	28	24
EVT47	28	16	12	16	28
EVT65	44	4	12	18	16
EVT75	28	14	18	24	32
<b>Mean (<math>\pm</math>s.d.)</b>	<b>27.1 (<math>\pm</math>6.7)</b>	<b>11.6 (<math>\pm</math>4.7)</b>	<b>15.3 (<math>\pm</math>5.7)</b>	<b>22.8 (<math>\pm</math>6.8)</b>	<b>26.9 (<math>\pm</math>8.6)</b>

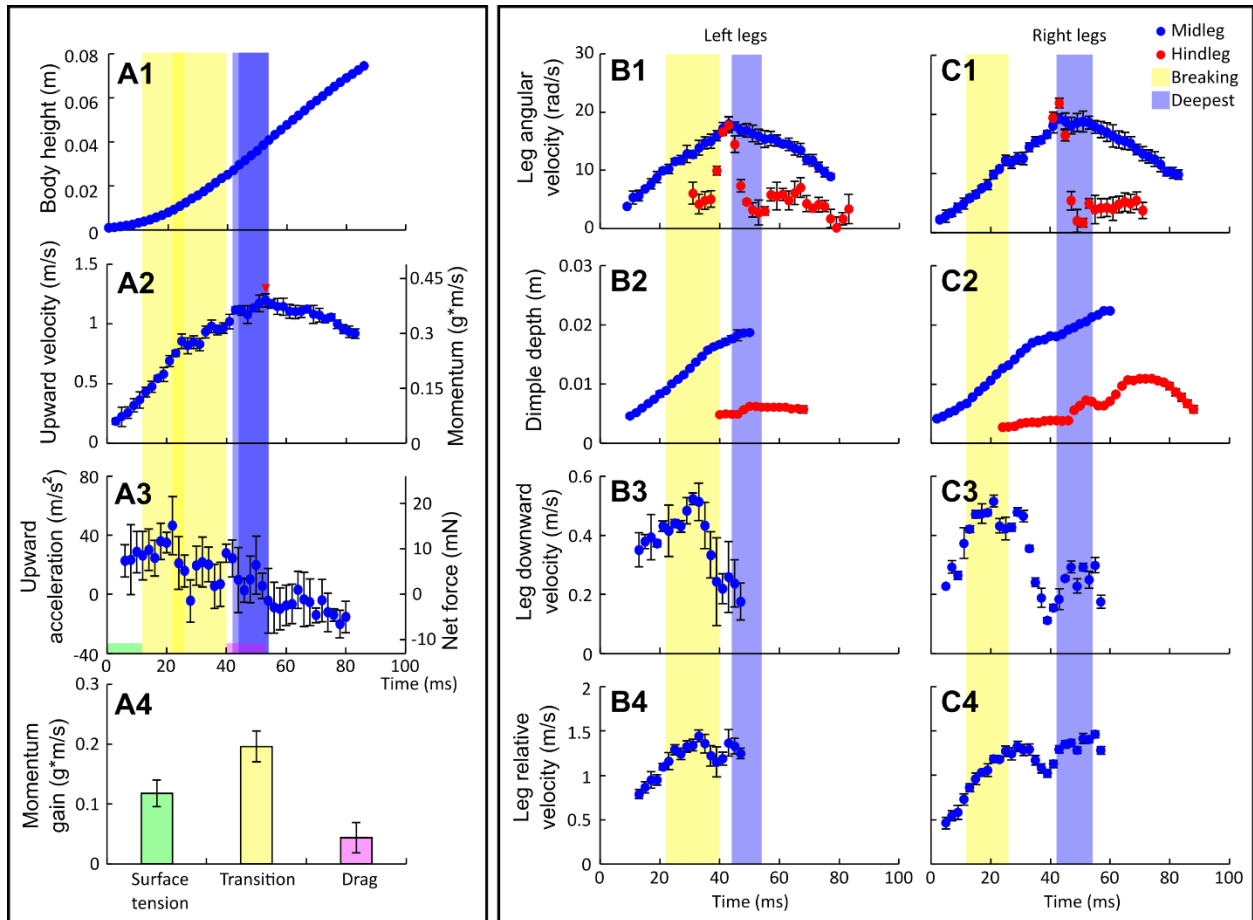


**Fig. S4. Box-whisker plots of phase durations (ms).** Duration of each phase of the jumps of *G. gigas* in the water container. Surface tension phase is from start of the jump until surface breaking starts. Transition phase is from the start of surface breaking until end of surface breaking. Drag phase is from end of surface breaking until leg reaches the deepest point (i.e., leg stops moving downward). Bubble attached phase is from the start of surface breaking until the air bubble is completely detached from the leg and floats upwards in the form of bubbles. Bubble attached phase is usually included in After breaking phase. After breaking phase is from the start of surface breaking until leg reaches the deepest point (hence it is a sum of “Transition phase + Drag phase”). The data are in Table S7.

Supplementary Materials PART 5: Additional Results from the detailed analyses of jumps



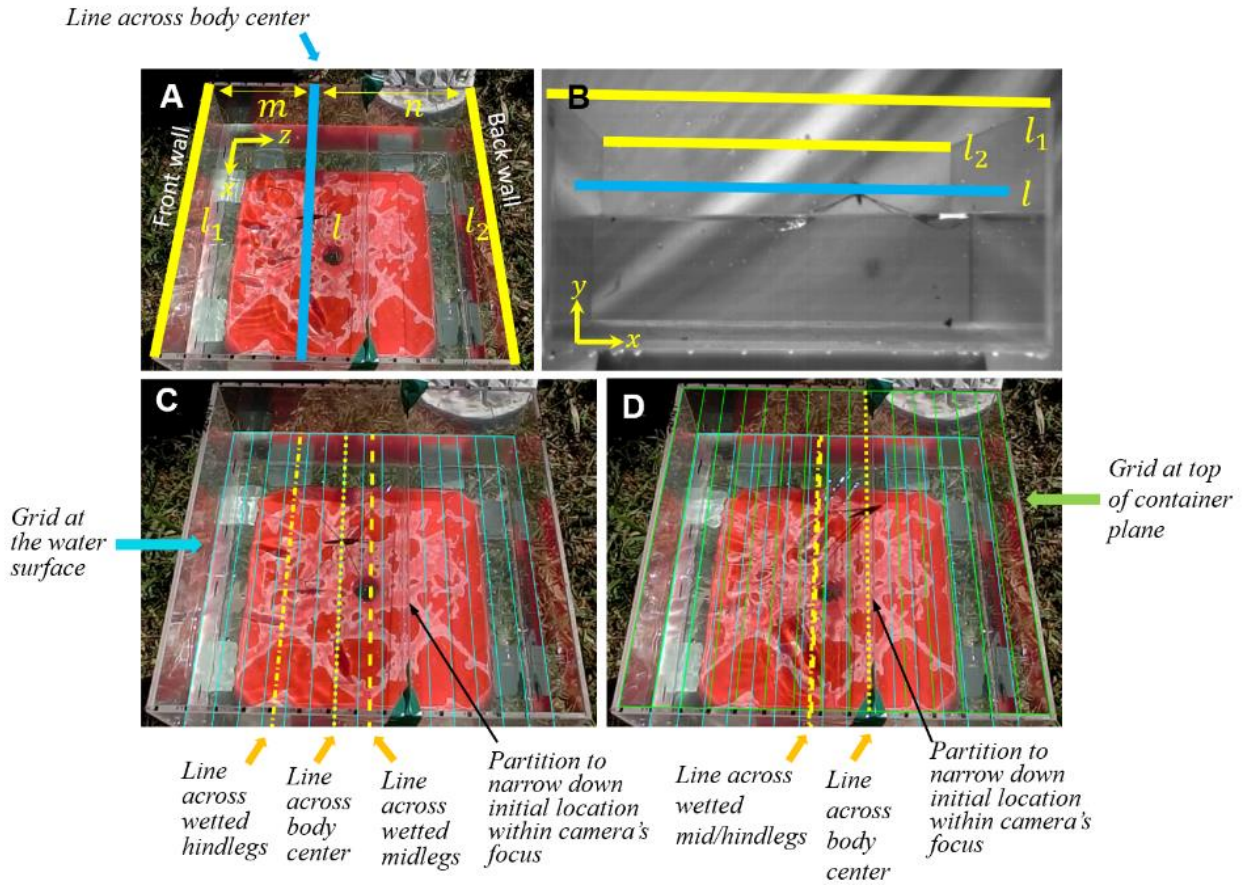
**Fig. S5. Kinematics and dynamics of the jumping on water by the giant water strider, *Gigantometra gigas*.** Results from analysis of a jump “EVT05 (2)”. (A) variables obtained from the body movement: changes of body height above the water surface (A1), body velocity (A2) and body acceleration (A3) during the jump. Right side axes in A2 and A3 indicated the changes of body momentum (A2) and net force (A3) during the jump calculated from the body movement and body mass. (A4) shows the comparison between the values of momentum gained during the three phases of jump: the surface tension phase (green), the transition phase (yellow) and the drag phase (purple). (B) and (C) contain variables concerning movements of the left (B) and right (C) midlegs (blue circles) and hindlegs (red circles in B1, B2, C1, C2): angular downward velocity (B1, C1), depth (B2, C2), downward velocity (B3, C3) and downward velocity relative to the body position (B4, C4). Yellow background indicates the transition phase when surface is breaking. Blue background indicates the bubble detaching phase duration of each leg. Red triangle in A2 indicates the moment of maximal body velocity.



**Fig. S6. Kinematics and dynamics of the jumping on water by the giant water strider, *Gigantometra gigas*.** Results from analysis of a jump “EVT41”. (A) variables obtained from the body movement: changes of body height above the water surface (A1), body velocity (A2) and body acceleration (A3) during the jump. Right side axes in A2 and A3 indicated the changes of body momentum (A2) and net force (A3) during the jump calculated from the body movement and body mass. (A4) shows the comparison between the values of momentum gained during the three phases of jump: the surface tension phase (green), the transition phase (yellow) and the drag phase (purple). (B) and (C) contain variables concerning movements of the left (B) and right (C) midlegs (blue circles) and hindlegs (red circles in B1, B2, C1, C2): angular downward velocity (B1, C1), depth (B2, C2), downward velocity (B3, C3) and downward velocity relative to the body position (B4, C4). Yellow background indicates the transition phase when surface is breaking. Blue background indicates the bubble detaching phase duration of each leg. Red triangle in A2 indicates the moment of maximal body velocity.

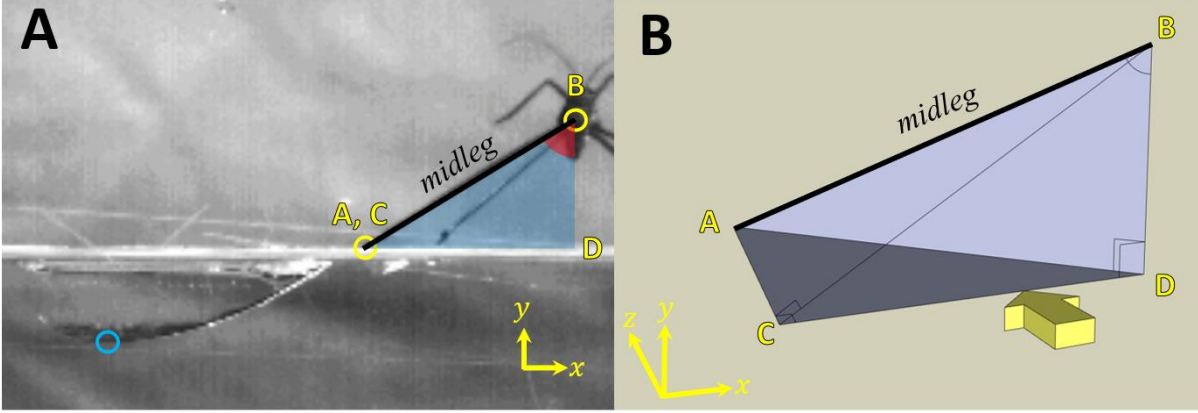
Fig. 3 of the main text, and Fig. S5, S6 present the details extracted from the three best movies. In total we observed 65 jumps (51 in males and 14 in females) by 17 individuals (12 males and 5 females). We also recorded 43 jumps by 5 individuals of *Ptilonera tigrina*. In all observed jumps the water striders broke the water surface and the jump was produced by a mixture of two types of forces: surface tension followed by drag. In all 65 jumps the legs moving in the water were surrounded by the layer of air captured within the long hairs of tibia and tarsi. Also, in all jumps the midlegs moving upward eventually left some of the air in the form of bubbles. In all jumps, we observed the three main phases: surface tension, transition, and drag phase. See table S7 and Fig. S4 for timing of each phase based on timing recorded in 15 leg movement events from 12 videos.

Supplementary Materials PART 6: Assumptions and methods of digitizing



**Fig. S7. The method of re-calculation from pixel-based to absolute (cm/mm) coordinates.** The jumping of the water strider was recorded with a high-speed camera through the front wall (left side wall in a) of the 30 cm by 30 cm transparent water tank, i.e., the high-speed camera was facing the front wall marked with  $l_1$ , and its view is shown in B. The views in A, C, D are from a standard camcorder that recorded the jump from above. The thin blue lines at the level of water surface are 2cm apart. The real size of a pixel at any specific distance to the front wall (example of such a point is the water strider's body center through which a thick blue line crosses in a and b) was deduced from the following formula:  $30\text{cm}/l = 30\text{cm}/(\frac{nl_1+ml_2}{m+n})$ , where  $m$  and  $n$  are horizontal relative distances along the z-axis from the line across the digitized point (e.g., thick blue line across body center in (A) to the front and back wall respectively, and  $l_1$  and  $l_2$  are lengths in pixels of the front and back wall in the view of the slow motion camera. This principle was directly applied to convert pixels to centimeters for the body center digitized (from the high-speed camera view) at the start of a jump (C) and at the takeoff (D). The body center z-axis at the takeoff was measured by using a grid in the plane corresponding to the upper part of the container (green lines), because the y axis coordinates of the body center at the takeoff were approaching this upper plane and were distant from the plane of the water surface (D). Hence for these two points of time, the  $m$  and  $n$  values were directly measured from an image from the standard camera view from above at two different planes: the water level plane for the start of jump (blue grid at the water surface) and the top-of-container plane for the takeoff moment (when legs still left on water surface; blue grid in C, D). The conversion from pixels to centimeters for frames located between these two points of time used  $m$  and  $n$  values calculated assuming a linear change of  $m$  (and  $n$ ) during the jump duration between the initial (C; start of jump) and final (D; moment of takeoff) values of  $m$  and  $n$ . The same procedure was applied to the legs. For the two points digitized on legs (point of contact with water and the deepest point of tibia/tarsus for midlegs, as well as femur/tibia joint and the deepest point for hindlegs), we used an approximate distance to the front wall,  $m$  (and the corresponding distance to the back wall,  $n$ ). It was approximately assumed to be the distance between the line going through the midrange of the wetted midleg/hindleg (marked as broken yellow lines in C, D).





**Fig. S8. Calculations of midleg-to-vertical angles for each frame.** Points on the water surface (A, C), the deepest point (blue circle) of the middle leg, and the body center (B) were tracked in every frame using MaxTRAQ program. The vertical angle of a midleg (ABD) was defined as angle between section AB (along the leg) and vertical line (section BD). However, the camera (3D arrow along the lens's axis indicates where the camera was pointing) provided direct measure of distances and angles within the plane marked by the triangle CBD (i.e., plane perpendicular to the lens axis). Using this information together with the inferred distance AB (from insect empirical measurements of leg length and proportion of leg above water measured from the video) we estimated (by trigonometry) the angle ABD in each frame in movies with insects facing the camera while jumping. The formulas are explained below:

The angle between the midleg (section AB) and the vertical line (red shaded angle in Fig. S8A; angle ABD in b) was calculated in each frame using the trigonometric functions and coordinates of the body center and the water surface contact point of the middle leg. The middle leg angle is expressed as below.

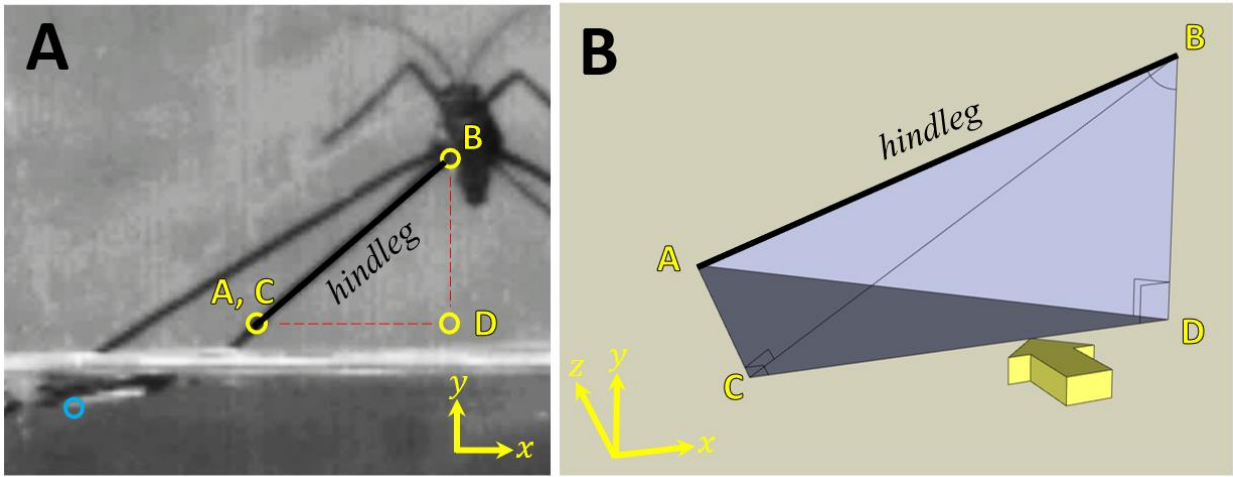
$$\begin{aligned} \angle \text{Middle leg} = \angle \text{ABD} &= \tan^{-1} \frac{\overline{AD}}{\overline{BD}} = \tan^{-1} \frac{(\overline{AC}^2 + \overline{CD}^2)^{1/2}}{\overline{BD}} \\ &= \tan^{-1} \frac{\sqrt{(\text{Body}_z - \text{Surface}_z)^2 + (\text{Body}_x - \text{Surface}_x)^2}}{\text{Body}_y - \text{Surface}_y} \\ &= \tan^{-1} \frac{\sqrt{(B_z - A_z)^2 + (B_x - A_x)^2}}{B_y - A_y} \end{aligned}$$

The angle between the hind leg's femur and the vertical line was calculated in each frame by the three-dimensional approximation using the second law of the cosines and using the known length of femur (Fig S9). The angle was calculated as below.

$$\begin{aligned} \angle \text{Hind leg} = \angle \text{ABD} &= \cos^{-1} \left( \frac{\overline{AB}^2 + \overline{BD}^2 - \overline{AD}^2}{2 \cdot \overline{AB} \cdot \overline{BD}} \right) \\ &= \cos^{-1} \left( \frac{\overline{AB}^2 + \overline{BD}^2 - (\overline{AC}^2 + \overline{CD}^2)}{2 \cdot \overline{AB} \cdot \overline{BD}} \right) \\ &= \cos^{-1} \left( \frac{\overline{AB}^2 + \overline{BD}^2 - [(\overline{AB}^2 - \overline{BC}^2) + \overline{CD}^2]}{2 \cdot \overline{AB} \cdot \overline{BD}} \right) \\ &= \cos^{-1} \left( \frac{\overline{BD}^2 + \overline{BC}^2 - \overline{CD}^2}{2 \cdot \overline{AB} \cdot \overline{BD}} \right) \end{aligned}$$

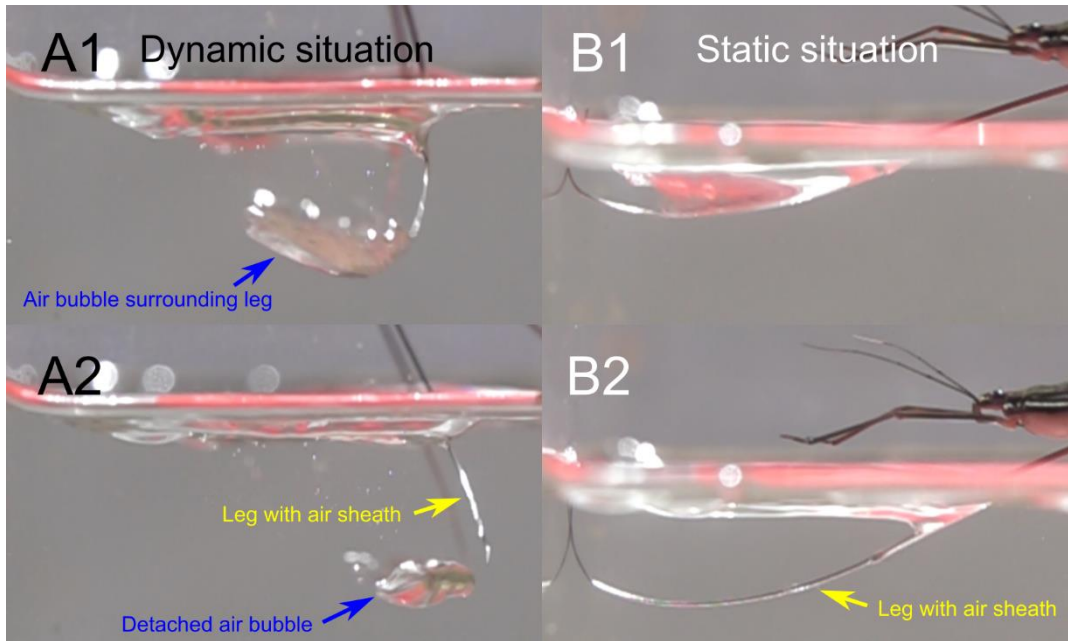
$$\begin{aligned}
&= \cos^{-1}\left(\frac{(B_y - D_y)^2 + [(B_y - C_y)^2 + (B_x - C_x)^2] - (D_x - C_x)^2}{2 \cdot \overline{AB} \cdot (B_y - D_y)}\right) \\
&= \cos^{-1}\left(\frac{(B_y - C_y)^2 + [(B_y - C_y)^2 + (B_x - C_x)^2] - (B_x - C_x)^2}{2 \cdot \overline{AB} \cdot (B_y - C_y)}\right) \\
&= \cos^{-1}\left(\frac{B_y - C_y}{\overline{AB}}\right)
\end{aligned}$$

The angle was calculated since the length of the femur ( $\overline{AB}$ ) was already known from empirical measurements.



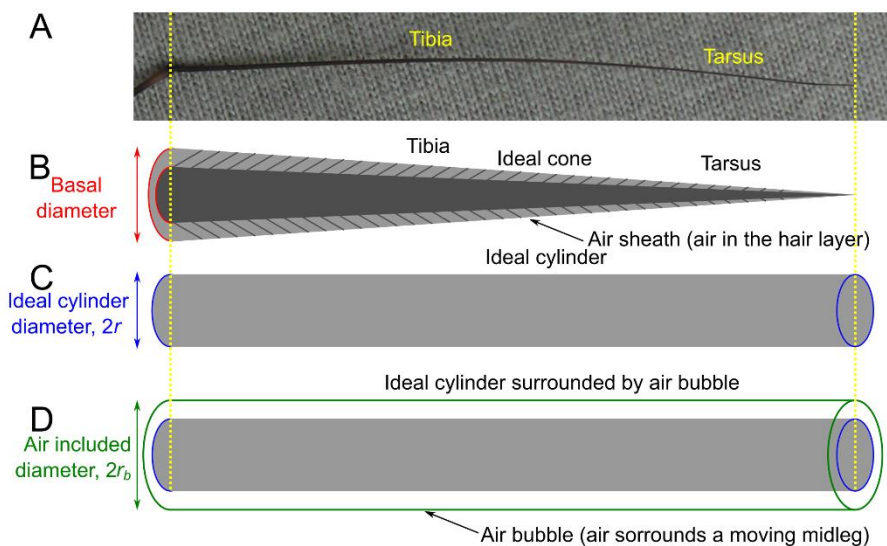
**Fig. S9. Calculations of hindleg-to-vertical angles for each frame.** Hind femur angle was calculated for each frame from the empirically measured femur length and information extracted from the video. As we knew the real femur length of the hind leg ( $\overline{AB}$ ), the angle  $\angle ABD = \cos^{-1}\left(\frac{B_y - C_y}{\overline{AB}}\right)$ . Femur tip (yellow) and the deepest point (blue) of the hind leg were also digitized.

**Supplementary Materials PART 7: Extraction of information from empirical measurements for the model's assumptions about the functional/effective radius of the wetted leg.**



**Fig. S10. Air sheath and air bubble exist in both dynamic and static situations.** In the dynamic situation (A), the wetted leg captures both air sheath and air bubble. The high-speed video frames show that the leg slips out from the air bubble but still keeps the air sheath (A2). In the static situation, when the insect accidentally breaks the water surface, the leg only captures and keeps the air sheath (B2).

The model dramatically simplifies some of the aspects of reality. One of the simplifications is an assumption about midleg shape that is used to estimate the drag force in the drag phase of a jump. The model assumes that the two midlegs are cylinders (or rods)



**Fig. S11.** Tibia and tarsus of the real water strider leg (A) considered for calculations. At the first approximation, tibia and tarsus were assumed to form an ideal cone (B) of the length corresponding to the total length of tibia and tarsus, and the diameter (including hairs) ranging from the thickness of the proximal tibia at the femur/tibia joint to zero (at the tip). At the next step of approximation, we assumed the leg is a cylinder/rod with the diameter that results in the cylinder's volume in (C) equal to the volume of the cone in (B). Air-bubble-including radius was calculated by assuming that the volume of the air bubble covers the ideal cylinder evenly (D): i.e., knowing the physical length and basal diameter of a wetted leg (A, B), we estimated the thickness of the leg assuming that air surrounds the leg in a uniform symmetrical manner (D).

of a diameter based on the empirical measurements of legs of water striders and on the empirical estimates of the air volume captured around the leg during a jump. The functional (effectively working for drag force) leg diameter during the initial moments of the drag phase, when air bubble surrounds the leg, is calculated assuming that the air bubble surrounds the cylinder as a uniform layer (Fig. S11D) of a thickness calculated from the empirically derived measurements of the volume of air caught around the leg (Table S8). We measured the basal diameter of the legs, including their hair layer, as shown in Fig. S11B, based on empirical data. This is because the air sheath captured by the hairs always remains attached to the legs in both dynamic and static situations, as depicted in Fig. S10. As a result, we were able to estimate the volume of the air bubble (excluding the air sheath) by measuring the detached air bubbles (Fig. S10A).

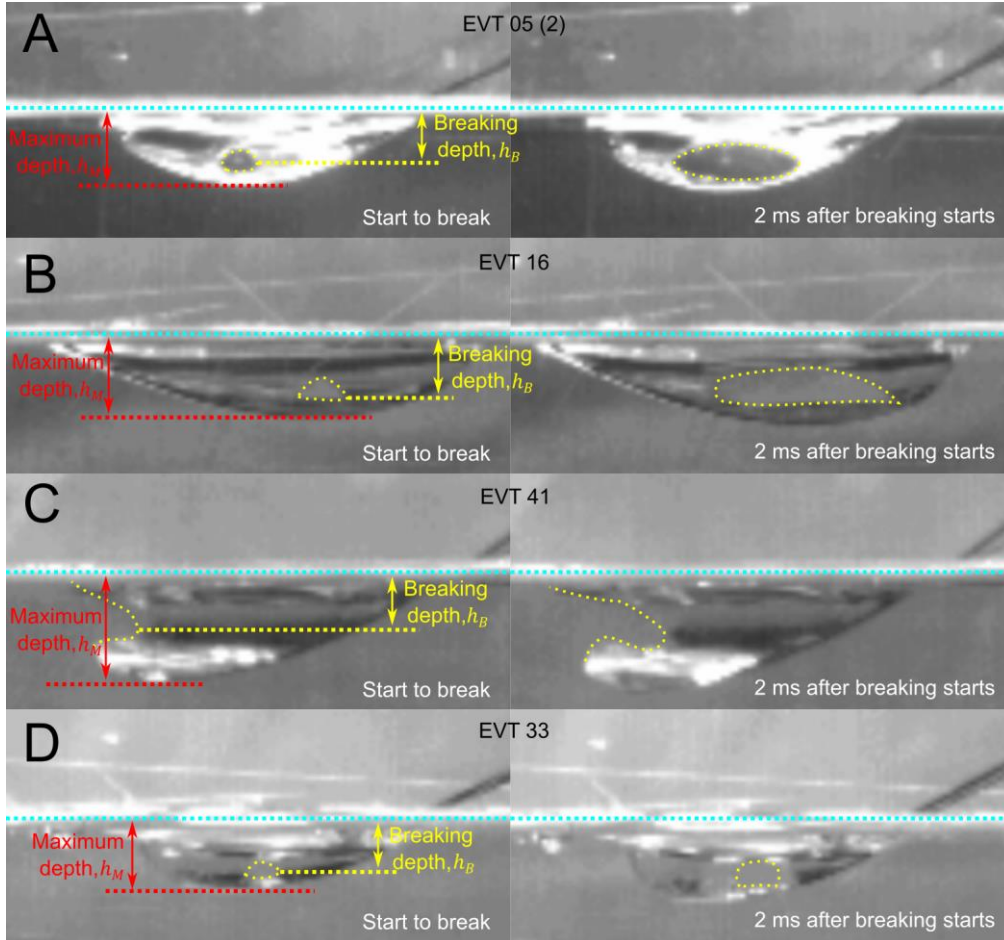
**Table S8. Calculated ideal radius of a cylinder imitating the midleg (Fig. 11C), and the ideal radius of a cylinder imitating the midleg surrounded by air bubble (Fig. 11D), as well as the ratio between these two radii (radius with bubble to radius without bubble).** The observed minimum value is colored blue, and the maximum value is colored red in the table. Data derived from slow motion movies of *G. gigas*.

Videos	Ideal radius (mm)	Observed bubble volume for a leg (mm <sup>3</sup> )	Ideal bubble included radius (mm)	Radius ratio
EVT16	0.131	43.4	0.520	3.96
EVT05 (2)	0.113	9.9	0.285	2.54
EVT41	0.137	36.3	0.482	3.52
EVT75	0.149	31.3	0.461	3.10
EVT45	0.137	26.9	0.421	3.07
EVT47	0.137	78.2	0.692	5.05
EVT63	0.117	7.8	0.261	2.24
EVT65	0.117	16.4	0.358	3.06
EVT67	0.117	23.1	0.419	3.58
EVT00	0.113	23.1	0.416	3.70
EVT03 (2)	0.113	18.2	0.373	3.31
EVT12	0.131	56.6	0.589	4.49
EVT14	0.131	61.1	0.611	4.65
EVT28	0.117	11.3	0.323	2.76
Mean (S.D.)	0.126 (0.012)	31.7 (21.2)	0.444 (0.126)	3.50 (0.81)

The model simulated several situations of different radius of leg cylinder (or rod) to imitate the leg with the air bubble around it assuming the “radius ratio” (Table S8) of 2.24, 3.50, and 5.05 to simulate the situation of the minimum, average, and maximal air volume of the air bubble trapped around the moving leg. We also imitated that ratio of 1 to simulate the leg without any additional air bubble trapped around the moving leg with air sheath in the hair layer.

**Supplementary Materials PART 8: Observations of midleg dimple breaking and the role of the breaking process in the simulation model.**

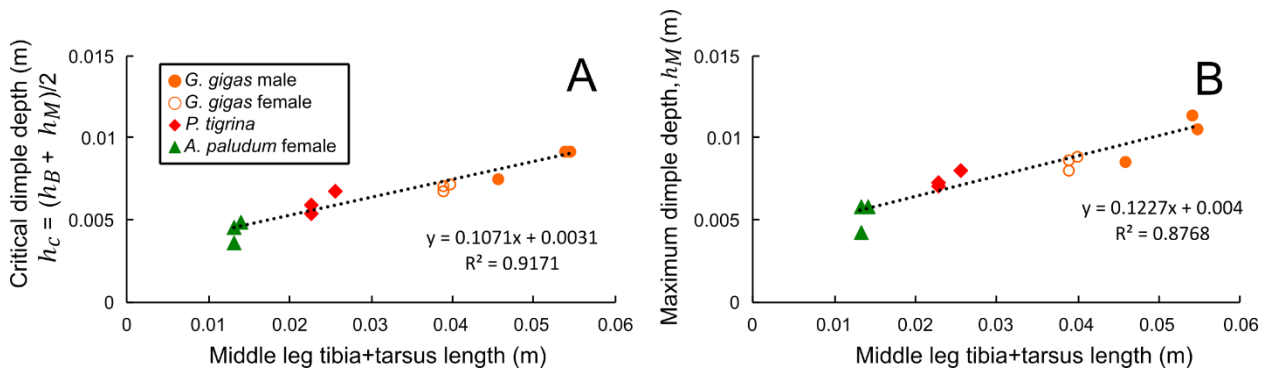
The model is a simplified representation that does not directly simulate a leg breaking the surface at a different point along the



**Fig. S12. Examples of dimple breaking by the midleg of the giant water strider during jumps.** The dimple starts to break when the leg reaches the maximum depth of the dimple ( $h_M$ , red arrows). However, the breaking of the dimple does not occur at the deepest point (i.e., not at the maximum depth,  $h_M$ ), but rather at a certain depth (yellow arrows) that is shallower than the maximum depth: the depth of breaking initiation,  $h_B$ . The breaking initiation point varies and the breaking can start either at the middle of the dimple (A, B, D) or at the end of the dimple in the longitudinal direction (C). The breaking of the dimple expands along the leg in both longitudinal directions (A, B, D) or in a single direction (C), which can potentially affect the duration of the breaking process. The right panels of the figure depict this phenomenon 2 ms after the start of breaking.

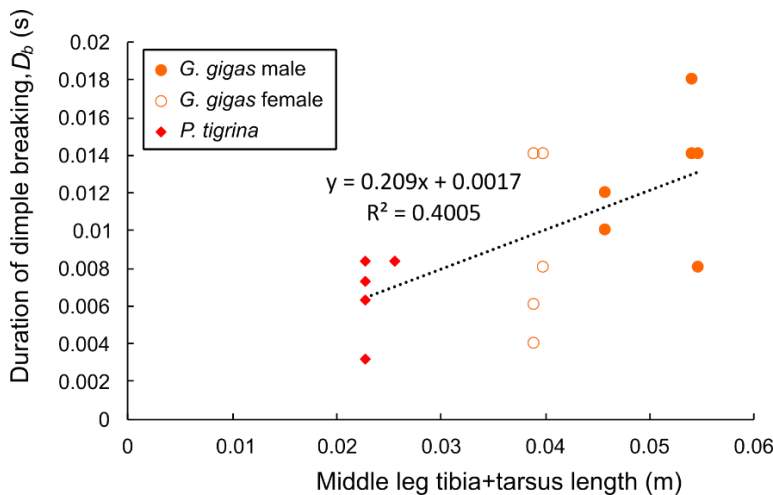
wetted leg than the point of maximum dimple depth (Fig. S12). In the previous model by Yang et al. (1), a leg was modeled as a horizontal cylinder (or rod) based on a theoretical model of a cylinder by Vella (3), and it was assumed that water surface breaks at a critical dimple depth in a single moment. However, our model attempts to imitate an additional transition phase during which a combination of surface tension and drag contribute to the jump. We assume that the transition phase begins at the critical time,  $t_c$ , when the theoretically modeled dimple depth of the two horizontal cylinders (representing the two symmetrically moving midlegs in the model) reaches the critical depth,  $h_c$ . This critical depth is calculated in the model from the regression formula of  $h_c$ , (defined as the average between the breaking point depth,  $h_B$ , and the maximum dimple depth at the breaking moment,  $h_M$ ) which was measured in videos of water striders of different sizes (Fig. S12), on the wetted midleg length (Fig. S13A). In addition, the model uses an empirical relationship shown in Fig. S13B to calculate an index of maximum dimple depth,  $i = h_M/l_c$ , for water striders of different sizes. This index modifies Yang's (1) formula, where the original  $2l_c$  part (denominator) of the surface tension formula is replaced by " $il_c$ " (Formula 6). This modification allows the deeper dimple depth for theoretical simulation of surface tension than the original Vella's model of a rigid cylinder (3) used by Yang et al. (1).

Once the transition phase starts at  $t_c$ , it lasts for a duration of  $D_b$ , which is calculated in the model from the empirically derived regression in Fig. S14. During this time, the surface tension from the two midlegs is calculated based on the assumed dimple depth of  $h_c$  and the wetted length of the horizontal rod/cylinder (representing the midleg) that gradually decreases from 100% to 0% of the midleg tibia+tarsus length over the period  $D_b$ . Simultaneously, the drag force gradually increases over the same period, as the length of the horizontal cylinder (rod) moving downward in the water increases from 0% to 100% of the midleg tibia+tarsus length. The horizontal rod's downward velocity, which also contributes to the drag, is calculated in the model, considering the angular velocity of midleg rotation,  $\omega$ , the height of the insect body above the surface, and the body's upward velocity, in accordance with Yang et al. (1).



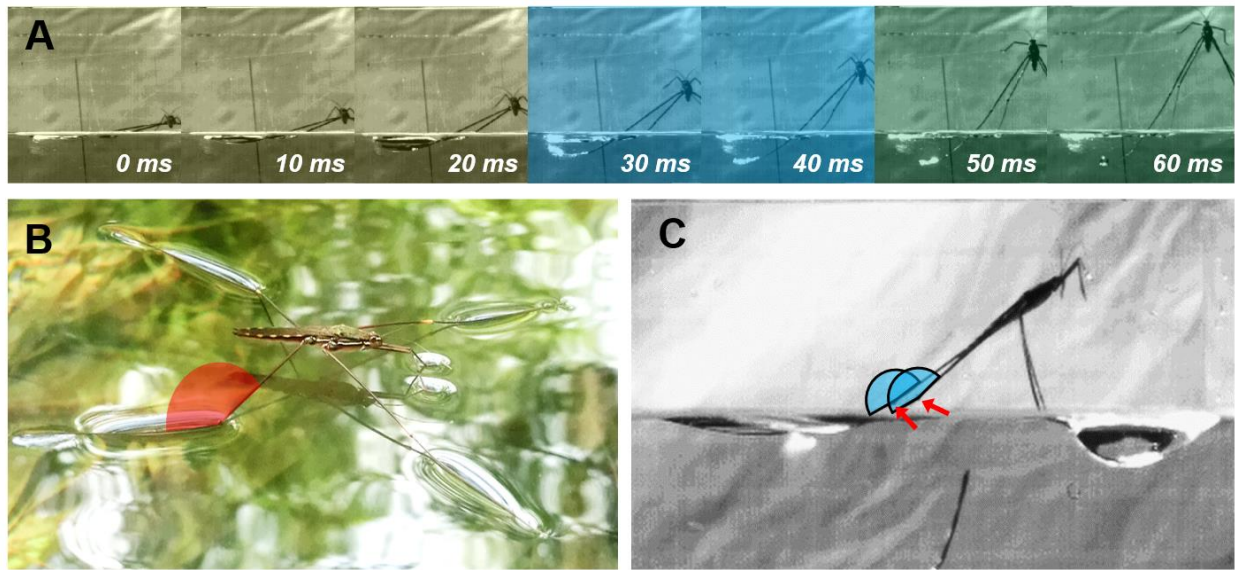
**Fig. S13. Relationship between midleg tibia+tarsus length (constant wetted midleg length) and dimple depth measures derived from the videos of jumping water striders of different sizes.**

The breaking point depth,  $h_B$ , and the maximum dimple depth at breaking moment,  $h_M$ , defined in Fig. S12, were found to be linearly related to the wetted length of the middle leg among the studied species who use surface breaking jumps. The average of  $h_B$  and  $h_M$  was used to determine  $h_c$  for water striders with various sizes using linear regression of depth on middle leg constant wetted length (A). The  $h_M$  was used to determine index of dimple depth,  $i$ , in the model for water striders with various sizes using linear regression of depth on middle leg constant wetted length (B).



**Fig. S14. Relationship between midleg tibia + tarsus length (constant wetted midleg length) and the duration of dimple breaking phase of a midleg,  $D_b$ , which is also the duration of the transition phase if both midlegs act in an entirely symmetrical manner (assumed in the model).** Several factors can affect the duration of dimple breaking, including the wetted length, leg downward velocity, and breaking point (whether at the center or end of the dimple in the leg's longitudinal direction). For simplicity, the regression of the empirically observed duration of breaking,  $D_b$ , on the midleg tibia + tarsus length (constant wetted midleg length) was used in the model to predict the duration of dimple breaking,  $D_b$ , for water striders of different sizes (midleg tibia + tarsus length). However, we were unable to include data from *A. paludum* in the regression because their complete breaking of the dimple was not observed under natural conditions.

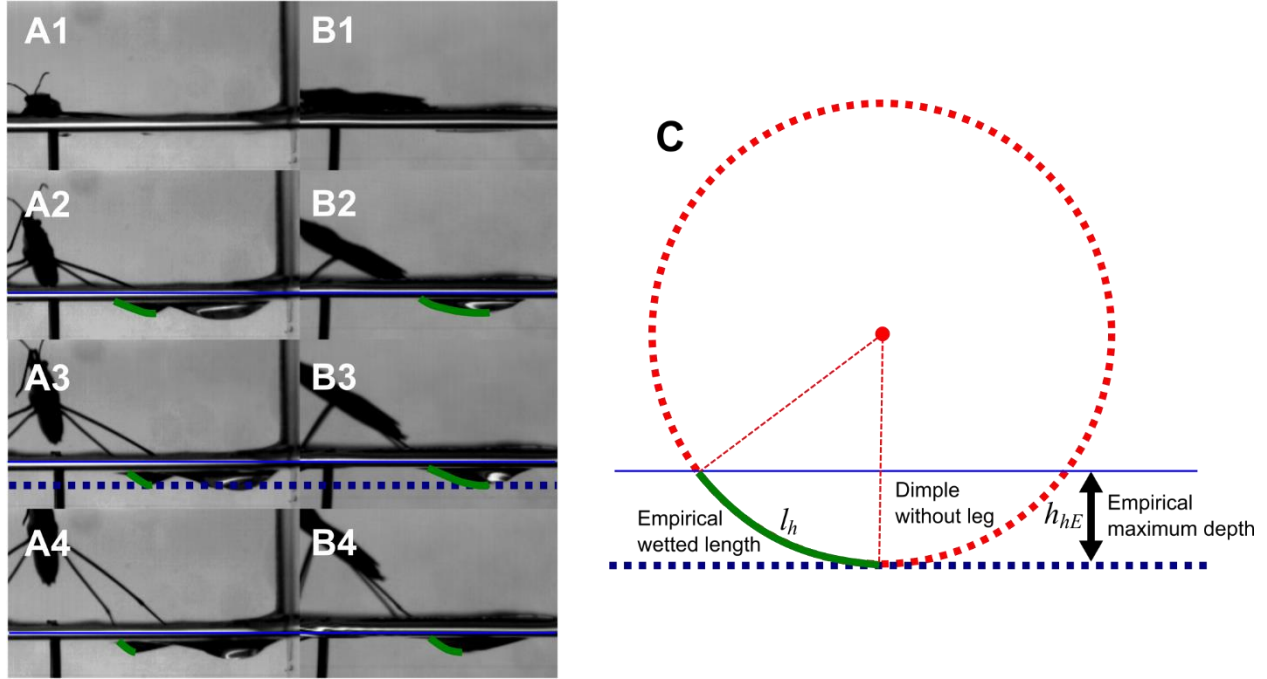
**Supplementary Materials PART 9:** Observations of hindlegs in the jumps of *Gigantometra gigas*.



**Fig. S15. Hindlegs in the jump of the giant water strider.** Changes of body pitch during the jump analyzed in Fig. 3 are the most pronounced in the final phase (40-60 ms in a), when a sudden short-lasting increase in the downward angular velocity of hindlegs occurs (in Fig. 3, S5, S6). Hindleg's dimples depth remain relatively stable at the initial phases (0-20 ms of surface tension phase in a) and subsequently during the transition and drag phases (30-40 ms in A), and they are generally similar to the dimples in resting position (b). During the jump, the angle between femur and tibia at the femur/tibia joint appears to remain roughly similar for extensive portion of the jump. The resulting dimples during jump may deepen slightly in the final stages of jump when the body pitch changes, and when the femur/tibia angle (marked red) becomes wider and approaches  $180^\circ$  in the final stages of the hindlegs' leaving the water surface. However, this typically this does not lead to breaking the water surface (A, C) because the hindlegs bend quite extensively (C) and because the water strider's legs at this stage are already moving upwards and do not push the surface (green shaded frames in a). Red arrows in (C) mark the femur-tibia joints for each hindlegs.

### Supplementary Materials PART 10: Hindleg's constant depth, $h_{hm}$ .

To calculate for each movie and species the theoretically assumed constant depth of a hindleg ( $h_{hm}$ ; see page 36 in Supplementary Materials PART 19), we used empirical maximum depth from high-speed videos. The constant depth used in the model ( $h_{hm}$ ) was calculated from the empirical maximum depth,  $h_{hE}$ , and wetted leg length,  $l_h$ , assuming the wetted length as a half of an arc. The average depth of the arc was used as the constant depth.



**Fig. S16. The constant depth of hind leg.** The constant depth,  $h_{hm}$ , was calculated as an average depth of a half of an arc that has same maximum depth,  $h_{hE}$  and wetted length,  $l_h$ , of empirical measurements of species.

### Supplementary Materials PART 11: Maximum jumping height calculation.

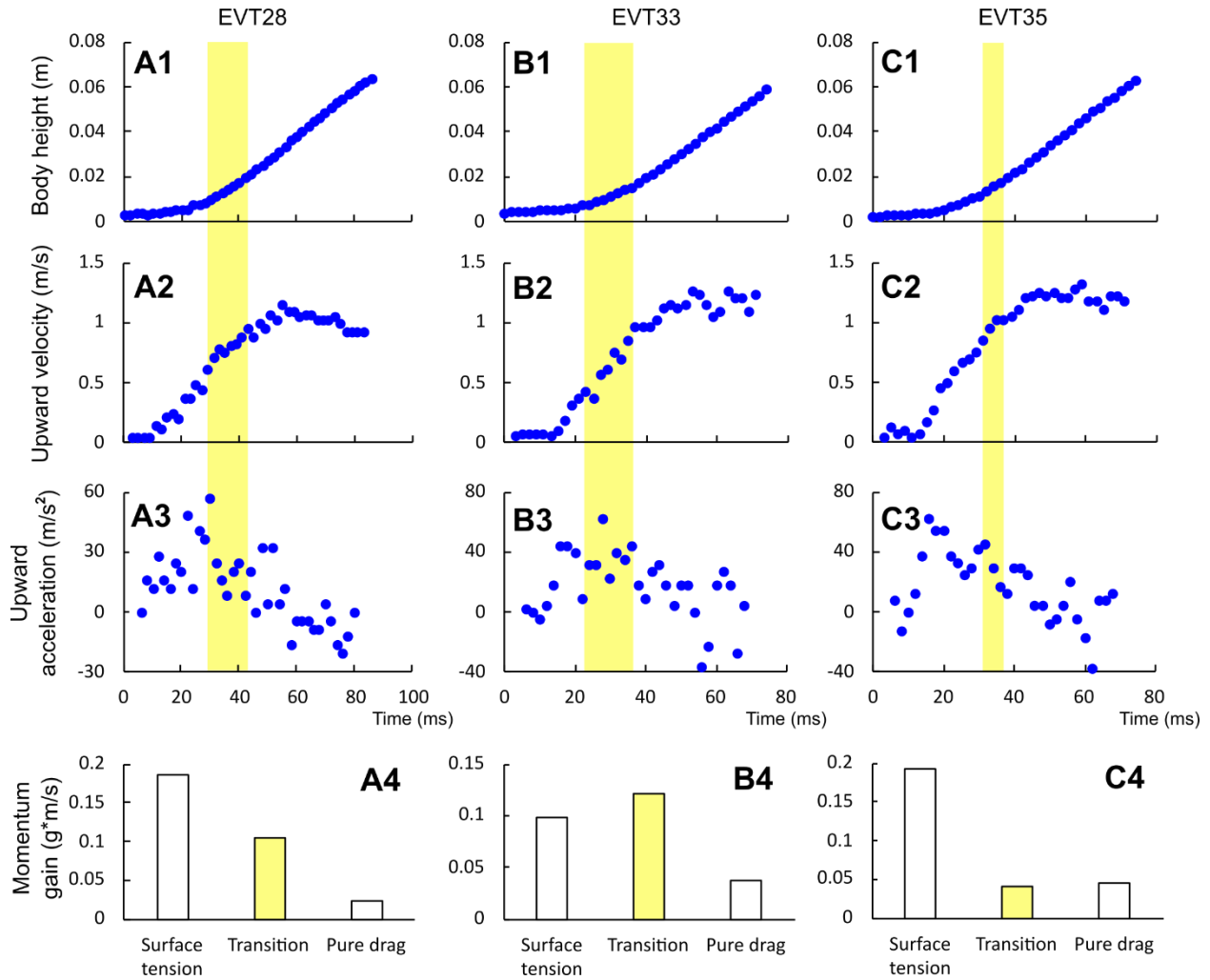
If an object takes off vertically at the moment of takeoff,  $t_f$ , with the takeoff velocity,  $v_f$ , from initial height,  $H_0$ , the object will be at the maximum height,  $H_m$ , when the total kinetic energy transferred to potential energy. Hence, the maximum jumping height,  $H_m$ , can be calculated as follows:

$$E_{potential} = mgh = mg(H_m - H_0) = E_{kinetic} = \frac{1}{2}mv_f^2$$

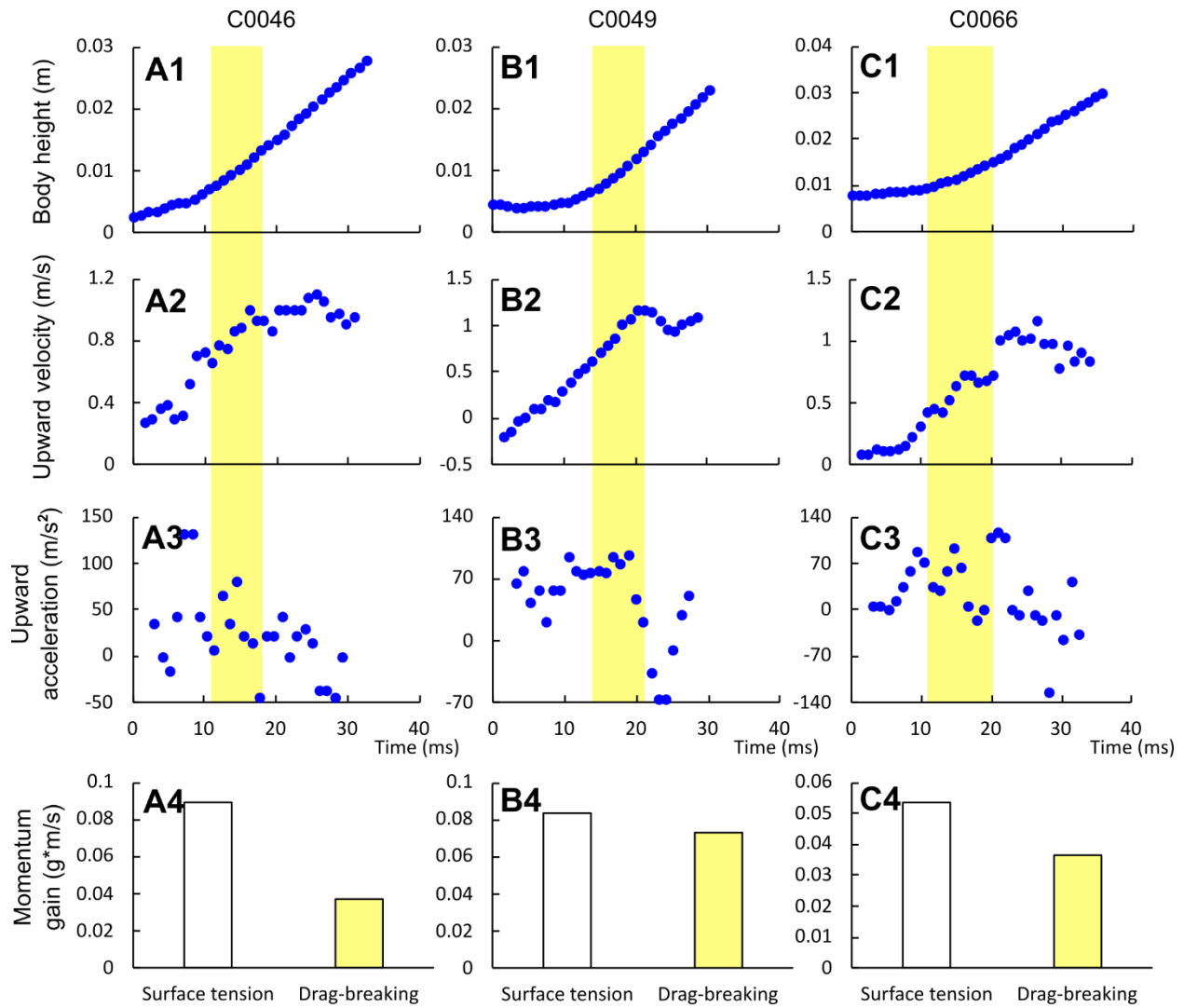
$$H_m = H_0 + \frac{v_f^2}{2g}$$



**Supplementary Materials PART 12: Additional empirical results for *G. gigas* females and *P. tigrina***



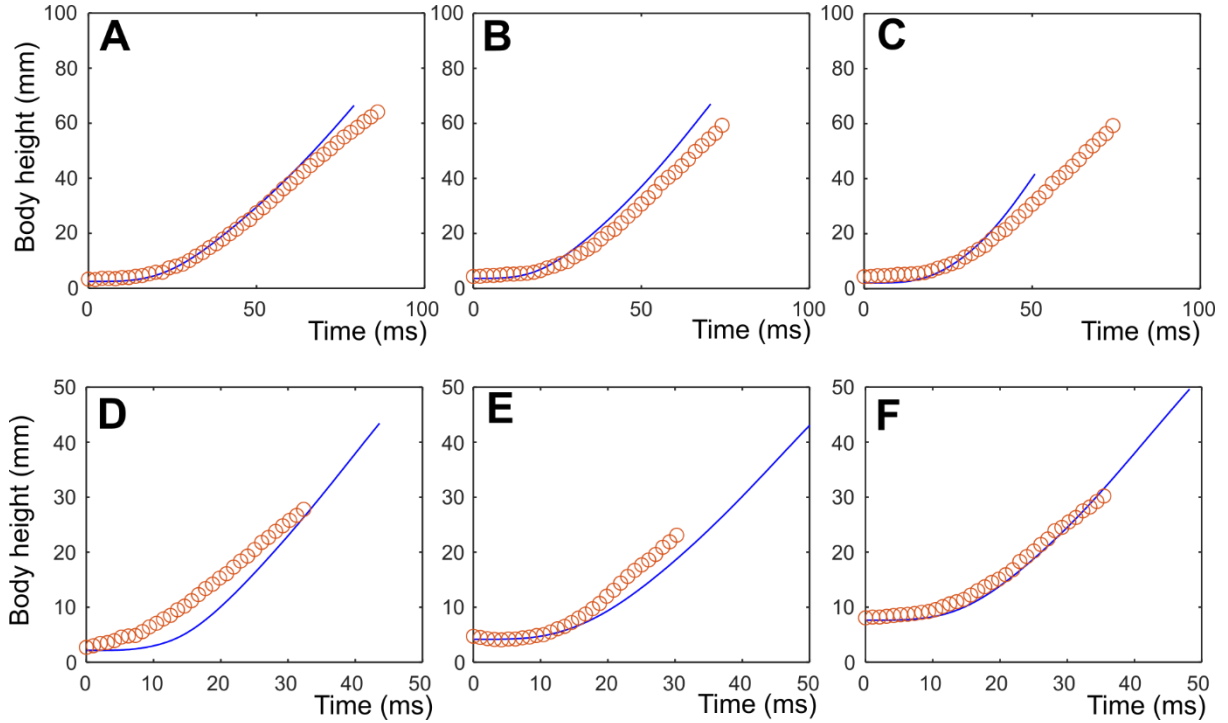
**Fig. S17. Kinematics of the jumping on water by the giant water strider (*Gigantometra gigas*) females.** Extra results from analyses of jumps “EVT28”, “EVT33”, “EVT35”. A1, B1, C1 show body height; A2, B2, C2 show body velocity; A3, B3, C3 show body acceleration during the jump. A4, B4, C4 show the comparison between the values of momentum gained during the three phases of jump: the surface tension phase, the transition phase (yellow), and the drag phase. The vertical yellow band across the panels indicates the transition phase when surface is in the process of breaking.



**Fig. S18. Kinematics of the jumping on water by *Ptilomera tigrina*.** Results of analysis of jumps in movies "C0046", "C0049", "C0066". A1, B1, C1 show body height; A2, B2, C2 show body velocity; A3, B3, C3 show body acceleration during the jump. A4, B4, C4 show the comparison between the values of momentum gained during the two phases of jump: the surface tension phase, and the drag-breaking phase (corresponding to the transitional phase in *G. gigas*). Pure drag phase is not observed because *P. tigrina* legs go up before full breaking of the middle leg dimple. Yellow vertical bands across the panels indicates the "drag-breaking" phase (i.e., the transition phase) when surface is in the process of breaking under the midlegs (see also Supplementary Movie 3).

### Supplementary Materials PART 13: Model validation - comparison with empirical observations

The supplementary results of model validation are similar to those shown in Fig. 3 in the main text. The results illustrate a reasonable match between empirical (Data from Supplementary Materials PART 12) and theoretical trajectories of body center for specific jumps of three females of *G. gigas* (Fig. S19A-C) and three individuals of *P. tigrina* (Fig. S19D-F).

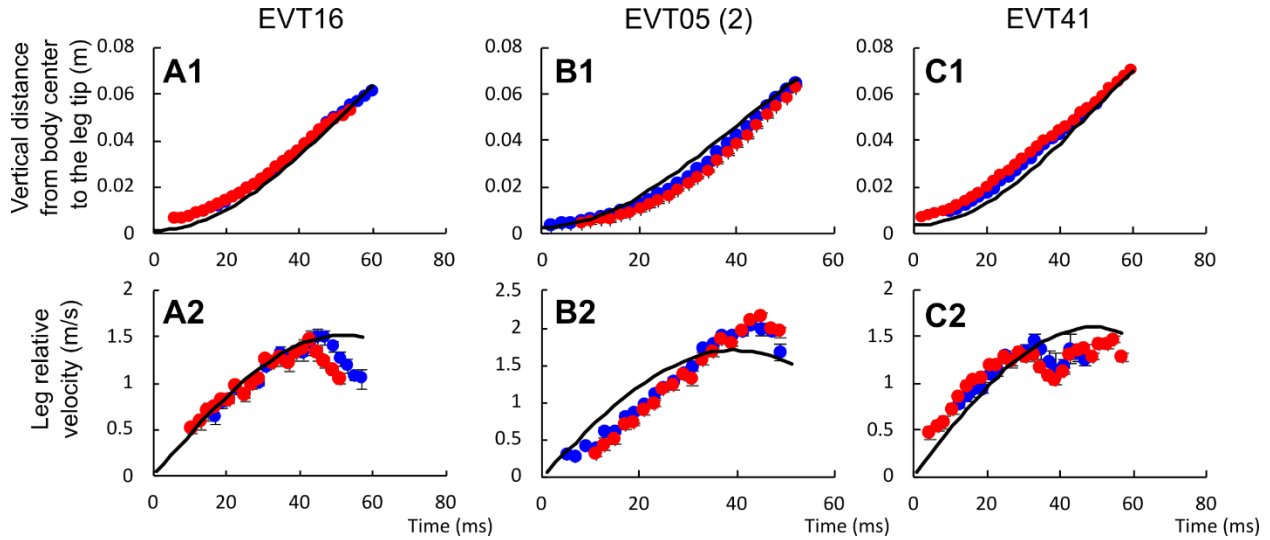


**Fig. S19. The model results (simulations of separate jumps based on empirically measured input into the model) compared to the empirically observed trajectories for individual jumps of *G. gigas* females and *P. tigrina*.** (A, B, C) - The theoretical model results and empirical results for the jumps of *G. gigas* females in movies EVT28, EVT33, and EVT35. (D, E, F) - The theoretical model results and empirical results for the jump videos of *P. tigrina*: C0046, C0049, and C0066. Horizontal axis represents time (ms); Vertical axis represents height of body center above water surface (mm). Blue line indicates model results and orange circles represent empirically measured values.

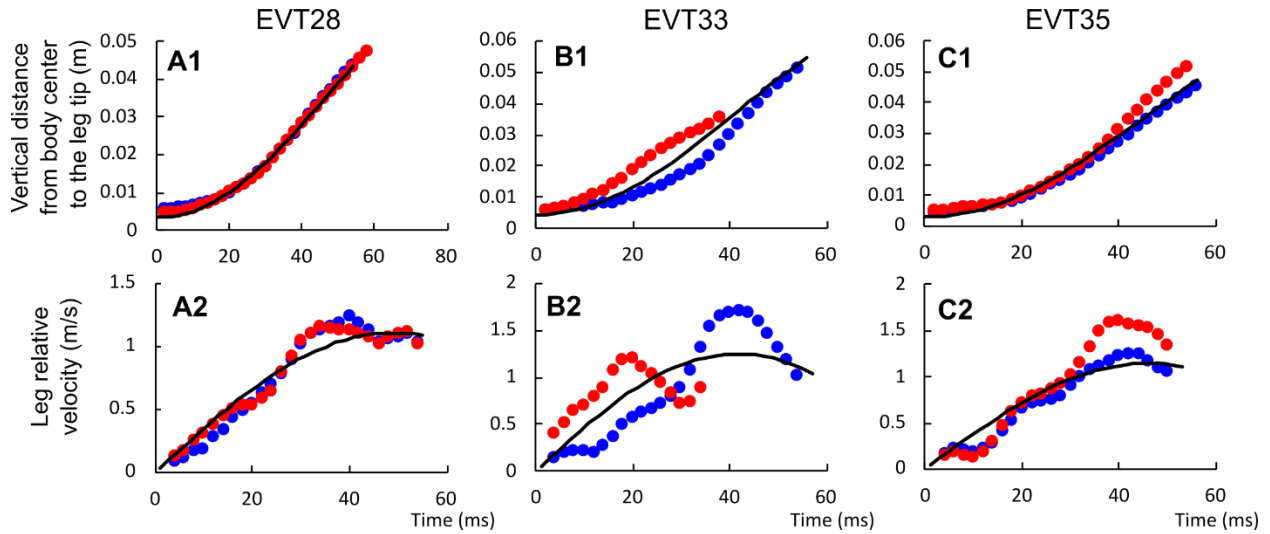
## Supplementary Materials PART 14: Validation of the use of empirical constant angular velocity of the middle leg rotation, $\omega_e$ .

One of the model's simplifying assumptions is that the angular downward midleg movement occurs at a constant angular velocity that can be determined from empirical data on leg and body coordinates from the videos under certain assumptions described in Yang et al. (1), where it was shown to be acceptably close to the empirical average of angular velocity and resulted in valid conclusions regarding the surface tension jumps in small and medium size water striders. This angular velocity of middle leg rotation,  $\omega_e$ , is empirically derived from basic observations of jump kinematics under the assumption that the empirically measured linear downward velocity of wetted midleg relative to water surface,  $v_l$ , can be approximated by the simple formula:  $v_l = \omega(l_l - y_i)\sin(2\omega t) - \dot{y}$ , while the vertical distance from the tip of the legs to the body center,  $l_s$ , can be approximated by another formula:  $l_s = \Delta l[1 - \frac{1}{2}\cos(2\omega t) + y_i]$  (see Yang et al. (1) and Supplementary Materials PART 19 for more details). To validate our use of the same procedure for determining the simple value of constant angular velocity of middle leg rotation,  $\omega_e$ , we compared the empirically observed leg movements in specific jumps where in reality the leg angular velocity of rotation vary during a jump with the theoretical leg movements calculated using the constant value of  $\omega_e$  extracted from each video separately. We did this for 3 jumps from each size class: *G. gigas* male, *G. gigas* female, and *P. tigrina* (data from Fig. 3, S13, S14, S15). The results suggest an approximate reasonable agreement between observed and theoretically predicted profiles of leg tip distance to body and leg tip relative velocity during jumps performed by relatively synchronized symmetrical movements by the left and right midleg.

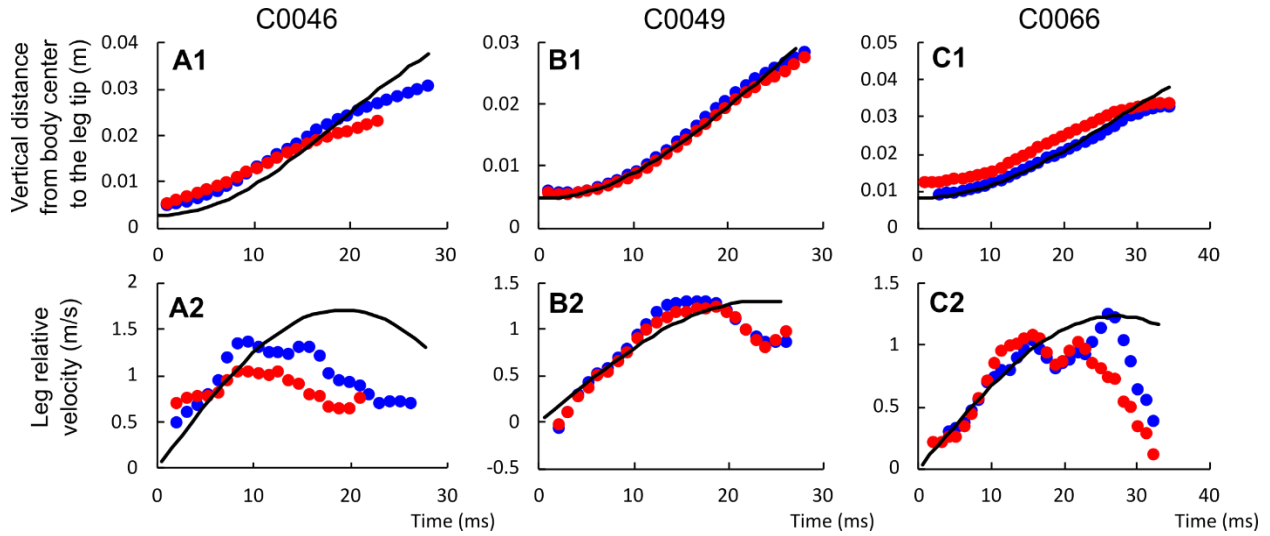
In order to determine the theoretical performance for "virtual" water strider jumps that do not occur in nature we calculated the three hypothetical angular midleg velocities,  $\omega_t$ , that are theoretically expected in the hypothetical situations of the three large classes using surface tension jumps and in the hypothetical situation of *A. paludum* using drag-involving jump. For the former, we first extracted  $\omega_e$  values from the clips of jumps of *A. paludum*, which resulted in the range of  $\omega_e$  between 23-41 rad/s (n = 7, Table S9). This corresponds to 56-99% [calculated as  $(\omega_e/\omega_c)\cdot 100\%$ ] of the theoretical critical midleg angular velocity,  $\omega_c$ , for *A. paludum* (marked as  $\omega_c$  in Fig. 5) at which the water surface breaks. Then, we decided that the best feasible estimates of the hypothetical surface tension jumps' performance by the three large water strider classes are represented by the performance for the range of the midleg angular velocity corresponding to 56-99% of  $\omega_c$  for each of the three classes of large water striders (i.e., the range of  $\omega_t$  is from  $0.56\omega_c$  to  $0.99\omega_c$ ). Similarly, we calculated theoretical performance in the hypothetical drag-involving jumps by *A. paludum* assuming the range of angular midleg velocities calculated as corresponding to the hypothetical midleg angular velocity ( $\omega_t$ ) range from  $1.13\omega_c$  to  $1.69\omega_c$  (1.13 is the average of the three lowest  $\omega_e/\omega_c$  ratio, and 1.69 is the average of the three highest  $\omega_e/\omega_c$  ratio for the three classes of large water striders calculated from the empirically based  $\omega_e$  and from the theoretically calculated  $\omega_c$  for each of the three classes separately; n = 6 for each class, Table S9).



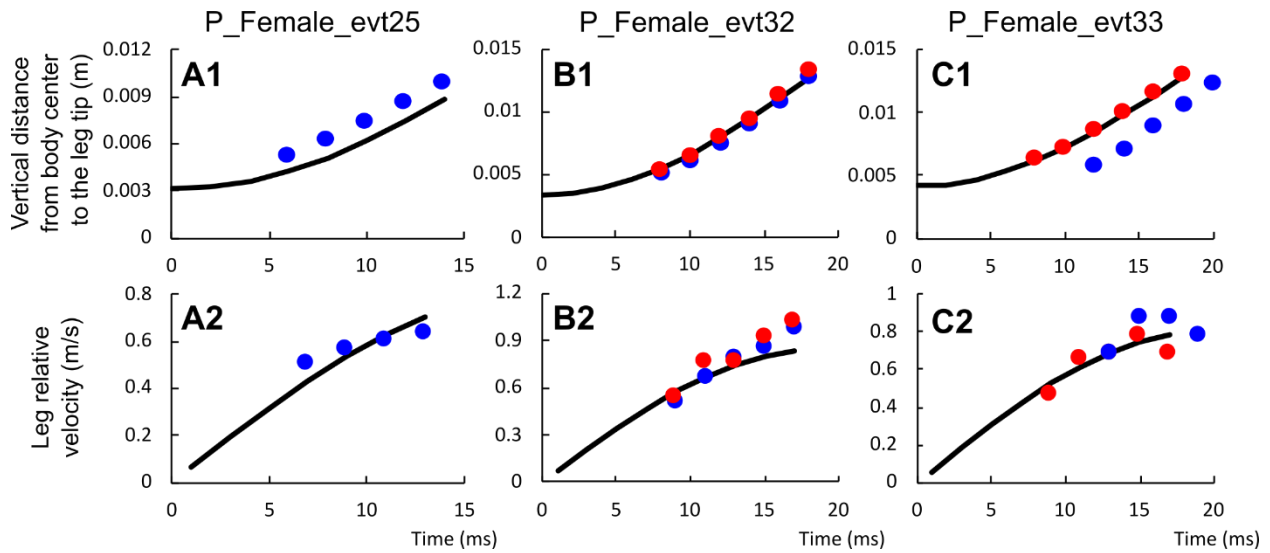
**Fig. S20.** Three examples of the comparison of theoretical predictions based on constant midleg angular velocity,  $\omega_e$ , extracted from the video analysis according to (1) with empirically derived variables directly measured from the video of water striders (*G. gigas* male), who naturally use midleg angular velocity that varies during the course of a jump. (A1, B1, C1) – The profile of the vertical distance from body center to the leg tip in jumps by *G. gigas* males; (A2, B2, C2) – The profile of the velocity of the leg relative to the body center in jumps of *G. gigas* males. Data from videos EVT16 (A1, A2), EVT05 (2) (B1, B2), and EVT41 (C1, C2). Red dots indicate left leg and blue dots indicate right leg.



**Fig. S21.** Three examples of the comparison of theoretical predictions based on constant midleg angular velocity,  $\omega_e$ , extracted from the video analysis according to (1) with empirically derived variables directly measured from the video of water striders (*G. gigas* female), who naturally use midleg angular velocity that varies during the course of a jump. (A1, B1, C1) – The profile of the vertical distance from body center to the leg tip in jumps by *G. gigas* females; (A2, B2, C2) – The profile of the velocity of the leg relative to the body center in jumps of *G. gigas* females. Data from videos EVT28 (A1, A2), EVT33 (B1, B2), and EVT35 (C1, C2). Red dots indicate left leg and blue dots indicate right leg.



**Fig. S22.** Three examples of the comparison of theoretical predictions based on constant midleg angular velocity,  $\omega_e$ , extracted from the video analysis according to (1) with empirically derived variables directly measured from the video of water striders (*P. tigrina*), who naturally use midleg angular velocity that varies during the course of a jump. (A1, B1, C1) – The profile of the vertical distance from body center to the leg tip in jumps by *G. gigas* males; (A2, B2, C2) – The profile of the velocity of the leg relative to the body center in jumps of *G. gigas* males. Data from videos C0046 (A1, A2), C0049 (B1, B2), and C0066 (C1, C2). Red dots indicate left leg and blue dots indicate right leg.

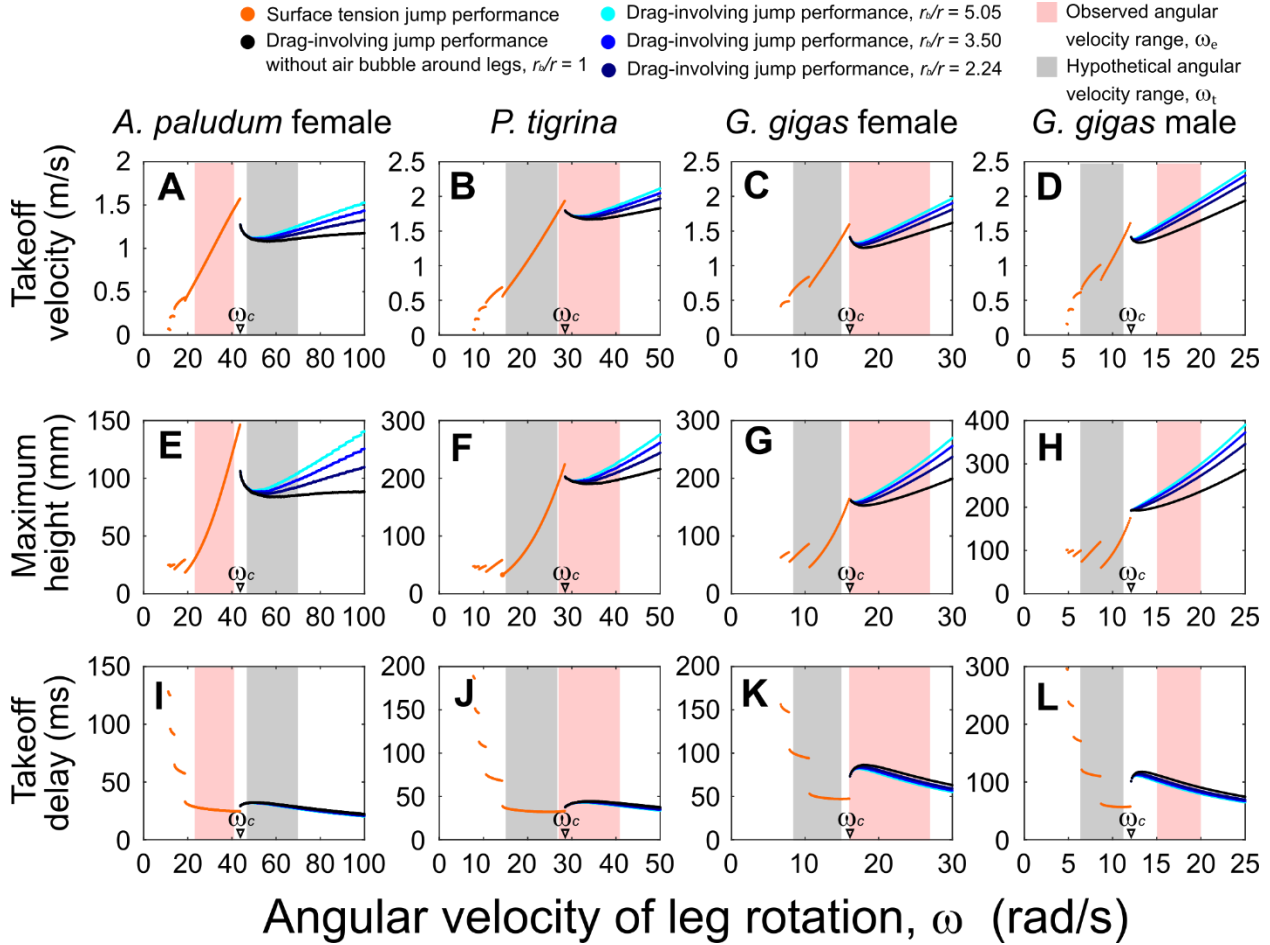


**Fig. S23.** Three examples of the comparison of theoretical predictions based on constant midleg angular velocity,  $\omega_e$ , extracted from the video analysis according to (1) with empirically derived variables directly measured from the video of water striders (*A. paludum* female), who naturally use midleg angular velocity that varies during the course of a jump. (A1, B1, C1) – The profile of the vertical distance from body center to the leg tip in jumps by *G. gigas* males; (A2, B2, C2) – The profile of the velocity of the leg relative to the body center in jumps of *G. gigas* males. Data from videos P\_Female\_evt25 (A1, A2), P\_Female\_evt32 (B1, B2), and P\_Female\_evt33 (C1, C2). Red dots indicate left leg and blue dots indicate right leg. We also extracted the values of constant empirical angular velocity of leg rotation,  $\omega_e$  (1), in these jumps in order to use the values in Fig. 5, 6 as the indicators of the range of values of midleg angular velocity by this species. Only one leg was digitized in P\_Female\_evt25 since the other was not visible.

**Table S9.** Calculated empirical angular velocity of leg rotation,  $\omega_e$ , for 6-7 jumps analyzed in details for each size class.

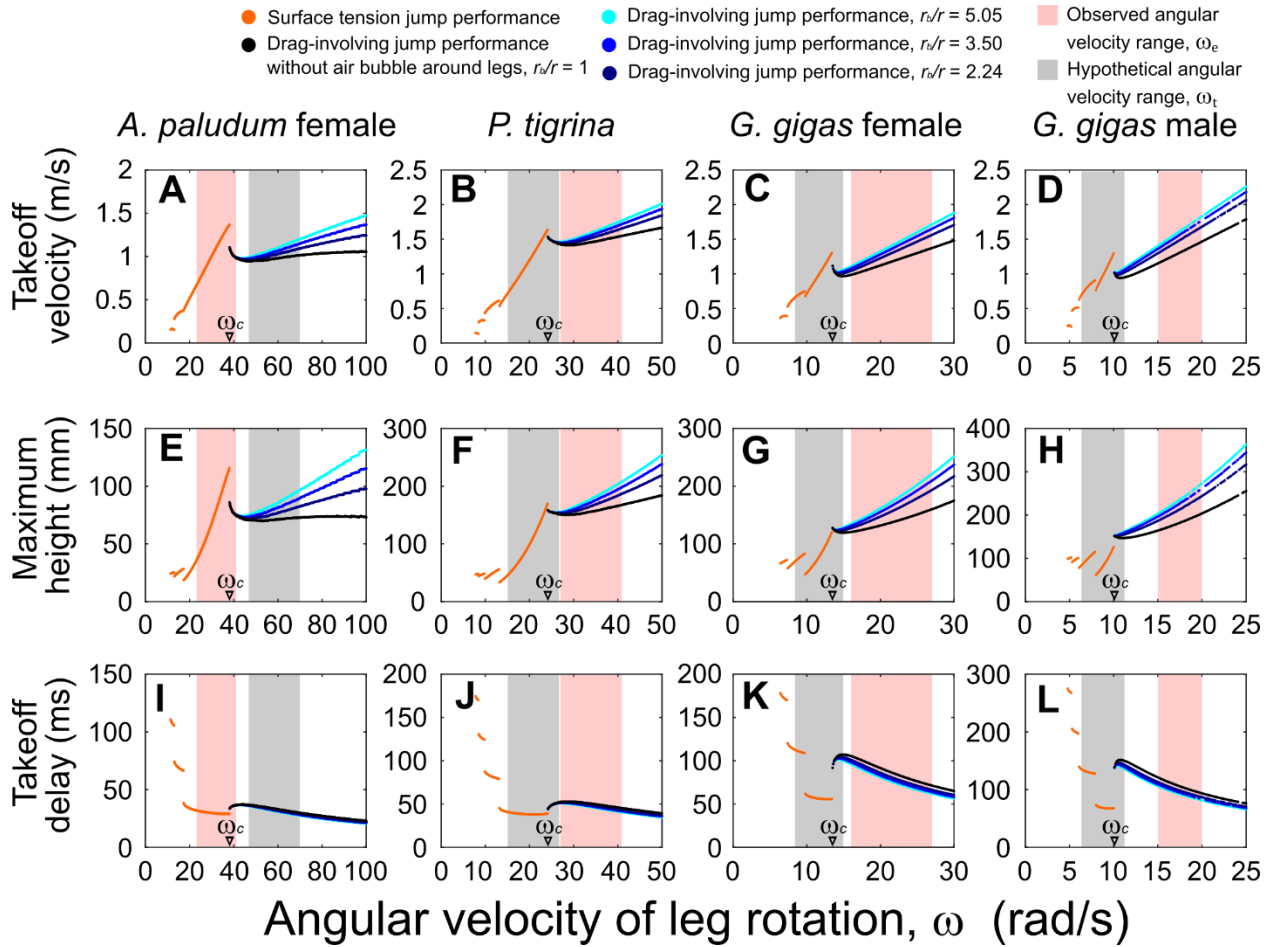
Species/sex	Individual	Mass (mg)	Video	Empirical angular velocity of leg rotation, $\omega_e$
<i>G. gigas</i> male	19	374.76	EVT05 (2)	20
<i>G. gigas</i> male	20	483.23	EVT16	15
<i>G. gigas</i> male	12	315.64	EVT39	19
<i>G. gigas</i> male	13	325.41	EVT41	16
<i>G. gigas</i> male	3	424.01	EVT70 (2)	15
<i>G. gigas</i> male	4	404.27	EVT75	16
<i>G. gigas</i> female	8	315.64	EVT03	19
<i>G. gigas</i> female	8	315.64	EVT05	27
<i>G. gigas</i> female	21	305.67	EVT28	16
<i>G. gigas</i> female	11	226.81	EVT31	25
<i>G. gigas</i> female	11	226.81	EVT33	19
<i>G. gigas</i> female	11	226.81	EVT35	17
<i>P. tigrina</i>	1	134	C0044	31
<i>P. tigrina</i>	1	134	C0045	29
<i>P. tigrina</i>	1	134	C0046	41
<i>P. tigrina</i>	1	134	C0049	33
<i>P. tigrina</i>	2	106	C0061	27
<i>P. tigrina</i>	3	123	C0066	29
<i>A. paludum</i> female	1113	45.2	P_Female_evt1,2	33
<i>A. paludum</i> female	1113	45.2	P_Female_evt3,4	27
<i>A. paludum</i> female	1114	48.5	P_Female_evt7,8	27
<i>A. paludum</i> female	1114	48.5	P_Female_evt25,26	39
<i>A. paludum</i> female	2111	42.6	P_Female_evt31,32	40
<i>A. paludum</i> female	2111	42.6	P_Female_evt33,34	41
<i>A. paludum</i> female	2113	54.2	P_Female_evt35,36	23

**Supplementary Materials PART 15:** Additional simulation results for different Young's modulus of insect cuticle.



**Fig. S24. Theoretically predicted jump performance as a function of midleg angular velocity for four classes of water striders' body size based on *A. paludum* females, *P. tigrina*, *G. gigas* females, and *G. gigas* males when  $E = 15$  GPa.** Jump performance measured by three variables calculated by the model: takeoff velocity (A-D), maximum jump height (E-H), takeoff delay (I-L). Average empirical values (mass, leg length for each leg section, leg radius, initial height of the body; average values are shown in Tables S1, S3) for each body size class were used to simulate the jumps for each body size class across a wide range of angular velocity of leg rotation ( $x$ -axis). Orange dots represent surface tension jumps, and the other colors of dots represent drag-involving jumps. The performances of drag-involving jumps were calculated for various size of air bubble surrounding the leg. The radius ratio of 5.05, 3.5, 2.24, and 1 (i.e., no bubble situation) are represented as light blue, blue, dark blue, and black dots, respectively. The red vertical shades represent the ranges of the observed leg angular velocity ( $\omega_e$ ). The gray vertical shades represent the range of the hypothetical leg angular velocity ( $\omega_t$ ) for *A. paludum* using drag in their jumps, and for the other large species using surface tension jumps. The angular velocity of leg rotation,  $\omega_e$ , values were determined from slow motion jumping videos as explained in the Supplementary Materials PART 14 and the values are listed in Table S9.

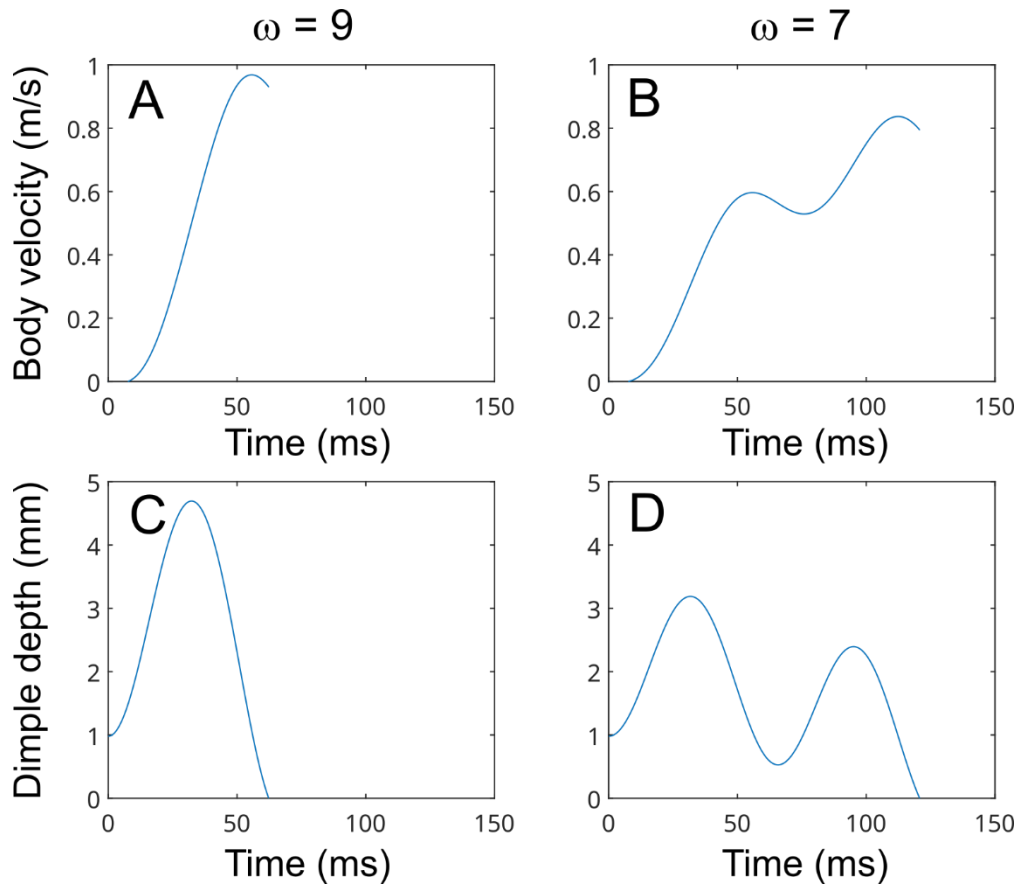




**Fig. S25. Theoretically predicted jump performance as a function of midleg angular velocity for four classes of water striders' body size based on *A. paludum* females, *P. tigrina*, *G. gigas* females, and *G. gigas* males when  $E = 5$  GPa.** Jump performance measured by three variables calculated by the model: takeoff velocity (A-D), maximum jump height (E-H), takeoff delay (I-L). Average empirical values (mass, leg length for each leg section, leg radius, initial height of the body; average values are shown in Tables S1, S3) for each body size class were used to simulate the jumps for each body size class across a wide range of angular velocity of leg rotation ( $x$ -axis). Orange dots represent surface tension jumps, and the other colors of dots represent drag-involving jumps. The performances of drag-involving jumps were calculated for various size of air bubble surrounding the leg. The radius ratio of 5.05, 3.5, 2.24, and 1 (i.e., no bubble situation) are represented as light blue, blue, dark blue, and black dots, respectively. The red vertical shades represent the ranges of the observed leg angular velocity ( $\omega_e$ ). The gray vertical shades represent the range of the hypothetical leg angular velocity ( $\omega_t$ ) for *A. paludum* using drag in their jumps, and for the other large species using surface tension jumps. The angular velocity of leg rotation,  $\omega_e$ , values were determined from slow motion jumping videos as explained in the Supplementary Materials PART 14 and the values are listed in Table S9.

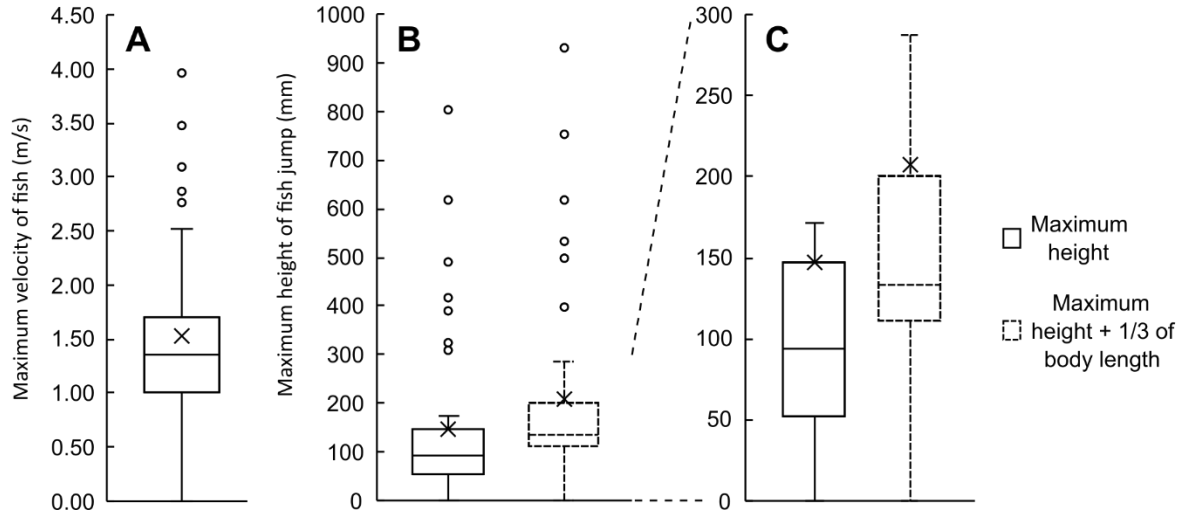
**Supplementary Materials PART 16:** Examples from the model simulations of the repeated “cycle” of dimple depth and body velocity fluctuations.

The simulation results show that the performance of surface tension jumps (takeoff velocity, maximum height, and takeoff delay) for the lower range of the angular velocity of leg movement has discontinuities as the angular velocity of leg rotation changes (Fig. 5). We propose the following explanation of this phenomenon (see details in Fig. S26). During a jump, the dimple depth under insect's leg is initially getting deeper, leading to larger upward force which causes faster upward movement of the body. As the body ascends, the dimple depth becomes shallower because the leg is pulled upward from the water surface at a faster speed than the downward leg rotation. This leads to the weaker upward force causing decrease of body upwards acceleration to the point when gravitation slows the upward speed of the body, allowing the legs to “catch up” and to start pushing against the water surface increasing the dimple and the force. This repeated “cycle” of dimple depth and body velocity fluctuations can happen several times depending on the angular velocity of leg rotation. The takeoff velocity, maximum height, and takeoff delay change in an abrupt manner between jumps with different numbers of those cycles. These discontinuities do not happen if the downward leg rotation is sufficiently fast to always counteract the upward body velocity until the near end of the jump.



**Fig. S26. Examples of model simulation illustrating a repeated “cycle” of dimple depth and body velocity fluctuations during relatively short angular midleg velocities (b, d) compared to the changes of dimple depth and body velocity for larger angular leg velocity for water striders’ body size based on *G. gigas* males.** The figure illustrates body velocity (A, B) and dimple depth (C, D) of jumps when the angular velocities of leg rotation are 9 (A, C) and 7 (B, D). When the angular velocity of leg rotation is not high enough (B, D), one “cycle” cannot generate sufficient force for takeoff, causing the body to decelerate before takeoff (B) and resulting in the deepening of the dimple again (D). This phenomenon causes performance discontinuities of surface tension jump in Fig. 5, S24, and S25. These discontinuities do not happen if the downward leg rotation is sufficiently fast to always counteract the upward body velocity until the near end of the jump (A, C) The final performance of these jumps in (A, C/B, D) is illustrated in Fig. 5D.

**Supplementary Materials PART 17: Maximum jumping performance of fish.**



**Fig. S27. The calculated hypothetical maximum performance of fish based on the literature on fish movement speeds (4).** (A) Maximum velocity achieved by fish in the water; (B, C) the estimated hypothetical height of jumping fish assuming that a fish of a given body length moves vertically upward with the body velocity recorded in the literature (shown in A) and calculated according to the formula explained in Supplementary Materials PART 10. The height from the water surface is represented by solid lines. The height including 1/3 of body length is represented by dashed lines by assuming fish lose their thrust when 1/3 of their body came out from the water.

**Supplementary Materials PART 18: Weber number of the study species: *Gigantometra gigas*, *Ptilomera tigrina*, and *Aquarius paludum*.**

**Table S10.** Weber number of jumps respective to each size classes (same analyzed jumps from Fig. 6A). Calculation method for the Weber number was implemented from (5).

Size class	Video	$\rho$ (kg/m <sup>3</sup> )	$\sigma$ (N/m)	$w$ , Basal tibia thickness (m)	$U$ (m/s)	$We = \rho U^2 w / \sigma$ (5)
<i>G. gigas</i> male	EVT05 (2)	998	0.072	0.00039	0.60	1.95
<i>G. gigas</i> male	EVT16	998	0.072	0.000455	0.49	1.51
<i>G. gigas</i> male	EVT41	998	0.072	0.000475	0.52	1.78
<i>G. gigas</i> female	EVT28	998	0.072	0.000405	0.39	0.85
<i>G. gigas</i> female	EVT33	998	0.072	0.00036	1.17	6.83
<i>G. gigas</i> female	EVT35	998	0.072	0.00036	0.46	1.06
<i>P. tigrina</i>	C0046	998	0.072	0.000261	0.73	1.93
<i>P. tigrina</i>	C0049	998	0.072	0.000261	0.65	1.53
<i>P. tigrina</i>	C0066	998	0.072	0.000327	0.51	1.18
<i>A. paludum</i> female	P_Female_evt25	998	0.072	0.000176	0.09	0.02
<i>A. paludum</i> female	P_Female_evt32	998	0.072	0.000194	0.28	0.21
<i>A. paludum</i> female	P_Female_evt33	998	0.072	0.000194	0.32	0.28

**Supplementary Materials PART 19: Detailed description of the mathematical model of jumping.**  
**p. 34-44.**

**I. Introduction**

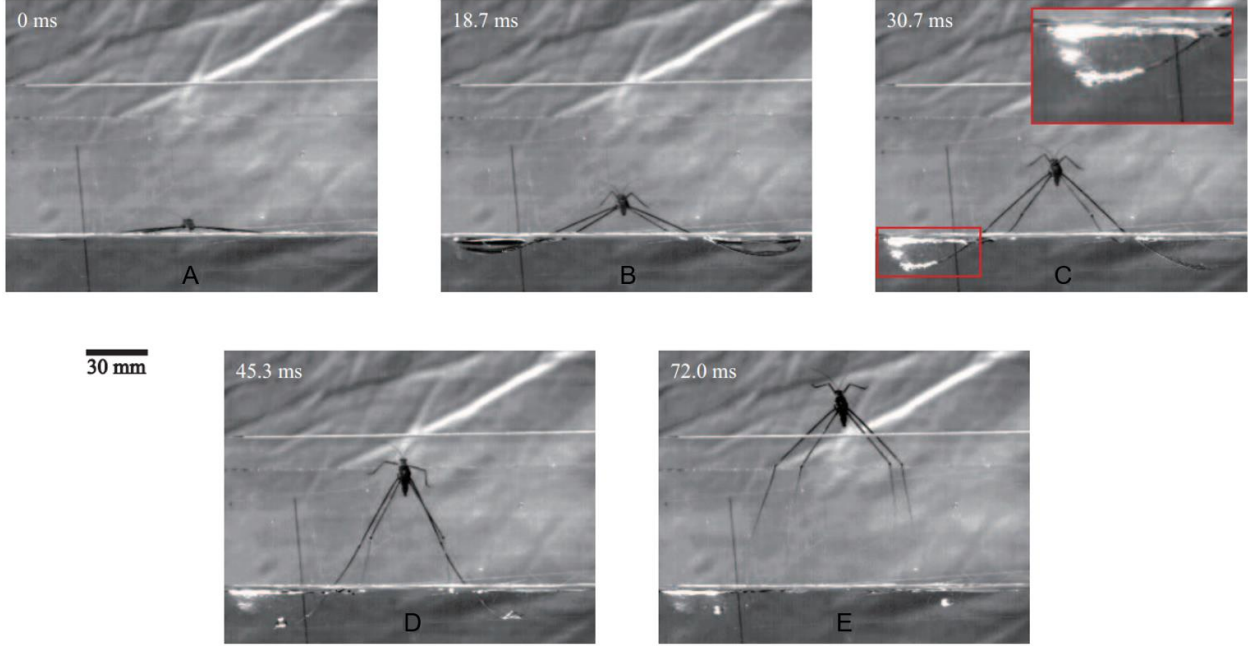
The mechanics of jumping of mid-sized Palearctic water striders, such as *Gerris latiabdominis*, *G. gracilicornis*, *Aquarius remigis* and *A. paludum* (Fig. S28A) on water has been previously studied (6). It has been shown that their leg stroke speeds are optimized to maximize their jumping speed and minimize time to take off given their mass and leg length (1), and that individual water strider are able to adjust their angular velocity of midlegs based on previous jumping experience (7). By pressing the water surface until just before it breaks under water strider legs, these typically studied water striders make a full use of capillary forces that the water surface provides.

Water strider legs may be approximated as long thin cylinders (see also Supplementary Materials Part 7: Fig. S10, 11 for link to empirically measured leg diameter and length). The surface is pierced when a very thin cylinder of a radius  $r \ll l_c$  is pressed downward against the water surface in a quasi-static manner to a distance of the order of the capillary length  $l_c = [\sigma/(\rho g)]^{1/2}$  with  $\sigma$  and  $\rho$  respectively being the surface tension coefficient and density of water, and  $g$  being the gravitational acceleration. When the legs sink into the water surface, the drag forces act on the legs, which are significantly smaller than the capillary forces for the mid-sized striders.

While the mid-sized water striders do not break water surfaces for efficient jumps, the larger species such as *Gigantometra gigas* (Fig. S28B) do not follow the aforementioned rule of motion in jumping. *G. gigas* is up to ten times heavier than mid-sized water striders in leg length. Typical mass and middle leg length of *G. gracilicornis* (Fig. S28A) are respectively 30 mg and 20 mm, whereas the giant water striders are up to 500 mg and 100 mm for *Gigantometra gigas* (Fig. S28B). Figure S29 shows a sequence of the jump of a *G. gigas* on water taken by a high-speed camera in a field experiment. We see that the middle legs pierce the water surface to a significant degree, which is not observed for mid-sized striders. Here, we describe the kinematic models of the two pairs of legs separately, and combine the models to predict the jump dynamics of the *G. gigas* and other water striders with similar jumping behavior.



**Fig. S28. Two different-sized water striders and basic parameters.** (A) A mid-sized water strider, *Gerris gracilicornis*. (B) A gigantic water strider, *Gigantometra gigas*. (C) A side view of a *G. gigas* during its jump with parameters used in the theoretical model. Symbols and variables used in the model are explained in Table S11 and Fig. S32.



**Fig. S29. A sequence of the jump of *G. gigas* on water.** (A) The initial posture of the *G. gigas* before jumping. (B) Surface tension phase. The middle and hind legs create dimples on the water surface. (C) The early stage in the drag phase. The middle legs break the water surface with air bubbles covering the legs (magnified image) until they reach the deepest location. (D) The late stage in the drag phase. The air bubbles surrounding the middle legs are absent. (E) Gravity driven phase. All the legs are completely disengaged from the water surface.

## II. Kinematics of middle and hind legs

First, we consider the kinematics of middle legs. We assume that their movements comprise three phases: the surface tension phase, the transition phase, and the drag phase. In the surface tension phase, the middle legs push the water surface down with a constant wetted length,  $l_m$  (the length of tibia plus tarsus of the middle leg). Symbols and variables used in the model are explained in Table S11 and Fig. S32 in part IV. The dimple depth generated by the middle leg,  $h$ , grows, leading to the increase of the body center height,  $y$ , with time,  $t$  (Fig. S28C). As the angular velocity of midleg's downward rotation can be approximated to be a constant,  $\omega$  (1), the downward linear velocity of the middle leg relative to the body center,  $v_m$ , can be written as:

$$v_m = \dot{l}_s = \omega(l_l - y_i) \sin(2\omega t), \quad (1)$$

where  $l_s = y + h$  is the vertical distance from the body center to the tip of the leg.  $l_l$  is the entire length of the leg consisting of femur, tibia, and tarsus, and  $y_i$  is the initial height of the body centre from the undisturbed free surface. Integrating  $v_m$  over time,  $t$ , gives:

$$l_s = \frac{1}{2}(l_l - y_i)[1 - \cos(2\omega t)] + y_i \text{ for } l_s = y_i \text{ at } t = 0. \quad (2)$$

Based on empirical leg measurements, we model the wetted middle legs as cylinders of diameter,  $d$ , and length,  $l_m$ , according to the details described in the Supplementary Materials PART 7. The water surface cannot withstand the depression of cylindrical legs when the dimple reaches a critical depth,  $h_c$ , which was determined by empirical measurement for different wetted leg length (Fig. S13A, Supplementary

Materials PART 8). When the dimple depth,  $h = l_s - y$ , exceeds  $h_c$  at time  $t_c$ , in the model, then the wetted part of the middle leg starts to pierce the water surface, entering the transition phase. In this phase, there are both sunk and unsunk part of middle leg. The unsunk part is supported by surface tension, while sunk part experiences drag. We assumed that the proportion of wetted leg for surface tension,  $p_s$ , and for drag,  $p_d$ , gradually changes from only surface tension to only drag, i.e., from the start of sinking to completely sunk leg. The duration of this changing proportion was determined by empirical measurement (Fig. S14, Supplementary Materials PART 8). After the transition phase, the drag phase begins at time  $t_d$ . During this third phase, the middle legs can only provide drag.

To calculate drag in both transition and drag phase, the middle legs are considered almost straight with the wetted length decreasing according to formula:

$$l_1 = l_l - \frac{y}{\cos\left(\frac{\pi}{2} - \omega t\right)}, \quad (3)$$

that takes into account the ascent of the insect body. The downward linear velocity of a middle leg relative to the water surface is then given by:

$$v_l = \dot{l}_s - \dot{y} = v_m - \dot{y} = \omega(l_l - y_l) \sin(2\omega t) - \dot{y}. \quad (4)$$

Because the legs penetrate the water with a high velocity, an air bubble forms around the leg, as shown in Fig. S29C. We assume in the model that the air bubble detaches after the moment when the middle legs reach the deepest point in the water. Thus, the effective frontal area, the projected area of the leg with its diameter,  $d$ , along its moving velocity, is  $A_f = d_b l_1$ , thanks to the presence of an air bubble that increases the cylindrical leg diameter, to  $d_b$  (“ $b$ ” stands for bubble of air) by the factor of 2.24–5.05 times ( $d_b = 3.5 * d$  in average value) as determined in empirical measurements (see Supplementary Materials PART 7: Table. S7).

We turn to the kinematics of hind legs which do not pierce the water surface during the jump. The stroke can be decomposed into two phases. In the first (pushing) phase, the hindlegs push the water surface down with a fully contacted constant wetted length,  $l_h$  (the length of tibia plus tarsus of the hind leg), with a growing dimple depth. We assume in the model that the depth of dimple created by a hind leg from the undisturbed free surface,  $h_h$ , grows at the same rate as dimple of the midleg until it reaches constant depth,  $h_{hm}$ . Constant depth of hindlegs is calculated using observed empirical maximum depth of hindlegs,  $h_{hE}$ , and wetted length of hindlegs assuming leg as half of an arc (see details in Supplementary Materials PART 9).

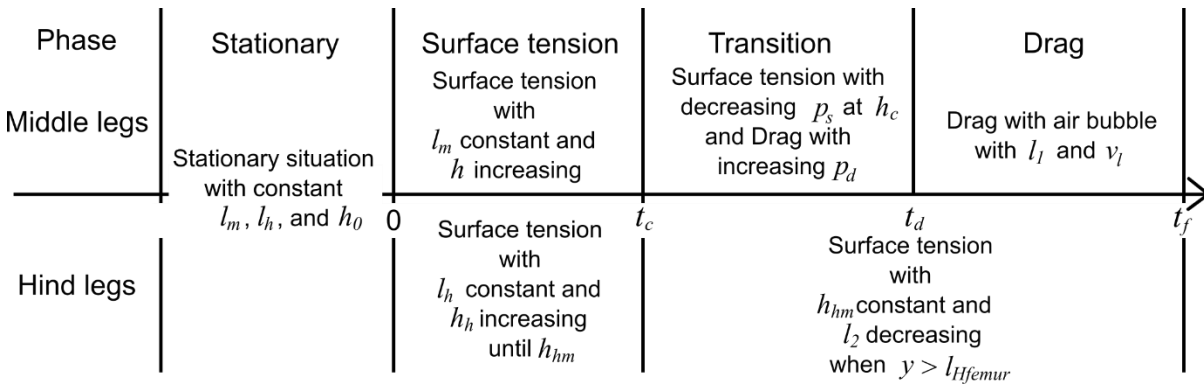
In the second phase, which starts when the dimple depth reaches its constant,  $h_{hm}$ , the legs slide on the water surface towards the body while detaching themselves from the surface. Thus, the wetted length eventually decreases by ascending the body while the dimple depth is constant. We calculate the wetted length of a hind leg,  $l_2$ , based on body heights,  $y$ , constant wetted length of a hind leg,  $l_h$ , and femur length of a hind leg,  $l_{Hfemur}$ . We use a simplifying assumption that the hindlegs that are out of the water align with femur along the direction of jump and are being dragged out from the water surface vertically (Fig. S30, Supplementary Movie 1), while the hindleg section on the water surface is bent creating a dimple without surface breaking. Therefore, the wetted length of a hind leg approximately follows:

$$l_2 = l_h - (y - l_{Hfemur}) \text{ when } y > l_{Hfemur} \text{ and } l_h > (y(t) - l_{Hfemur}). \quad (5)$$



**Fig. S30. Field jump of *G. gigas*.** Field jump of *G. gigas* shows its hindlegs are almost vertical when the wetted length is pulled out from the water surface. Red arrows mark the femur-tibia joint.

Summarizing the simplified kinematics of both middle and hind legs in the model, we schematically plot the timeline of different phases of the jump for the four legs as shown in Fig. S32. In the stationary phase,  $t = 0$ , both middle and hindlegs are in stationary situation with initial dimple depth,  $h_0$ . In the surface tension phase,  $0 < t < t_c$ , both the middle and hind legs moving with angular velocity,  $\omega$ , are pushing the water surface with growing of dimple, and only dimple depth of hind leg,  $h_h$ , stops growing when it reaches specific depth,  $h_{hm}$ . In the transition phase,  $t_c < t < t_d$ , where  $t_d$  is the moment when the breaking ends, the unsunk part of the middle leg is supported by surface tension, while the sunk part experiences drag. The proportion of the sunk and unsunk length of the middle legs changes gradually during this phase. In the drag phase,  $t_d < t < t_f$ , where  $t_f$  is the moment of take-off, the middle legs continue to move in water with an angular velocity,  $\omega$ , and are surrounded by air bubbles. The hind legs are being closed on the water surface with their wetted length being decreased with constant dimple depth,  $h_{hm}$ .



**Fig. S31.** Timeline of the simulated phases of the jump for the middle and hind legs. Middle and hind legs contribute force resulting from surface tension to the jump until the critical moment of time when water surface is broken,  $t_c$ . After this moment of time, middle legs of diameter,  $d_b$ , resulting from the presence of the air bubble, create drag force until the moment,  $t_f$ . Between the moment of  $t_c$  and  $t_d$ , middle legs utilize surface tension and drag with unsunk and sunk parts, respectively. After  $t_d$ , the dimple under the middle legs is completely broken, and the middle legs exploit drag only. Hindlegs create force resulting from surface tension during the whole period from  $t_c$  to  $t_f$ . This force gradually decreases as the wetted leg length,  $l_2$ , decreases, while dimple depth,  $h_{hm}$ , is assumed constant.

### III. Jump dynamics of *Gigantometra gigas*

#### SURFACE TENSION PHASE

Symbols and variables used in the model, including geometric schematics for some of the variables, are explained in Table S11 and Fig. S32 in part IV. The water strider ascends from the water surface because the interaction of its legs and water produces upward thrust. Newton's second law of motion dictates  $F = m\ddot{y}$ , where  $F$  is the total force acting on the water strider legs and  $m$  is the water strider mass. We find the temporal evolution of the body center height and the take-off velocity by analyzing the forces produced by the movement of legs of angular velocity,  $\omega$ .

During the "Surface tension phase" (Fig. S32) of the simplified jump, various forces are exerted on the legs including the capillary force  $F_c \sim \sigma l_w$ , pressure force  $F_p \sim \rho U^2 dl_w$ , buoyancy  $F_b \sim \rho g d h l_w$ , added inertia  $F_a \sim \rho d^2 l_w U^2 / h$ , viscous force  $F_v \sim \mu r l_w U / l_c$ , and the weight of the water strider (for the large *G. gigas* males it is  $\sim 5$  mN). Here,  $l_w$  is the wetted leg length, and  $U$  is the rate of the vertical growth of dimple, which is a direct consequence of downward linear velocity of the middle leg,  $v_l$  that according to formula (4) depends on, among others, on the leg angular velocity,  $\omega$ .

Using the typical values for middle legs  $d = 260 \mu\text{m}$ ,  $l_w = 53.5 \text{ mm}$ ,  $h = 5 \text{ mm}$ , and  $U = 0.4 \text{ ms}^{-1}$ , we found that the capillary force dominates the other forces, and we decided to ignore the other forces in the simplified model.

The capillary force acting on a pair of floating flexible cylinders is given by formula 6 below, which is a modified formula from Yang et al. (1) based on model for a cylinder by Vella et al. (3).

$$F_c = 4C\rho g l_c l_w h \left[ 1 - \left( \frac{h}{il_c} \right)^2 \right]^{1/2}, \quad (6)$$

where  $C$  is the flexibility factor depending on the scaled leg length  $L_f = l_w / l_e$ . Here,  $l_e = (Bl_c / \sigma)^{1/4}$  is the modified elastocapillary length of the leg with the bending rigidity  $B = \pi E d^4 / 64$  and  $E$  being Young's modulus of insect cuticle. We approximate  $C \approx (1 + 0.082L^{3.3})^{-1}$  for  $L_f < 2$  and  $C \approx (0.88L)^{-1}$  for  $L_f > 2$ . In comparison to the original model of Yang et al. (1), we modified the denominator in the formula 6 from  $2l_c$  to  $il_c$ , by introducing the index of maximum dimple depth,  $i = h_M / l_c$ . The maximum dimple depth at surface breaking moment,  $h_M$ , was empirically derived for water striders of different sizes using the linear regression of  $h_M$  on the constant wetted length of midleg ( $h_M = 0.1227l_m + 0.004$ ; Fig. S13B, Supplementary Materials PART 8). This index allowed us to extend the range of the dimple depths beyond the mathematical limitation of  $h \leq 2l_c$  from the original model (1).

We first model the stationary situation, "Stationary phase" (Fig. S31). We assume the stationary dimple depth of each individual by calculating force balance between gravity and surface tension. When the water strider is on the water surface using their two middle legs and two hind legs, the stationary dimple depth,  $h_0$ , satisfies the following formula by assuming the same dimple depth for middle and hind legs:

$$mg = 4\rho g l_c \left\{ C_{m0} l_m h_0 \left[ 1 - \left( \frac{h_0}{il_c} \right)^2 \right]^{1/2} + C_{h0} l_h h_0 \left[ 1 - \left( \frac{h_0}{il_c} \right)^2 \right]^{1/2} \right\}. \quad (7)$$

In the surface tension phase, the dimple depth is given by  $h = l_s - y$ , leading us to write  $\ddot{h} = \ddot{l}_s - (F - g) / m$ . Here,  $F$  is the sum of the capillary forces acting on the middle and hind legs:



$$F = 4\rho g l_c \left\{ C_m l_1 h \left[ 1 - \left( \frac{h}{il_c} \right)^2 \right]^{1/2} + C_h l_2 h_h \left[ 1 - \left( \frac{h_h}{il_c} \right)^2 \right]^{1/2} \right\}. \quad (8)$$

This gives a second-order nonlinear differential equation for  $h$  with the initial conditions of  $h(t = 0) = h_0$  and  $\dot{h}(t = 0) = 0$ , which we solve using Matlab. Then we get the body centre height  $y = l_s - h$  as a function of time for  $0 < t < t_c$  (i.e.,  $h < h_c$ ).

## TRANSITION PHASE

Once the middle legs start to pierce the water surface,  $t > t_c$  (i.e.,  $h > h_c$ ; where  $h_c$  is empirically established for each water strider size; Fig. S13A), the middle legs experience the drag force  $F_d$  of water in addition to the capillary force. The drag force acting on a pair of middle legs moving with the velocity  $v_l = \omega(l_l - y_l) \sin(2\omega t) - \dot{y}$  as obtained above is given by

$$F_d = \rho C_D A_f v_l^2, \quad (9)$$

where  $C_D = 0.8$  is the drag coefficient on the flexible cylinder (8), taken to be about 30% lower than the value for a rigid cylinder at a Reynolds number,  $Re = \frac{\rho v_l d}{\mu} \approx 100$ . We simply assumed that the drag coefficient of the middle legs is the same as that of a solid cylinder. This is because calculating the exact drag coefficient of the middle legs would require detailed analysis of the movement of air inside the bubble around the leg and between hairs, which is beyond the scope of our study. The frontal area is  $A_f = d_b l_1$  in transition and drag phase,  $t_c < t < t_f$ .

During the transition phase ( $t_c < t < t_d$ ), the middle legs utilize both capillary and drag forces as the legs progressively sink. We assumed that the leg sinks continuously during a certain breaking duration,  $D_b$ , which was calculated from the wetted length using linear regression of empirical measurements (Fig. S14, Supplementary Materials PART 8). Thus, the functional wetted leg length for each force is linearly changed by introducing the proportion of wetted leg length for utilizing surface tension,  $p_s$ , and for drag,  $p_d$  ( $p_s + p_d = 1$ ). During the breaking duration,  $D_b$ , the proportion of wetted leg length for utilizing surface tension,  $p_s$ , linearly decreases from 1 to 0, while the proportion of wetted leg length for utilizing drag,  $p_d$ , linearly increases from 0 to 1. For a given moment, we write  $p_s = (t_c + D_b - t)/D_b$  and  $p_d = 1 - p_s$ . In this phase, the dimple depth for capillary force is fixed at  $h_c$  since we observed that the breaking of the dimple expands laterally (as shown in Fig. S12 in Supplementary Materials PART 8).

Then the total force acting on the middle and hind legs becomes

$$F = 4\rho g l_c C_m p_s l_1 h_c \left[ 1 - \left( \frac{h_c}{il_c} \right)^2 \right]^{1/2} + \rho C_D d_b p_d l_1 v_l^2 + 4C\rho g l_c l_2 h_h \left[ 1 - \left( \frac{h_h}{il_c} \right)^2 \right]^{1/2}. \quad (10)$$

## DRAG PHASE

In the drag phase, after the dimple is completely broken,  $t > t_d$ , the proportion of wetted leg for utilizing surface tension,  $p_s$ , becomes 0 and middle leg utilize drag only.

Then the total force acting on the middle and hind legs naturally becomes

$$F = \rho C_D A_f v_l^2 + 4C\rho g l_c l_2 h_h \left[ 1 - \left( \frac{h_h}{il_c} \right)^2 \right]^{1/2}. \quad (11)$$

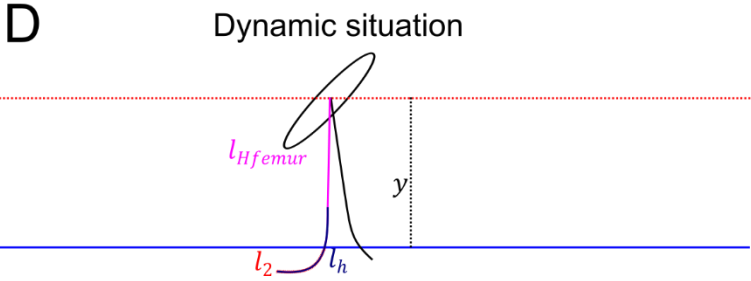
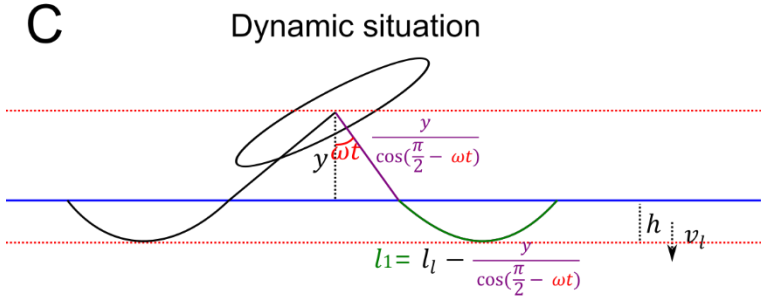
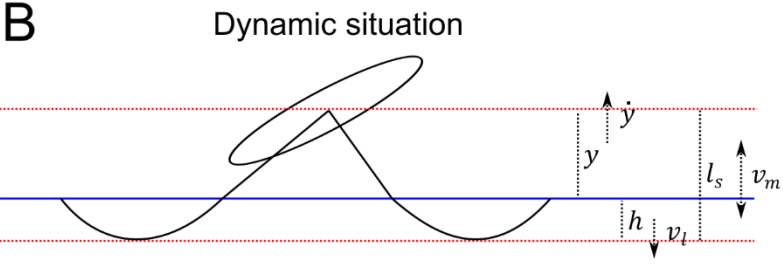
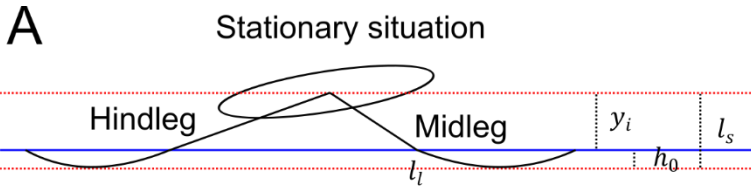
In the transition and drag phase, solving  $\dot{y} = (F - g)/m$ , a second-order differential equation with  $A_f$ ,  $v_l$ ,  $l_2$ ,  $h_h$  being functions of  $y$  and  $t$ , gives the body center height versus time. The initial conditions are provided from the results of the surface tension phase. From the relationship between the body center height versus time we predict time of take-off,  $t_f$ , and body speed at  $v_f$ . From the body speed and body mass, we predict that maximum jump height above the water surface as  $H_m = y_i + \frac{v_f^2}{2g}$  (Supplementary Materials PART 11). These model predictions can be calculated for various vales of angular leg velocities, and for water striders of various body mass and leg lengths.

#### IV. Explanations of the symbols used in the paper

The symbols and variable names used in the model are listed here in Table S11, and additionally some of them are shown in a graphical schematic in Fig. S32. The font colors in the Table S11 correspond to the colors used in the Fig. S32.

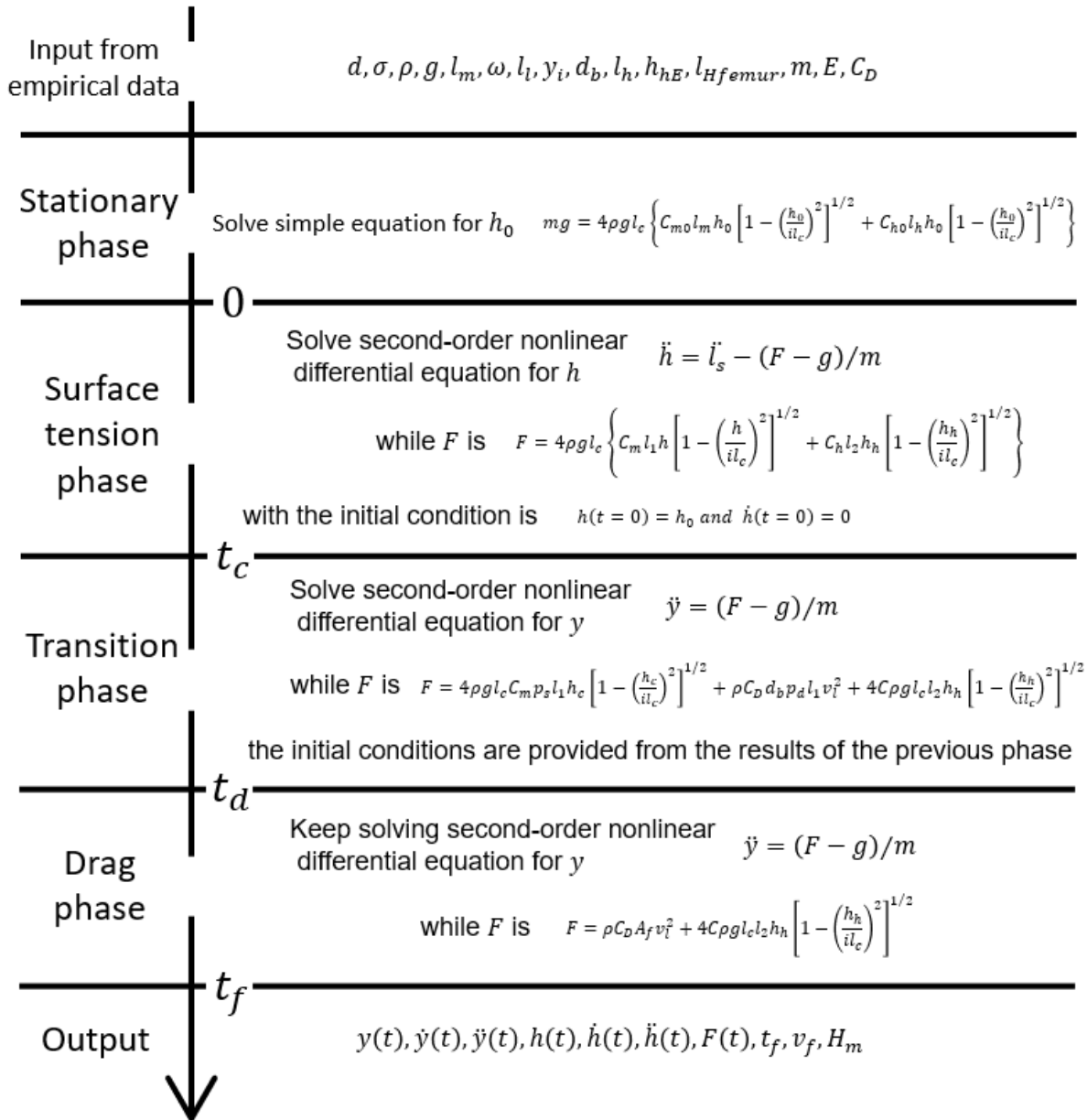
Table S11. Explanations of the symbols in the model	
$r$	Radius of legs as cylinder
$\sigma$	Surface tension coefficient of water
$\rho$	Density of water
$g$	Gravitational acceleration
$l_c = [\sigma/(\rho g)]^{1/2}$	Capillary length
$l_w$	Wetted length of the leg
$l_l$	Entire length of the middle leg consisting of femur, tibia, and tarsus
$l_m$	Constant wetted length of middle leg (the length of tibia plus tarsus of the middle leg)
$l_h$	Constant wetted length of hind leg (the length of tibia plus tarsus of the hind leg)
$l_{Hfemur}$	Femur length of hind leg
$l_2$	Dynamic wetted length of a hind leg
$l_s = y + h$	Vertical distance from the body center to the tip of the leg
$l_1 = l_l - y/\cos(\pi/2 - \omega t)$	Decreased wetted length of middle leg for ascent of the body
$l_e = (Bl_c/\sigma)^{1/4}$	Modified elastocapillary length of the leg
$h$	Dynamic dimple depth generated by the middle leg
$h_c$	Critical dimple depth
$h_o$	Constant dimple depth at stationary situation
$h_M$	Maximum dimple depth at surface breaking moment
$h_B$	The breaking point depth
$h_h$	Dynamic dimple depth created by a hind leg
$h_{hE}$	Maximum dimple depth of hind leg by empirical observations
$h_{hm}$	Constant dimple depth of hind leg derived from $h_{hE}$
$i$	Index of maximum dimple depth; $il_c = h_M$
$t$	Time
$t_c$	Critical moment of the start of water surface breaking
$t_d$	Last moment of complete water surface breaking
$t_f$	Moment of take-off
$D_b$	Duration of dimple breaking
$p_s$	The proportion of wetted leg for utilizing surface tension (i.e., proportion of the length of unsunk part from total wetted leg length); $p_s = (t_c + D_b - t)/D_b$
$p_d$	The proportion of wetted leg for utilizing drag (i.e., proportion of the length of sunk part from total wetted leg length); $p_d = 1 - p_s$
$y$	Body center location on vertical coordinate axis
$\dot{y}$	Time derivative of $y$ in Newtonian calculus notation; vertical speed of body center
$y_i$	Initial height of the body center from the undisturbed free surface
$m$	Mass of the water strider
$r$	Radius of the wetted middle leg as a cylinder
$r_b$	Radius of the wetted middle leg as a cylinder surrounded by the air bubble
$A_f$	Projected area of the leg

$\omega$	Angular velocity of middle leg rotation of a jump
$\omega_e$	Derived angular velocity of middle leg rotation in a jump under the assumption that empirically measured linear downward velocity of wetted midleg relative to water surface, and the vertical distance from the body center can be approximated using a constant value of $\omega$ , by two formulae: $v_l = \omega(l_l - y_i)\sin(2\omega t) - \dot{y}$ , $l_s = \Delta l[1 - \frac{1}{2}\cos(2\omega t) + y_i]$ .
$\omega_t$	Hypothetical velocity of midleg rotation of the hypothetical jumps (i.e., surface tension jumps of <i>G. gigas</i> and <i>P. tigrina</i> ; drag-involving jump of <i>A. paludum</i> )
$v_m$	Downward linear velocity of the middle leg relative to the body center
$v_f$	Take-off velocity
$v_l = \omega(l_l - y_i)\sin(2\omega t) - \dot{y}$	Downward linear velocity of a middle leg relative to the water surface
$U$	Rate of the vertical growth of dimple
$\mu$	Dynamic viscosity
$F_c$	Capillary force
$F_p$	Pressure force
$F_b$	Buoyancy
$F_a$	Added inertia
$F_v$	Viscous force
$L_f = l_w/l_e$	Scaled leg length
$B = \pi E d^4/64$	Bending rigidity
$E$	Young's modulus of insect cuticle
$C$	Flexibility factor; function of wetted length of a leg, $l_w$ , and its bending rigidity, $B$
$C_{m0}$	Middle leg flexibility factor; function of wetted length of a middle leg, $l_m$ , and its bending rigidity, $B$
$C_{h0}$	Hind leg flexibility factor; function of wetted length of a hind leg, $l_h$ , and its bending rigidity, $B$
$C_m$	Middle leg flexibility factor; function of wetted length of a middle leg, $l_1$ , and its bending rigidity, $B$
$C_h$	Hind leg flexibility factor; function of wetted length of a hind leg, $l_2$ , and its bending rigidity, $B$
$C_D$	Drag coefficient
$Re$	Reynolds number
$H_m$	Maximum height of the jump
$\Delta l_l = l_l - y_i$	Maximal downward reach of the middle leg
$L$	Downward stroke; dimensionless maximal reach of the average of four legs
$\Omega = \omega(l_c/g)^{1/2}$	Dimensionless angular velocity of the average four legs' rotation of a jump
$M = m/(\rho l_c^2 C l_w)$	Dimensionless index of insect body mass with respect to the leg; body mass with respect to maximal water mass can be displaced by the average of four legs
$L_m = \Delta l_l/l_c$	Midleg downward stroke; dimensionless maximal reach of the middle leg
$\Omega_m = \omega_e(l_c/g)^{1/2}$	Dimensionless angular velocity of middle leg rotation of a jump
$M_m = m/(\rho l_c^2 C_{m0} l_m)$	Dimensionless index of insect body mass with respect to the middle leg; body mass with respect to maximal water mass can be displaced by the middle leg



**Fig. S32. Schematics of geometric parameters.** Geometric parameters used in the mathematical model in stationary situation (A) and dynamic situations (B, C, D). (A) illustrates stationary phase with initial height,  $y_i$ , initial dimple depth,  $h_0$ . (B) illustrates dynamic variables during jumping situations: surface tension, transition, and drag phase. (C) illustrates the functional leg length for drag calculation in formula 3. Please note that while the drawing (C) shows a bent leg for dimple depth,  $h$ , and downward velocity,  $v_t$ , the leg length for drag,  $l_1$ , was assumed to be a solid cylinder. (D) illustrates hindleg's dynamic wetted length,  $l_2$ , in formula 5.

## V. Model diagram



**Fig. S33. Simplified diagram of model workflow.** After input of the empirical data, in the stationary phase, initial dimple depth,  $h_0$ , is calculated by solving simple equation for providing initial condition for the surface tension phase. In the surface tension phase,  $h$ ,  $y$ , and  $F$  are calculated in the range of  $0 < t < t_c$ , by solving second-order nonlinear differential equation for  $h$ . In the transition and drag phase,  $h$ ,  $y$ , and  $F$  are calculated in the range of  $t_c < t < t_f$ , by solving second-order nonlinear differential equation for  $y$ . The initial condition of the transition phase is fixed by calculation of the surface tension phase. Model provides distribution of body height,  $y$ , dimple depth,  $h$ , force,  $F$ , by time and take-off time,  $t_f$ , take-off velocity,  $v_f$ , and maximum height,  $H_m$ . The model simulations were conducted in Matlab. The Matlab code is available at <https://doi.org/10.5281/zenodo.7847879>.

## VI. Values of empirical parameters used in model simulations

Table S12. Empirical parameters used to model jump in each video that has been analyzed in detail.

Parameter/ variable (units)	<i>G. gigas</i> male			<i>G. gigas</i> female			<i>P. tigrina</i>		
	EVT05 (2)	EVT16	EVT41	EVT28	EVT33	EVT35	C0046	C0049	C0066
$\sigma$ (N/m)					0.072				
$\rho$ (kg/m <sup>3</sup> )					998				
$g$ (m/s <sup>2</sup> )					9.8				
$E$ (N/m <sup>2</sup> )					1e10				
$C_D$					0.8				
$r$ (m)	11.3e-5	13.1e-5	13.7e-5	11.7e-5	10.4e-5	10.4e-5	7.5e-5	7.5e-5	9.4e-5
$\omega_e$ (rad/s)	20	15	16	16	19	17	41	33	29
$m$ (kg)	374.76e-6	483.23e-6	325.41e-6	305.67e-6	226.81e-6	226.81e-6	134e-6	134e-6	123e-6
$y_i$ (m)	0.00017	0.00165	0.00088	0.00333	0.00435	0.00274	0.00271	0.00473	0.00806
$l_l$ (m)	88.64e-3	102.69e-3	103.17e-3	72.59e-3	70.13e-3	70.13e-3	44.72e-3	44.72e-3	50.63e-3
$l_m$ (m)	45.78e-3	54.60e-3	54.05e-3	39.80e-3	38.87e-3	38.87e-3	22.70e-3	22.70e-3	25.56e-3
$l_h$ (m)	63.36e-3	79.48e-3	77.17e-3	44.21e-3	36.98e-3	36.98e-3	16.34e-3	16.34e-3	14.46e-3
$l_{Hfemur}$ (m)	42.74e-3	47.42e-3	48.24e-3	32.25e-3	31.11e-3	31.11e-3	24.30e-3	24.30e-3	28.88e-3
$h_{hE}$ (m)	0.0039	0.0032	0.0062		0.0062			0.0065	
$r_b = d_b/2$	28.5e-5	52.0e-5	48.2e-5				3.5r		

Table S13. Empirical parameters used in size-specific simulations.

Parameter/variable (units)	<i>G. gigas</i> male	<i>G. gigas</i> female	<i>P. tigrina</i>	<i>A. paludum</i> female
$\sigma$ (N/m)			0.072	
$\rho$ (kg/m <sup>3</sup> )			998	
$g$ (m/s <sup>2</sup> )			9.8	
$E$ (N/m <sup>2</sup> )			0.5e10, 1e10, 1.5e10	
$C_D$			0.8	
$r$ (m)	13.14e-5	11.21e-5	8.934e-5	5.128e-5
$m$ (kg)	413.7e-6	265.2e-6	115.4e-6	47.6e-6
$y_i$ (m)	0.900e-3	0.900e-3	5.17e-3	3.00e-3
$l_l$ (m)	101.9e-3	71.7e-3	47.9e-3	25e-3
$l_m$ (m)	53.5e-3	38.5e-3	23.9e-3	13.4e-3
$l_h$ (m)		73.5e-3	40.6e-3	19.1e-3
$l_{Hfemur}$ (m)		49.5e-3	32.1e-3	27.6e-3
$h_{hE}$ (m)		0.0041		0.0065
$r_b = d_b/2$			2.24r, 3.5r, 5.05r	0.0041

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